

How to perform an iterate of the power method (without matrices)?

$$M_n \cdot x_k = \begin{pmatrix} M_{11} & \dots & M_{1n} \\ \vdots & & \vdots \\ M_{n1} & \dots & M_{nn} \end{pmatrix} \begin{pmatrix} x_k^{(1)} \\ \vdots \\ x_k^{(n)} \end{pmatrix} =$$

$$= \begin{pmatrix} M_{11} x_k^{(1)} + \dots + M_{1j} x_k^{(j)} + \dots + M_{1n} x_k^{(n)} \\ \vdots \\ M_{n1} x_k^{(1)} + \dots + M_{nj} x_k^{(j)} + \dots + M_{nn} x_k^{(n)} \end{pmatrix} =$$

Obs if $g=0 \Rightarrow M_{ij} = 1/n \quad \forall i$

$$= \begin{pmatrix} \sum_{j|g_j \neq 0} M_{1j} x_k^{(j)} + \frac{1}{n} \sum_{j|g_j=0} x_k^{(j)} \\ \vdots \\ \sum_{j|g_j \neq 0} M_{nj} x_k^{(j)} + \frac{1}{n} \sum_{j|g_j=0} x_k^{(j)} \end{pmatrix} =$$

Consider $j \neq i \quad c_j \neq 0 \Rightarrow M_{ij} = \begin{cases} 0 & \text{if } g_{ij} = 0 \\ (n-m) \cdot \frac{1}{c_j} & \text{if } g_{ij} = 1 \end{cases}$

$$g_{ij} = 0 \Leftrightarrow \nexists \text{ link } \boxed{i} \rightarrow \boxed{j} \Leftrightarrow$$

$$\Leftrightarrow i \notin L_j$$

Implementation of one iterate of the power method:

$$xc = x$$

$$x = 0$$

for j in range $(0, n)$:

if $(c[j] == 0)$:

$$x = x + xc[j]/n$$

else:

$$x[L[j]] = x[L[j]] + xc[j]/c[j]$$

$$x = (1-m) \cdot x + m/n$$