431 Class 04

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Today's Agenda

- Look at the Five Questions posed during Class 03
- Make use of the data presented and cleaned in Class 03

From Class 03

Load packages and set theme

```
1 library(janitor)
2 library(patchwork)
3 library(tidyverse)
4
5 theme_set(theme_bw())
```

Read in data from .csv file

```
1 quicksur_raw <-
2 read_csv("c04/data/quick_survey_2022.csv", show_col_types = FALSE) |>
3 clean_names()
```

Manage the data into qsdat

Select variables

```
1 qsdat <- quicksur_raw |>
2     select(student, year, english, smoke,
3         pulse, height_in, haircut)
```

Change variable types

Where are we now?

```
1 summary(qsdat)
```

```
student
                               english
                                          smoke
                                                       pulse
                      year
Length: 494
                 2020
                        : 67
                                   :101
                                             : 456
                                                    Min. : 30.00
                               n
                 2016
                                         2 : 28
Class :character
                        : 64
                               v :390
                                                    1st Qu.: 65.00
                                         3 : 8
     :character
                 2019 : 61
                               NA's: 3
                                                    Median : 72.00
Mode
                  2021 : 58
                                         NA's:
                                                    Mean : 73.57
                  2022 : 54
                                                    3rd Ou.: 80.00
                  2018 : 51
                                                          :110.00
                                                    Max.
                  (Other):139
                                                    NA's
                                                          :75
 height in
                 haircut
Min. :57.00
               Min. : 0.00
1st Qu.:64.00
               1st Qu.: 14.00
Median :67.00
               Median : 20.00
Mean :67.33
               Mean
                    : 30.17
3rd Qu.:70.00
               3rd Qu.: 40.00
Max. :77.50
               Max. :250.00
1. T 7. I _.
```

Today's Questions

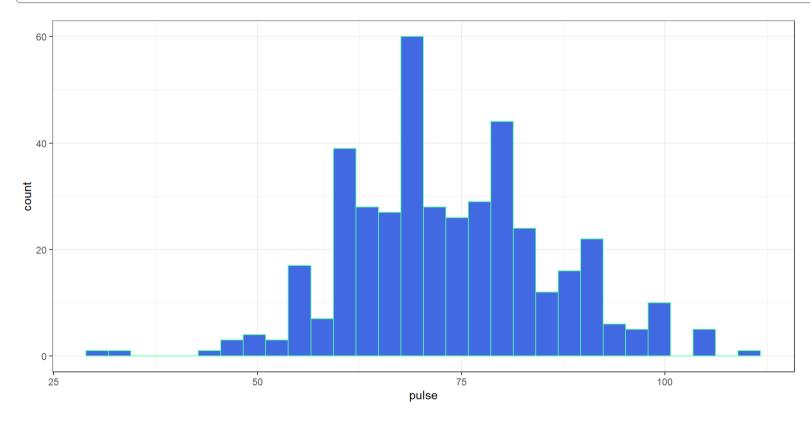
- 1. What is the distribution of pulse rates among students in 431 since 2014?
- 2. Does the distribution of student heights change materially over time?
- 3. Is a Normal distribution a good model for our data?
- 4. Do taller people appear to have paid less for their most recent haircut?
- 5. Do students have a more substantial tobacco history if they prefer to speak English or a language other than English?

Question 1 (Distribution of Student Pulse Rates)

Histogram, first try

What is the distribution of student pulse rates?

```
1 ggplot(data = qsdat, aes(x = pulse)) +
2 geom_histogram(bins = 30, fill = "royalblue", col = "seagreen1")
```



Describing the Pulse Rates

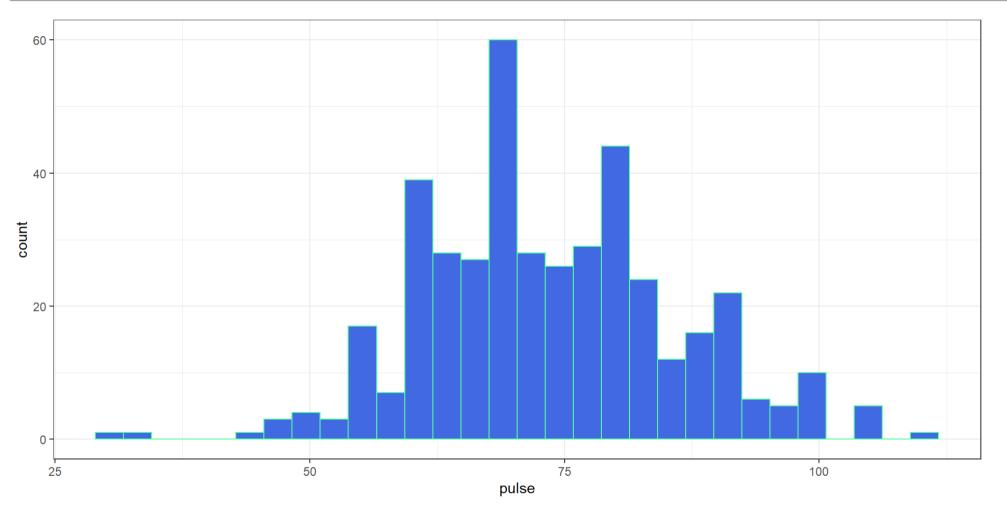
How might we describe this distribution?

- What is the center?
- How much of a range around that center do we see? How spread out are the data?
- What is the shape of this distribution?
 - Is it symmetric, or is it skewed to the left or to the right?

(Histogram is replotted on the next slide)

Histogram, first try again

```
1 ggplot(data = qsdat, aes(x = pulse)) +
2 geom_histogram(bins = 30, fill = "royalblue", col = "seagreen1")
```



Fundamental Numerical Summaries

```
1 qsdat |> select(pulse) |> summary()
    pulse
Min. : 30.00
1st Qu.: 65.00
Median : 72.00
Mean : 73.57
3rd Qu.: 80.00
Max. :110.00
NA's :75
```

- How do the summary statistics help us describe the data?
- Do the values make sense to you?

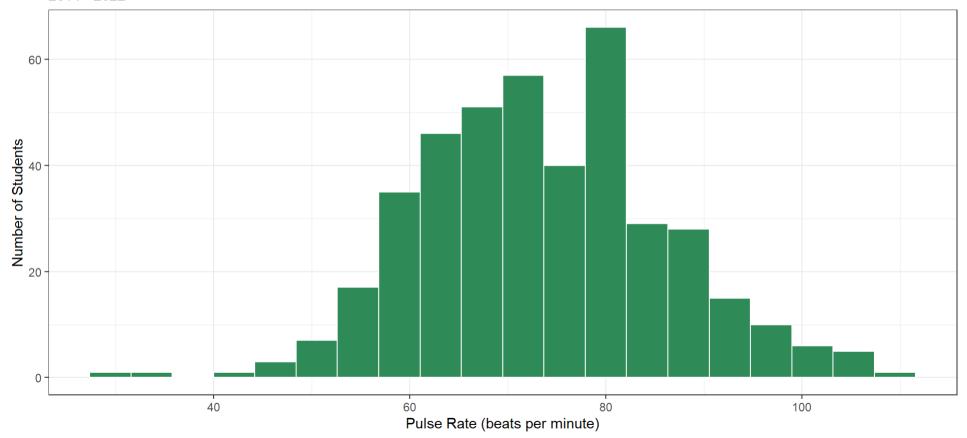
Histogram, version 2

- How did we deal with missing data?
- How did we add axis labels and titles to the plot?
- What is the distinction between fill and col?
- How many bins should we use?

Histogram, version 2

Pulse Rates of Dr. Love's students

2014 - 2022



Question 2 (Student Heights over Time)

Yearly Five-Number Summaries

```
1 qsdat |>
2    filter(complete.cases(height_in)) |>
3    group_by(year) |>
4    summarize(n = n(), min = min(height_in), q25 = quantile(height_in, 0.25)
5    median = median(height_in), q75 = quantile(height_in, 0.75),
6    max = max(height_in))
```

What should this produce? (Results on next slide)

Yearly Five-Number Summaries

```
# A tibble: 9 \times 7
               min
                      q25 median
                                   q75
 year
                                         max
 <fct> <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
1 2014
           40
                 60
                     64.8
                            68
                                  71
                                        73
2 2015
                     65
                            68
                               70
                                        74
                 61
3 2016
       64
                 60
                     64
                            67 70
                                        76
4 2017
          48
                 62
                     65
                            67 69
                                        77
5 2018
                     63
                              70
                                        7.3
          51
                 60
                            66
6 2019
                 57
                     65
                            68 70
                                        77.5
7 2020
          66
                 59
                     63
                            66 69.8
                                        76
8 2021
           55
                 60
                     64.5
                            67.5 71
                                        77.5
9 2022
           54
                 59
                     66
                            68.5
                                  70.4
                                        76
```

- Does the distribution of heights change materially in 2014-2022?
- What are these summaries, specifically?

Five-Number Summary

- Key summaries based on percentiles / quantiles
 - minimum = 0th, maximum = 100th, median = 50th
 - quartiles (25th, 50th and 75th percentiles)
 - Range is maximum minimum
 - IQR (inter-quartile range) is 75th 25th percentile
- These summaries are generally more resistant to outliers than mean, standard deviation
- Form the elements of a boxplot (box-and-whisker plot)

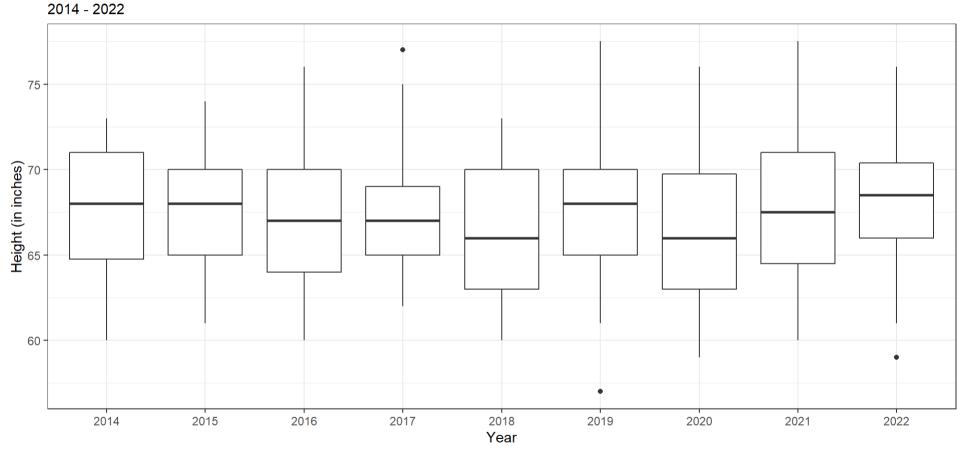
Comparison Boxplot of Heights by Year

```
1 dat2 <- qsdat |>
2    filter(complete.cases(height_in))
3
4 ggplot(data = dat2, aes(x = year, y = height_in)) +
5    geom_boxplot() +
6    labs(title = "Heights of Dr. Love's students, by year",
7    subtitle = "2014 - 2022", x = "Year", y = "Height (in inches)")
```

How did we deal with missing data here?

Comparison Boxplot of Heights by Year

Heights of Dr. Love's students, by year



Thinking about the Boxplot

- Box covers the middle half of the data (25th and 75th percentiles), and the solid line indicates the median
- Whiskers extend from the quartiles to the most extreme values that are not judged by **Tukey's** "fences" method to be candidate outliers
 - Fences are drawn at 25th percentile 1.5 IQR and 75th percentile + 1.5 IQR
- Are any values candidate outliers by this method? For which years?
- Was it important to change year to a factor earlier?

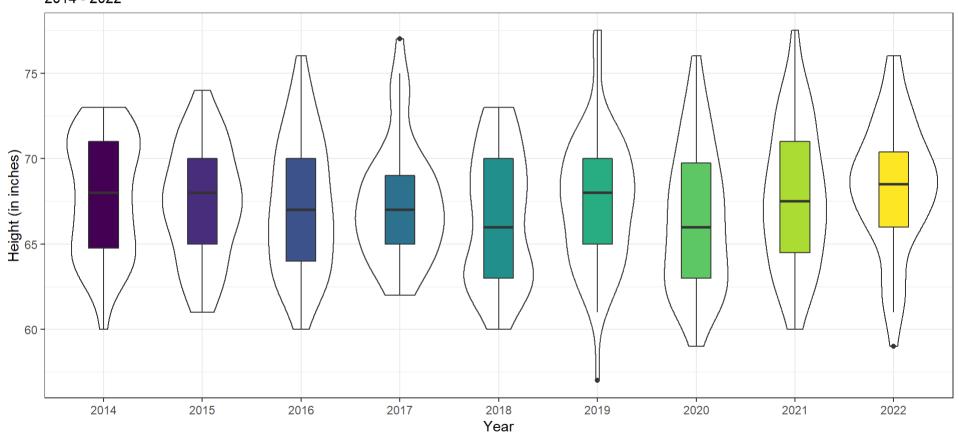
Adding a Violin to the Boxplot

 When we'd like to better understand the shape of a distribution, we can amplify the boxplot.

```
1 dat2 <- qsdat |>
2    filter(complete.cases(height_in))
3
4 ggplot(data = dat2, aes(x = year, y = height_in)) +
5    geom_violin() +
6    geom_boxplot(aes(fill = year), width = 0.3) +
7    guides(fill = "none") +
8    scale_fill_viridis_d() +
9    labs(title = "Heights of Dr. Love's students, by year",
10    subtitle = "2014 - 2022", x = "Year", y = "Height (in inches)")
```

Adding a Violin to the Boxplot

Heights of Dr. Love's students, by year 2014 - 2022



Thinking About our Boxplot with Violin

- How did we change the boxplot when we added the violin?
- What would happen if we added the boxplot first and the violin second?
- What does guides (fill = "none") do?
- What does scale_fill_viridis_d() do?

Table of Means and Standard Deviations

```
qsdat |>
       filter(complete.cases(height in)) |>
       group by (year) |>
       summarize(n = n(), mean = mean(height in), sd = sd(height in))
\# A tibble: 9 \times 4
                      sd
 year
           n mean
 <fct> <int> <dbl> <dbl>
          40 67.8 3.46
1 2014
2 2015 49 67.3 3.32
3 2016
      64 67.2 3.86
4 2017
          48 67.4 3.46
          51 66.5 3.81
5 2018
6 2019
          60 67.4 3.83
          66 66.4 4.09
7 2020
          55 67.8 4.13
8 2021
9 2022
          54 68.4 3.74
```

So, what do we think?

Are the distributions of student height very different from year to year?

- What output that I've provided here can help answer this question?
- What other things would you like to see?

Question 3 Can we assume that the Mean and SD are sensible summaries?

A Normal distribution (bell-shaped curve)

This is a Normal (or Gaussian) distribution with mean 150 and standard deviation 30.

Summarizing Quantitative Data

If the data followed a Normal model,

- we would be justified in using the sample mean to describe the center, and
- in using the sample standard deviation to describe the spread (variation.)

But it is often the case that these measures aren't robust enough, because the data show meaningful skew (asymmetry), or the data have lighter or heavier tails than a Normal model would predict.

The Empirical Rule for Approximately Normal Distributions

If the data followed a Normal distribution,

- approximately 68% of the data would be within 1 SD of the mean,
- approximately 95% of the data would be within 2 SD of the mean, while
- essentially all (99.7%) of the data would be within 3 SD of the mean.

Empirical Rule & 2022 Student Heights

In 2022, we had 54 students whose height_in was available, with mean 68.4 inches (173.7 cm) and standard deviation 3.7 inches (9.4 cm).

What do the histogram (next slide) and boxplot (seen earlier) suggest about whether a Normal model with this mean and standard deviation would hold well for these 54 student heights?

Histogram of 2022 Student Heights

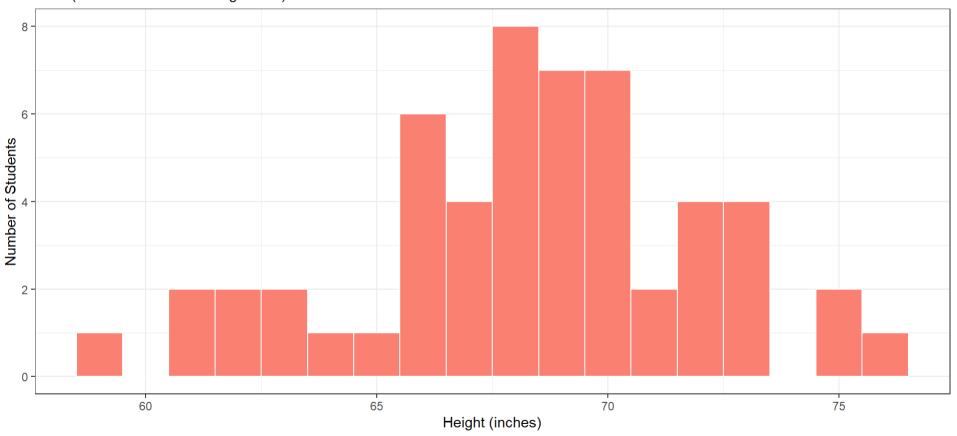
```
1 dat3 <- qsdat |>
2   filter(complete.cases(height_in)) |>
3   filter(year == "2022")
4
5   ggplot(data = dat3, aes(x = height_in)) +
6      geom_histogram(fill = "salmon", col = "white", binwidth = 1) +
7      labs(title = "Heights of Dr. Love's students",
8      subtitle = "2022 (n = 54 students with height data)",
9      y = "Number of Students", x = "Height (inches)")
```

- How did we use the two filter() statements?
- Why might I have changed from specifying bins to binwidth here?

Histogram of 2022 Student Heights

Heights of Dr. Love's students

2022 (n = 54 students with height data)



Checking the 1-SD Empirical Rule

- Of the 54 students in 2022 with heights, how many were within 1 SD of the mean?
 - Mean = 68.4, SD = 3.7.

0.7222222

 \bullet 68.4 - 3.7 = 64.7 inches and 68.4 + 3.7 = 72.1 inches

2-SD Empirical Rule

 How many of the 54 height_in values gathered in 2022 were between 68.4 - 2(3.7) = 61.0 and 68.4 + 2(3.7) = 75.8 inches?

3-SD Empirical Rule

 How many of the 54 height_in values gathered in 2022 were between 68.4 - 3(3.7) = 57.3 and 68.4 + 3(3.7) = 79.5 inches?

Empirical Rule Table for 2022 data

- \(\bar{x}\) = sample mean, \(s\) = sample SD
- For height_in: \(n\) = 54 with data, \(\bar{x} = 68.4, s = 3.7\)
- For pulse: \(n\) = 52 with data, \(\bar{x} = 75.4, s = 11.2\)

Range	"Normal"	height_in	pulse
\(\bar{x}	~68%	\(\frac{39}	\(\frac{43}
\pm s\)		{54}\) = 72.2%	{52}\) = 82.7%

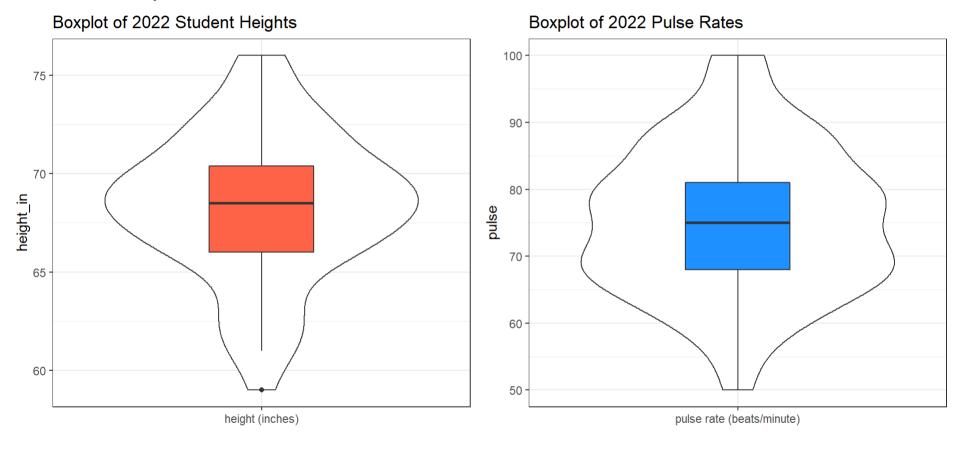
Boxplots of Height and of Pulse Rate

```
dat4 <- qsdat |> filter(complete.cases(height in), year == "2022")
   p4 \leftarrow qqplot(data = dat4, aes(x = "height (inches)", y = height in)) +
     geom violin() + geom boxplot(width = 0.3, fill = "tomato") +
     labs(title = "Boxplot of 2022 Student Heights", x = "")
   dat5 <- qsdat |> filter(complete.cases(pulse), year == "2022")
   p5 <- ggplot(\frac{data}{data} = \frac{dat5}{data}, aes(x = "pulse rate (beats/minute)", y = pulse))
     geom violin() + geom boxplot(width = 0.3, fill = "dodgerblue") +
10
     labs(title = "Boxplot of 2022 Pulse Rates", x = "")
11
12
13 p4 + p5 +
    plot annotation(title = "2022 Quick Survey Data")
14
```

- What is width = 0.3 doing? How about the x options?
- What am I doing with p3 + p4 + plot_annotation?
- What should this look like?

Boxplots of Height and of Pulse Rate

2022 Quick Survey Data



Normality and Mean/SD as summaries

If the data are approximately Normally distributed (like height_in and pulse) we can safely use the sample mean and standard deviation as summaries. If not "Normal", then ...

- The median is a more robust summary of the center.
- For spread, we often use the 25th and 75th percentiles.

A new quantitative variable

Let's look at haircut prices, across all years.

Does it seem like the Normal model will be a good fit for these prices?

- Why or why not?
- What more information do you need to make a decision?

2022 Haircut Prices

Unsorted

Sorted Counts

```
gsdat |> filter(year == "2022") |>
     select(haircut) |>
     as.vector() ## just to print it here horizontally
$haircut
             0 38
                   25
                            0 32
                                   60
                                       40
                                          45 52 52
                                                       0
                                                         30
                                                             15
                                                                 30 75
                       15
 [1]
         50
2.0
      4 45 20 35
                     0 50 25 40 240
                                       30
                                           6 45 25
                                                       2 30 25
                                                                 20 200
[20]
15
                                                      30
            20
                80
                    20
                       30
                           80
                               10
                                   50
                                       30
                                           60
                                              20
                                                  20
                                                             30
[39]
     35
```

2022 Haircut Prices, tabulated

```
1 qsdat |> filter(year == "2022") |> tabyl(haircut) |> adorn pct formatting()
haircut n percent
     0 5
           9.3%
        3.7%
     4 1 1.9%
     5 1 1.9%
        1.9%
    10 1 1.9%
    15 3 5.6%
    20 7
         13.0%
    25 4 7.4%
    30 8
        14.8%
    32 1 1.9%
    35 2 3.7%
    38 1 1.9%
    40 2 3.7%
           r /o
```

Normality of Haircut prices?

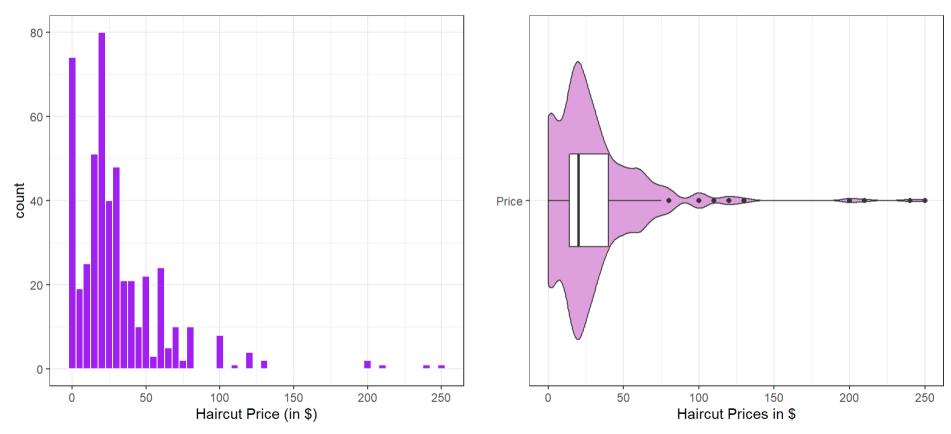
```
dat6 <- qsdat |> filter(complete.cases(haircut))
 2
   p6a <- qqplot(data = dat6, aes(x = haircut)) +
     geom histogram(binwidth = 5, fill = "purple", col = "white") +
    labs(x = "Haircut Price (in $)")
   p6b <- ggplot(data = dat6, aes(x = haircut, y = "Price")) +
     geom violin(fill = "plum") + geom boxplot(width = 0.3) +
     labs(y = "", x = "Haircut Prices in $")
10
   p6a + p6b +
12
    plot annotation (
  title = "Histogram and Boxplot of Haircut Prices",
1.3
1 4
       subtitle = "2014-2022 Students of Dr. Love in 431")
```

 Do you think that the distribution of these prices follows a Normal model?

Normality of Haircut prices?

Histogram and Boxplot of Haircut Prices

2014-2022 Students of Dr. Love in 431



Stem-and-Leaf of Haircut Prices

```
stem(qsdat$haircut, scale = 2) # scale makes plot twice as long as default
The decimal point is 1 digit(s) to the right of the |
  0000000000000000003555555558
  0000000000000000000022555
  000000000000000000000000055555
  000000002255
  000000000
8
9
  0000000
10 1 0000
```

• Note this is *not* a ggplot so it works differently than most plots we will make this term.

Empirical Rule Table for Haircut Prices

Let's look across all years, as well as just in 2022

```
1 mosaic::favstats(~ haircut, data = qsdat)
min Q1 median Q3 max
                     mean
                              sd
                                  n missing
         20 40 250 30.17214 31.4079 485
 0 14
1 mosaic::favstats(~ haircut, data = qsdat |> filter(year == "2022"))
min
      O1 median O3 max mean
                                  sd n missing
 0 16.25
            30 45 240 36.25926 41.81955 54
              "Normal"
                              2014-2022
    Range
                                                      2022
 \(\bar{x}\)
               ~68%
                              \(\frac{438}
                                                  \(\frac{50}
                            \{485\}\) = 90.3\% \{54\}\) = 92.6\%
   \pm s\)
```

Range	"Normal"	2014-2022	2022
\(\bar{x} \pm 2\times s\)	~95%	\(\frac{465} {485}\) = 95.6%	\(\frac{52} {54}\) = 96.3%
\(\bar{x} \pm 3\times s\)	~99.7%	\(\frac{478} {485}\) = 98.6%	\(\frac{52} {54}\) = 96.3%

How did I calculate those fractions?

```
1 # haircut price mean = 30.17 and sd = 31.41 across 2014-2022
 2
 3 qsdat |> count(haircut >= 30.17 - 31.41 & haircut <= 30.17 + 31.41)
   qsdat > count(haircut >= 30.17 - 2*31.41 & haircut <= 30.17 + 2*31.41)
   qsdat > count(haircut >= 30.17 - 3*31.41 & haircut <= 30.17 + 3*31.41)
   \# haircut price mean = 36.26 and sd = 41.82 in 2022 alone
 8
   gsdat |> filter(year == "2022") |>
    count(haircut >= 36.26 - 41.82 \& haircut <= 36.26 + 41.82)
10
   gsdat |> filter(year == "2022") |>
     count (haircut \geq 36.26 - 2*41.82 \& haircut \leq 36.26 + 2*41.82)
12
13 qsdat |> filter(year == "2022") |>
   count(haircut >= 36.26 - 3*41.82 \& haircut <= 36.26 + 3*41.82)
14
```

Question 4 (Heights and Haircut Prices)

Do tall people pay less for haircuts?

Why might we think that they do, before we see the data?

Convert our student heights from inches to centimeters...

```
qsdat <- qsdat |> mutate(height cm = height in * 2.54)
   qsdat |> select(student, height in, height cm) |> head()
# A tibble: 6 \times 3
 student height in height cm
 <chr>
             <dbl>
                       <dbl>
1 202201
            69.5
                        177.
2 202202
              63
                        160.
                       185.
3 202203
         73
         70
                        178.
4 202204
5 202205
         59
                        150.
6 202206
              68
                        173.
```

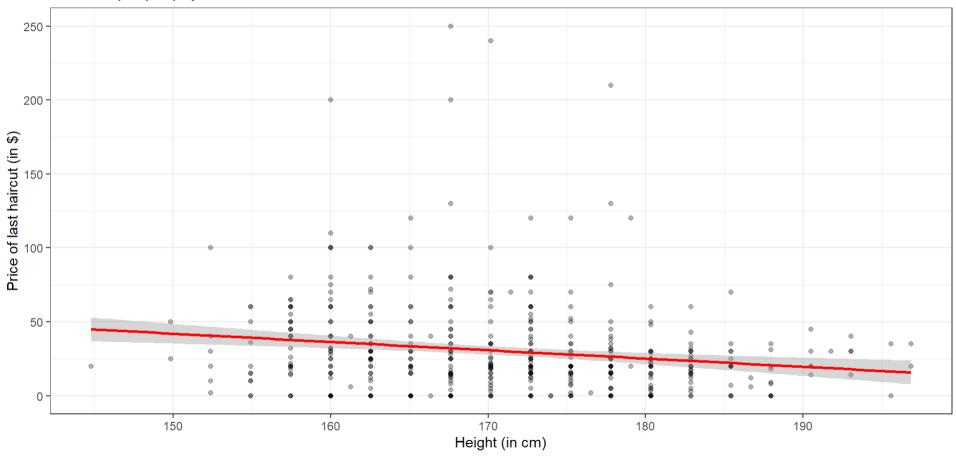
Initial Numerical Summaries

A First Scatterplot

• We'll include the straight line from a linear model, in red.

A First Scatterplot

Do taller people pay less for haircuts?



What is the (Pearson) correlation of height and haircut price?

```
1 dat7 <- qsdat |> filter(complete.cases(height_cm, haircut))
2
3 dat7 |>
4     select(height_in, height_cm, haircut) |>
5     cor()

height in height cm haircut
```

```
height_in 1.0000000 1.0000000 -0.1708551
height_cm 1.0000000 1.0000000 -0.1708551
haircut -0.1708551 -0.1708551 1.0000000
```

What is the straight line regression model?

```
1 dat7 <- qsdat |> filter(complete.cases(height_cm, haircut))
2
3 mod1 <- lm(haircut ~ height_cm, data = dat7)
4
5 mod1</pre>
```

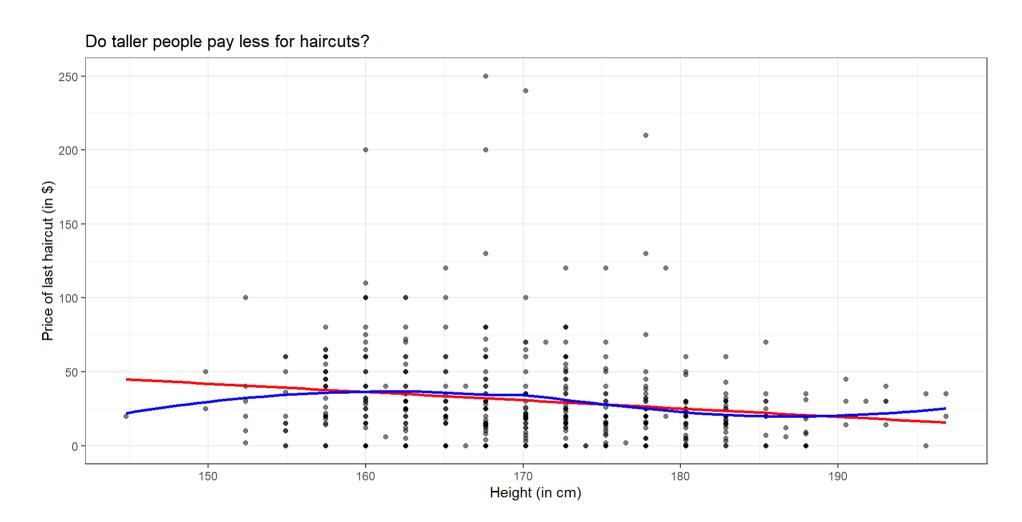
Summarizing our model mod1

```
1 summary (mod1)
Call:
lm(formula = haircut ~ height cm, data = dat7)
Residuals:
   Min 1Q Median 3Q Max
-39.233 -18.124 -6.095 8.165 217.876
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 125.9519 25.2161 4.995 8.25e-07 ***
height cm -0.5597 0.1472 -3.803 0.000161 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Compare 1m fit to loess smooth curve?

- Does a linear model appear to fit these data well?
- Do taller people pay less for their haircuts?

Compare 1m fit to loess smooth curve?



Question 5 (Tobacco and Language Preference)

Restrict ourselves to 2022 data

 Do students in the 2022 class have a more substantial history of tobacco use if they prefer to speak a language other than English?

```
dat9 <- qsdat |>
      filter(year == "2022") |>
       select(student, year, english, smoke)
   summary(dat9)
                               english smoke
  student
                       year
Length:54
                  2022
                         : 54
                               n:16
                                       1:47
Class: character 2014: 0
                               y:38 2: 6
                 2015 : 0
Mode
     :character
                  2016 : 0
                  2017
                  2018
                  (Other): 0
```

Tabulating the categorical variables individually

```
1 dat9 |> tabyl(english)
english n percent
    n 16 0.2962963
    y 38 0.7037037

1 dat9 |> tabyl(smoke) |> adorn_pct_formatting()

smoke n percent
    1 47 87.0%
    2 6 11.1%
    3 1 1.9%
```

What does adorn_pct_formatting() do?

Cross-Classification (2 rows \(\\times\) 3 columns)

```
1 dat9 |> tabyl(english, smoke)
english 1 2 3
    n 15 0 1
    y 32 6 0
```

Recode the smoke levels to more meaningful names in tobacco

Check our work?

• Everyone with smoke = 1 has tobacco as Never, etc.

Restate the cross-tabulation

Now we'll use this new variable, and this time, add row and column totals.

```
1 dat9 |> tabyl(english, tobacco) |>
2    adorn_totals(where = c("row", "col"))
english Never Quit Current Total
    n    15     0     1     16
    y    32     6     0     38
Total    47     6     1     54
```

What can we conclude about this association?

How about in 2014-2022?

```
english Never Quit Current Total

n 95 2 4 101

y 359 26 4 389

Total 454 28 8 490
```

Now, what is your conclusion?

Next Time

Analyzing a (small) health dataset

Cleaning up the temporary objects

```
1 rm(mod1,
2    p4, p5, p6a, p6b,
3    dat1, dat2, dat3, dat4, dat5, dat6, dat7, dat8, dat9
4    )
5
6 ## this just leaves
7 ## qsdat and quicksur_raw in my Global Environment
```

Session Information

Don't forget to close your file with the session information.

```
1 sessionInfo()
R version 4.2.1 (2022-06-23 ucrt)
Platform: x86 64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 22000)
Matrix products: default
locale:
[1] LC COLLATE=English United States.utf8
[2] LC CTYPE=English United States.utf8
[3] LC MONETARY=English United States.utf8
[4] LC NUMERIC=C
[5] LC TIME=English United States.utf8
attached base packages:
[1] stats graphics grDevices utils datasets methods
                                                                base
```