

431 Class 08

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Today's Agenda

- Working again with the `dm1000` data from Class 07
- Confidence Intervals around a Mean
- Building Visualizations to Compare Distributions
- Confidence Intervals for a Difference between Means

Today's Packages

```
1 library(broom)      ## tidying model output
2 library(ggribes)    ## help building ridgeline plots
3 library(Hmisc)      ## smean.cl.boot() and smean.cl.norm()
4 library(janitor)
5 library(kableExtra) ## for table neatening
6 library(naniar)
7 library(patchwork)
8 library(readxl)     ## new today, read in .xls or .xlsx files
9 library(tidyverse)
10
11 theme_set(theme_bw())
```

Data Ingest

Today, we'll use an Excel file (.xls, rather than .csv) to import the **dm1000** data.

```
1 dm1000 <- read_excel("c08/data/dm_1000.xls") |>
2   clean_names() |>
3   mutate(across(where(is.character), as_factor)) |>
4   mutate(subject = as.character(subject))
```

- The **readxl** package is a non-core part of the tidyverse, and also includes functions called **read_xls()** and **read_xlsx()**.
- Visit <https://readxl.tidyverse.org/>.

The `dm1000` tibble

```
1 dm1000
```

```
# A tibble: 1,000 × 17
```

	subject	age	insurance	n_income	ht	wt	sbp	dbp	a1c	ldl	tobacco
	<chr>	<dbl>	<fct>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<fct>
	1 M-0001	55	Medicaid	29853	1.63	103.	145	70	6.4	221	
Current											
	2 M-0002	52	Commercial	31248	1.75	112.	151	77	8.5	116	Never
	3 M-0003	69	Medicare	23362	1.65	74.9	127	73	8.9	52	
Former											
	4 M-0004	57	Medicaid	26033	1.63	81.4	125	74	6.8	122	Never
	5 M-0005	68	Medicare	85374	1.69	92.6	120	73	10.3	94	Never
	6 M-0006	56	Medicaid	31273	1.71	54.6	127	75	12.3	NA	
Current											
	7 M-0007	54	Commercial	25445	1.68	81.6	114	81	6.5	100	
Current											
	8 M-0008	45	Medicaid	67500	1.60	80.0	100	110	5.4	113	Never

Estimating a Population Mean from a Sample

Suppose our sample in `dm1000` is a random sample from the population of all Cuyahoga County residents between the ages of 31-75 receiving care for diabetes.

What's a good estimate for the mean Hemoglobin A1c of the people in that population?

- How would we make this estimate using our data?
- What would we want to know about the data?
- DTDP

Hemoglobin A1c in the **dm1000** sample

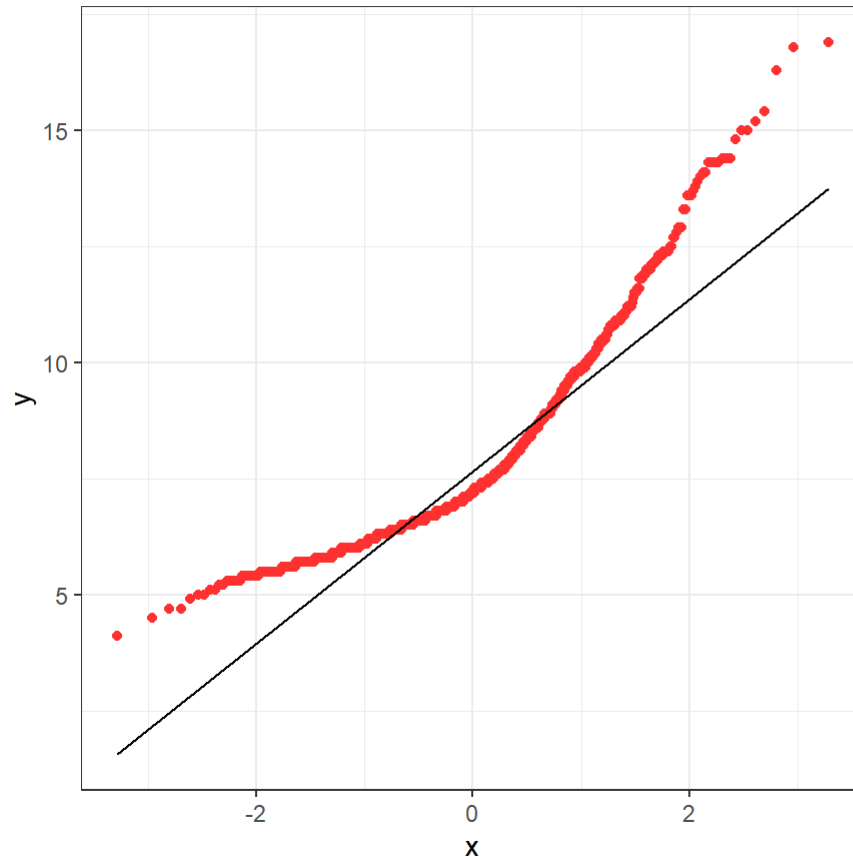
```

1 p1 <- ggplot(dm1000, aes(sample = a1c)) +
2   geom_qq(col = "firebrick1") +
3   geom_qq_line(col = "black") +
4   theme(aspect.ratio = 1) +
5   labs(title = "Normal Q-Q plot: dm1000 a1c")
6
7 p2 <- ggplot(dm1000, aes(x = a1c)) +
8   geom_histogram(aes(y = stat(density)),
9     bins = 20, fill = "firebrick1", col = "khaki") +
10  stat_function(fun = dnorm,
11    args = list(mean = mean(dm1000$a1c, na.rm = TRUE),
12      sd = sd(dm1000$a1c, na.rm = TRUE)),
13    col = "black", lwd = 1.5) +
14  labs(title = "Density Function: dm1000 a1c")
15
16 p3 <- ggplot(dm1000, aes(x = a1c, y = "")) +
17   geom_boxplot(fill = "firebrick1", outlier.color = "firebrick1") +
18   labs(title = "Boxplot: dm1000 a1c", y = "")
19

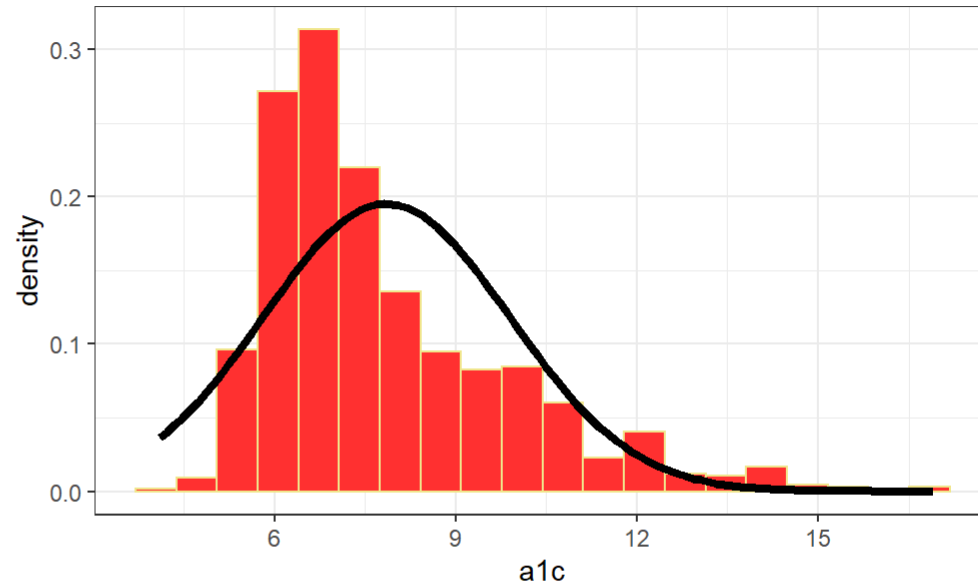
```

Hemoglobin A1c in the **dm1000** sample

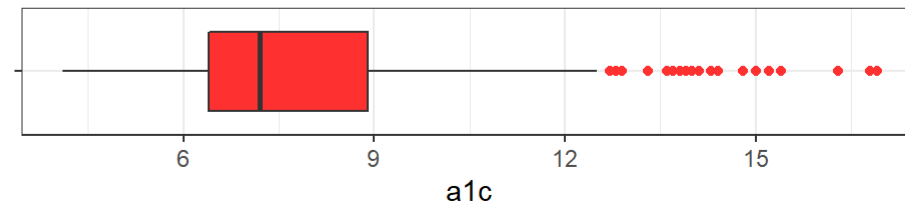
Normal Q-Q plot: dm1000 a1c



Density Function: dm1000 a1c



Boxplot: dm1000 a1c



Numerical Summaries of A1c in **dm1000**

- Should we assume the A1c values are drawn from a Normal distribution?

```
1 mosaic::favstats(~ a1c, data = dm1000) |>
2   kbl(digits = 2) |>
3   kable_styling(font_size = 32, full_width = FALSE)
```

min	Q1	median	Q3	max	mean	sd	n	missing
4.1	6.4	7.2	8.9	16.9	7.85	2.04	985	15

- The **kbl()** and **kable_styling()** functions are from the **kableExtra** package.
 - Read more about **kableExtra** in its vignette.

What if we assume the A1cs are Normally distributed?

Then we could use a linear regression model to obtain a 95% confidence interval for the population mean.

```
1 m1 <- lm(a1c ~ 1, data = dm1000)
2 tidy(m1, conf.int = TRUE, conf.level = 0.95) |>
3   select(estimate, conf.low, conf.high)
```

```
# A tibble: 1 × 3
  estimate conf.low conf.high
  <dbl>     <dbl>     <dbl>
1    7.85    7.73    7.98
```

What is the model we've fit here?

```
1 m1
```

Call:

```
lm(formula = a1c ~ 1, data = dm1000)
```

Coefficients:

```
(Intercept)  
      7.853
```

- This “intercept only” model simply predicts the mean value of our outcome, **a1c**.

Interpreting this interval? (1/3)

- Our 95% confidence interval for the population mean A1c is (7.73, 7.98).

We are estimating the mean of the **population** based on a mean from our *sample* of 1000 observations taken (at random, we assume) from that population.

- Sadly, this **doesn't** mean we're 95% confident that the actual population mean is in that range, even though lots and lots of people (incorrectly) assume it does.

Interpreting this interval? (2/3)

- Our 95% confidence interval for the population mean μ is (7.73, 7.98).

Essentially, we have 95% confidence in the **process** of fitting confidence intervals this way. If we fit 100 such confidence intervals to a variety of data sets, we have some reason to anticipate that 95 of them will contain the actual unknown value of the population mean.

Interpreting this interval? (3/3)

- Our 95% confidence interval for the population mean A1c is (7.73, 7.98).

That's oversimplifying a little, and a particular concern in this case is that the data are somewhat skewed (at any rate, not very close to Normally distributed) and this may impact our ability to generate accurate and efficient confidence intervals via a linear model like this.

An Equivalent Approach

We could use a t test to obtain a 95% confidence interval for the population mean.

```
1 tt <- t.test(dm1000$a1c, conf.level = 0.95)
2 tidy(tt) |> select(estimate, conf.low, conf.high)
```

```
# A tibble: 1 × 3
  estimate conf.low conf.high
  <dbl>    <dbl>    <dbl>
1    7.85    7.73    7.98
```

- This is exactly the same result as we obtain from the linear model `m1`.

Another Equivalent Approach

We could use a function called `smean.cl.normal()` from the `Hmisc` package to obtain the same 95% confidence interval for the population mean.

```
1 smean.cl.normal(dm1000$a1c, conf.int = 0.95)
```

Mean	Lower	Upper
7.852893	7.725167	7.980619

- Again, this is the same result as we have seen previously.

What if we weren't willing to assume that the A1c values came from a Normal distribution?

- Use the bootstrap to estimate the population mean with 95% confidence.

```
1 set.seed(2022431) # why do we set a seed here?  
2 smean.cl.boot(dm1000$a1c, conf.int = 0.95)
```

Mean	Lower	Upper
7.852893	7.726066	7.979513

Bootstrap CI with a different seed

```
1 set.seed(1234567) # what happens if we change the seed
2 smean.cl.boot(dm1000$a1c, conf.int = 0.95)
```

Mean	Lower	Upper
7.852893	7.725378	7.978716

- The `smean.cl.boot()` function comes from the `Hmisc` package.

Bootstrap is a resampling method where large numbers of samples of the same size are repeatedly drawn, with replacement, from a single original sample.

95% CIs for Population Mean A1c

Approach	Estimate	95% CI	Assume Normality?
Linear Model	7.853	(7.725, 7.981)	Yes
Bootstrap	7.853	(7.726, 7.978)	No

- How does this match up with our understanding of the distribution of the A1c data?
- What's an appropriate number of decimal places to use here?

```
1 dm1000 |> select(a1c) |> head(15) |> as.vector()
```

```
$a1c
```

```
[1] 6.4 8.5 8.9 6.8 10.3 12.3 6.5 5.4 7.1 8.9 6.6 6.4 11.1 11.8 6.5
```

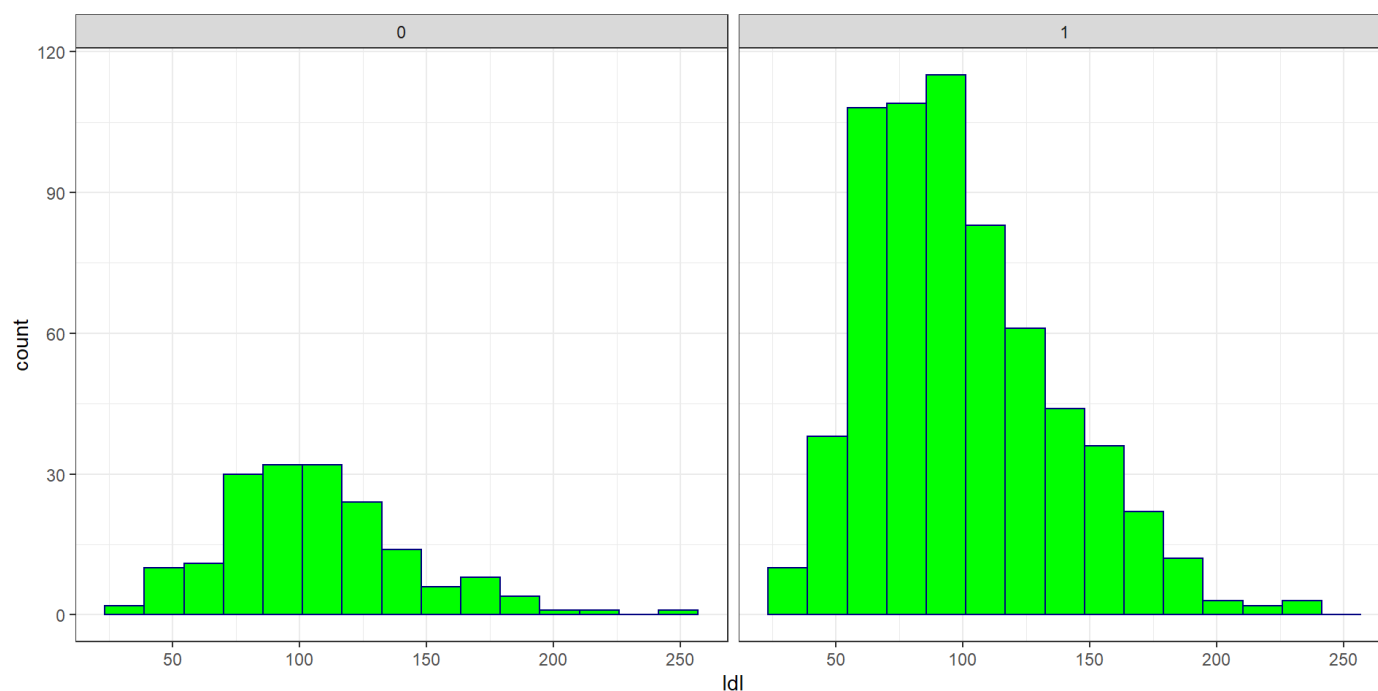
- Might the fairly large sample size (n = 985 non-missing) have something to do with these results?

Comparing Two Distributions

Is LDL higher or lower among adults with diabetes who have a statin prescription?

```
1 ggplot(data = dm1000, aes(x = ldl)) +  
2   geom_histogram(bins = 15, fill = "green", col = "navy") +  
3   facet_wrap(~ statin)
```

Warning: Removed 178 rows containing non-finite values (stat_bin).

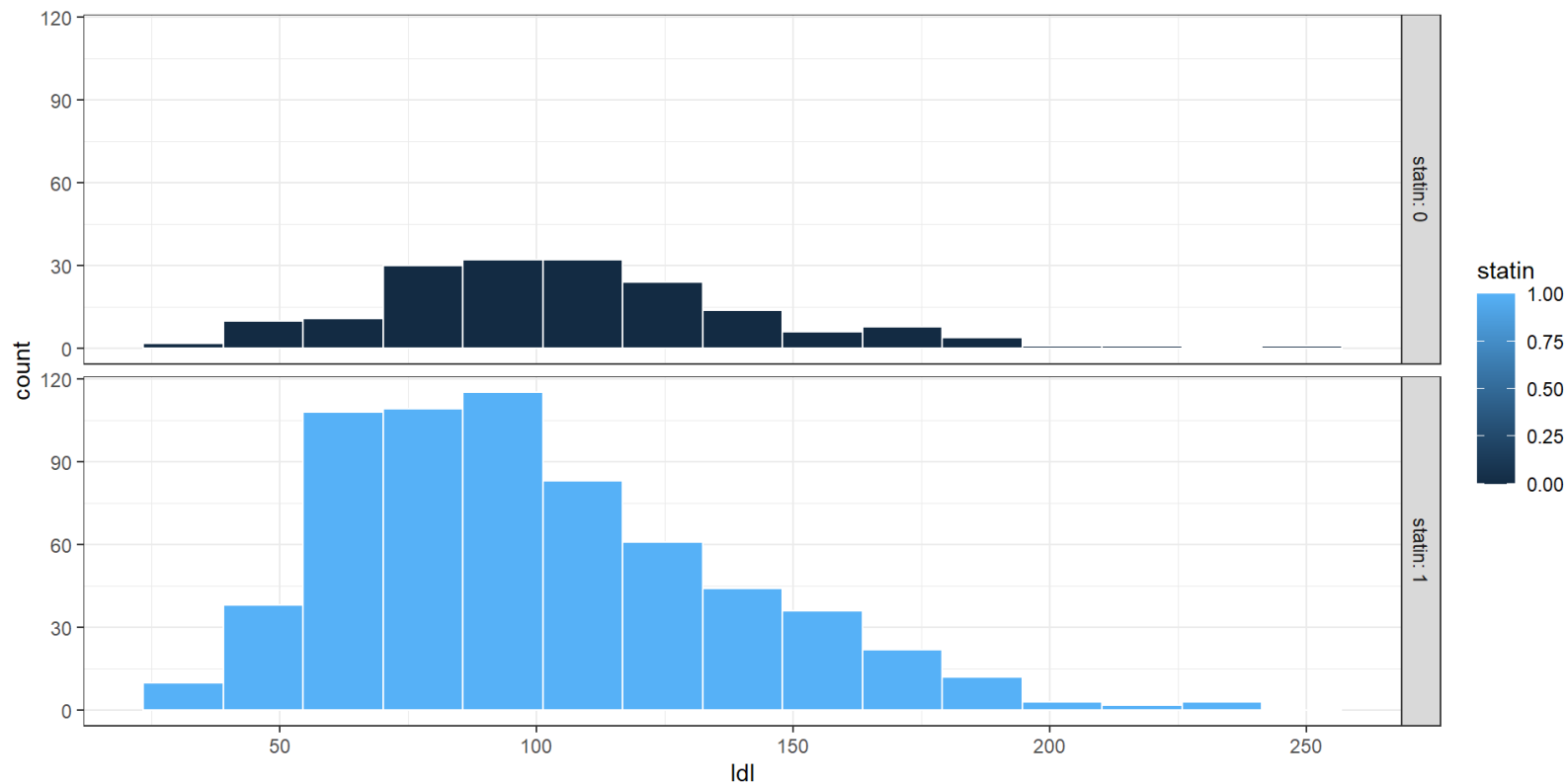


How might we improve this plot?

1. Remove the warning about non-finite (missing) values.
2. Place the histograms vertically to ease comparisons.
3. Fill the histograms differently for statin and no statin.
4. Augment the labels (0 and 1) to show they identify statin use.

LDL stratified by **statin** (Plot 2)

```
1 tempdat <- dm1000 |> filter(complete.cases(ldl, statin))
2
3 ggplot(data = tempdat, aes(x = ldl, fill = statin)) +
4   geom_histogram(bins = 15, col = "white") +
5   facet_grid(statin ~ ., labeller = "label_both")
```

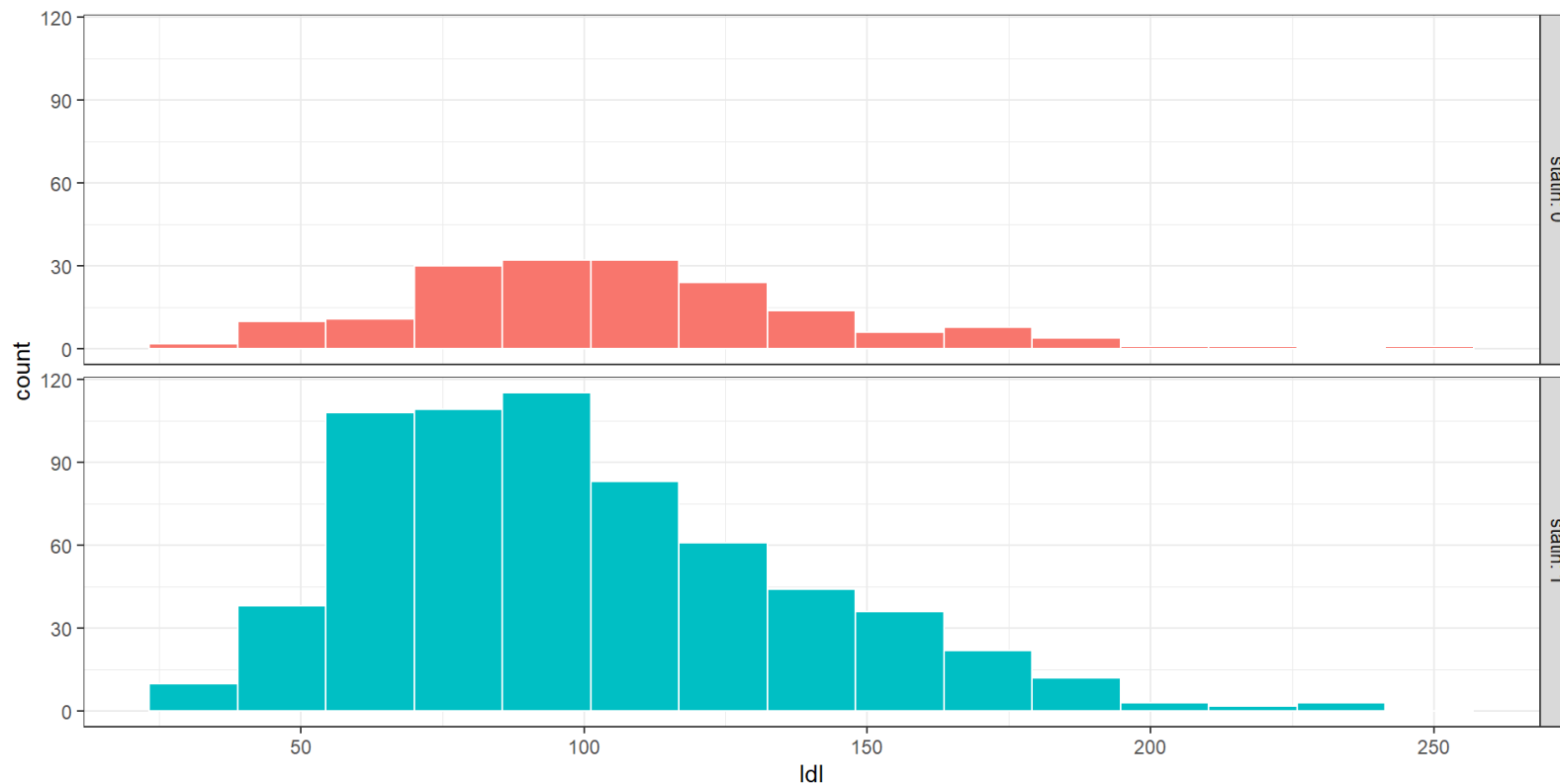


Problems with the previous plot

1. Statin is actually a two-category variable (1 and 0 are just codes) but the legend is treating it as if it was a numeric variable.
2. Do we actually need the legend (called a guide in R) or can we remove it?

But **statin** is categorical? (Plot 3)

```
1 tempdat <- dm1000 |> filter(complete.cases(ldl, statin))
2 ggplot(data = tempdat, aes(x = ldl, fill = factor(statin))) +
3   geom_histogram(bins = 15, col = "white") +
4   facet_grid(statin ~ ., labeller = "label_both") +
5   guides(fill = "none")
```



Faceting

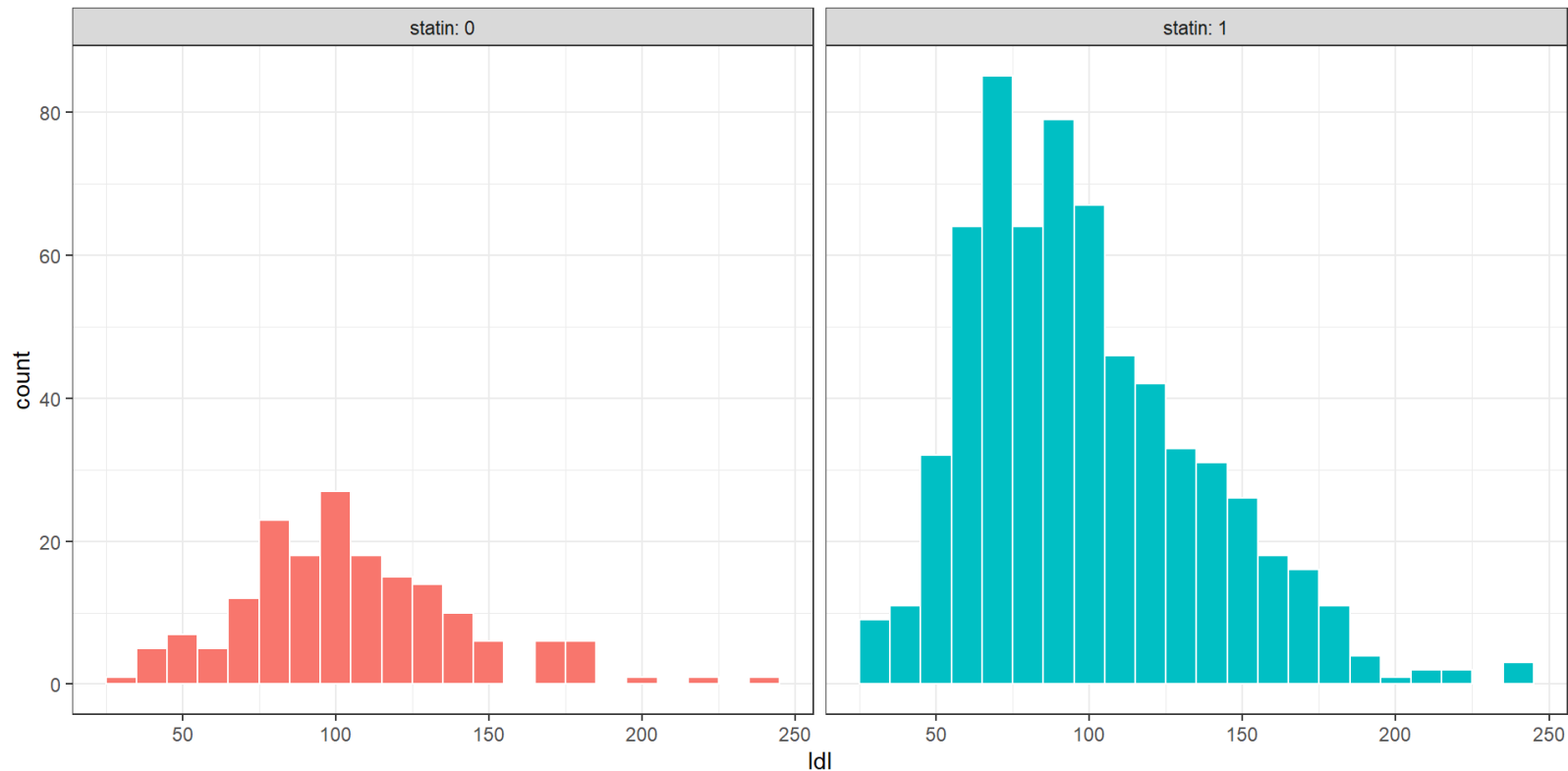
It's very useful to split data into groups and plot each group separately to make comparisons across the groups. We can then draw those subplots side by side.

We have two main tools: `facet_wrap()` and `facet_grid()`

- `facet_wrap(~ grp1)` to obtain plots within each `grp1` arranged into horizontal subpanels and wrapping around, like words on a page.
- `facet_grid(grp1 ~ .)` to obtain plots within each `grp1` arranged vertically (vertical subpanels)
- `facet_grid(grp1 ~ grp2)` to obtain plots within each combination of `grp1` and `grp2` with vertical and horizontal subpanels.

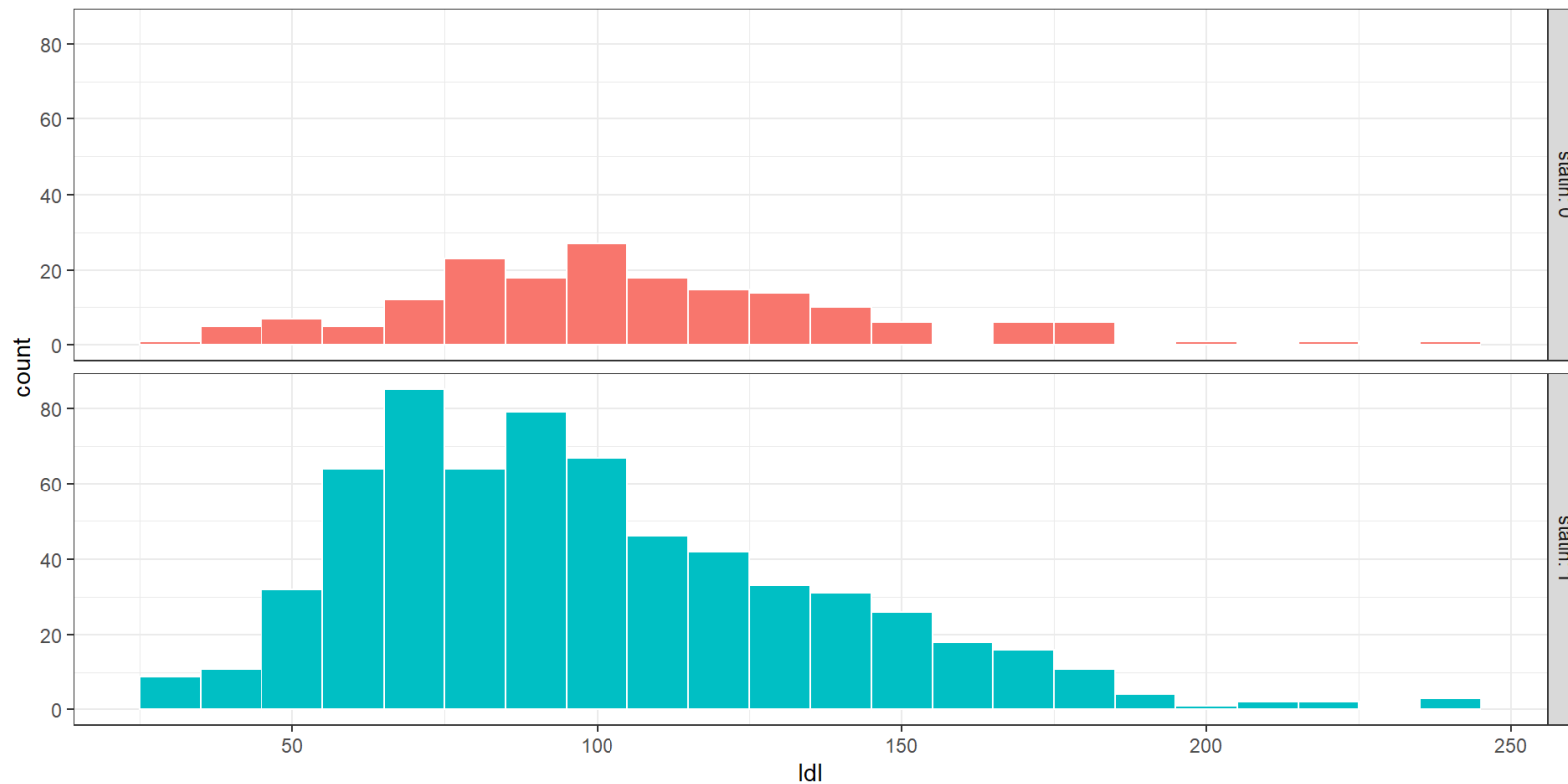
Using `facet_wrap()`

```
1 tempdat <- dm1000 |> filter(complete.cases(ldl, statin))
2 ggplot(data = tempdat, aes(x = ldl, fill = factor(statin))) +
3   geom_histogram(binwidth = 10, col = "white") +
4   facet_wrap(~ statin, labeller = "label_both") +
5   guides(fill = "none")
```



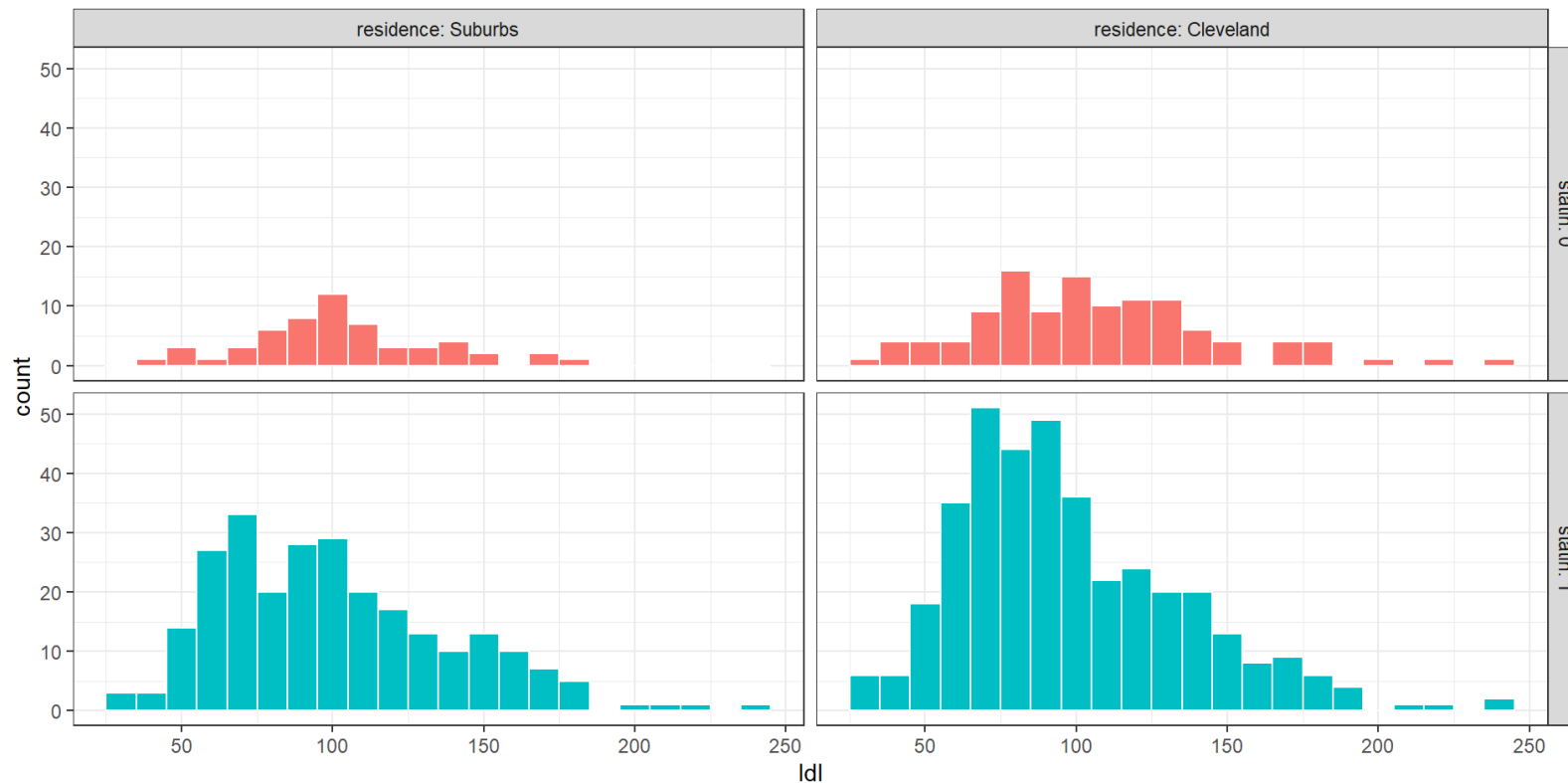
Using `facet_grid()`

```
1 tempdat <- dm1000 |> filter(complete.cases(ldl, statin))
2 ggplot(data = tempdat, aes(x = ldl, fill = factor(statin))) +
3   geom_histogram(binwidth = 10, col = "white") +
4   facet_grid(statin ~ ., labeller = "label_both") +
5   guides(fill = "none")
```



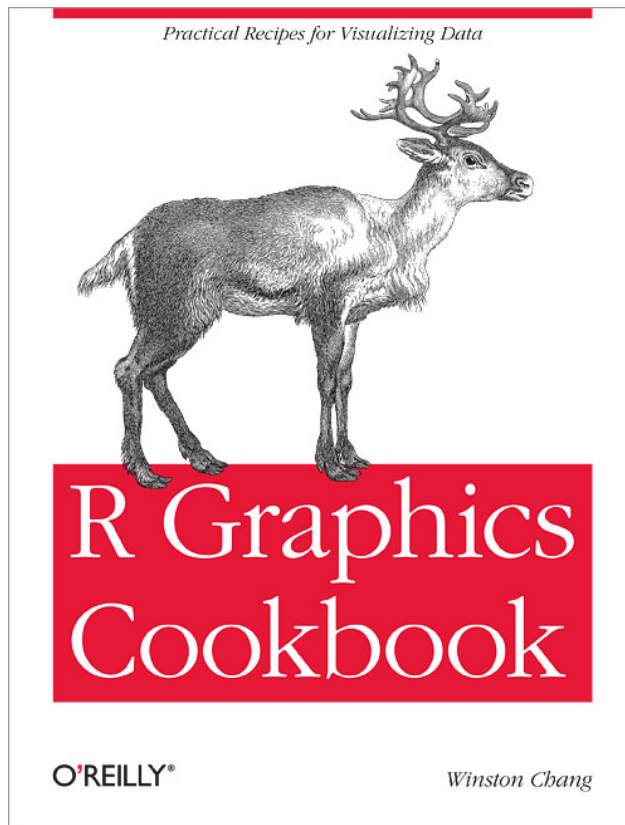
facet_grid(): two groupings

```
1 tempdat <- dm1000 |> filter(complete.cases(ldl, statin, residence))
2 ggplot(data = tempdat, aes(x = ldl, fill = factor(statin))) +
3   geom_histogram(binwidth = 10, col = "white") +
4   facet_grid(statin ~ residence, labeller = "label_both") +
5   guides(fill = "none")
```



My Main Source for `ggplot2` Visualization Recipes

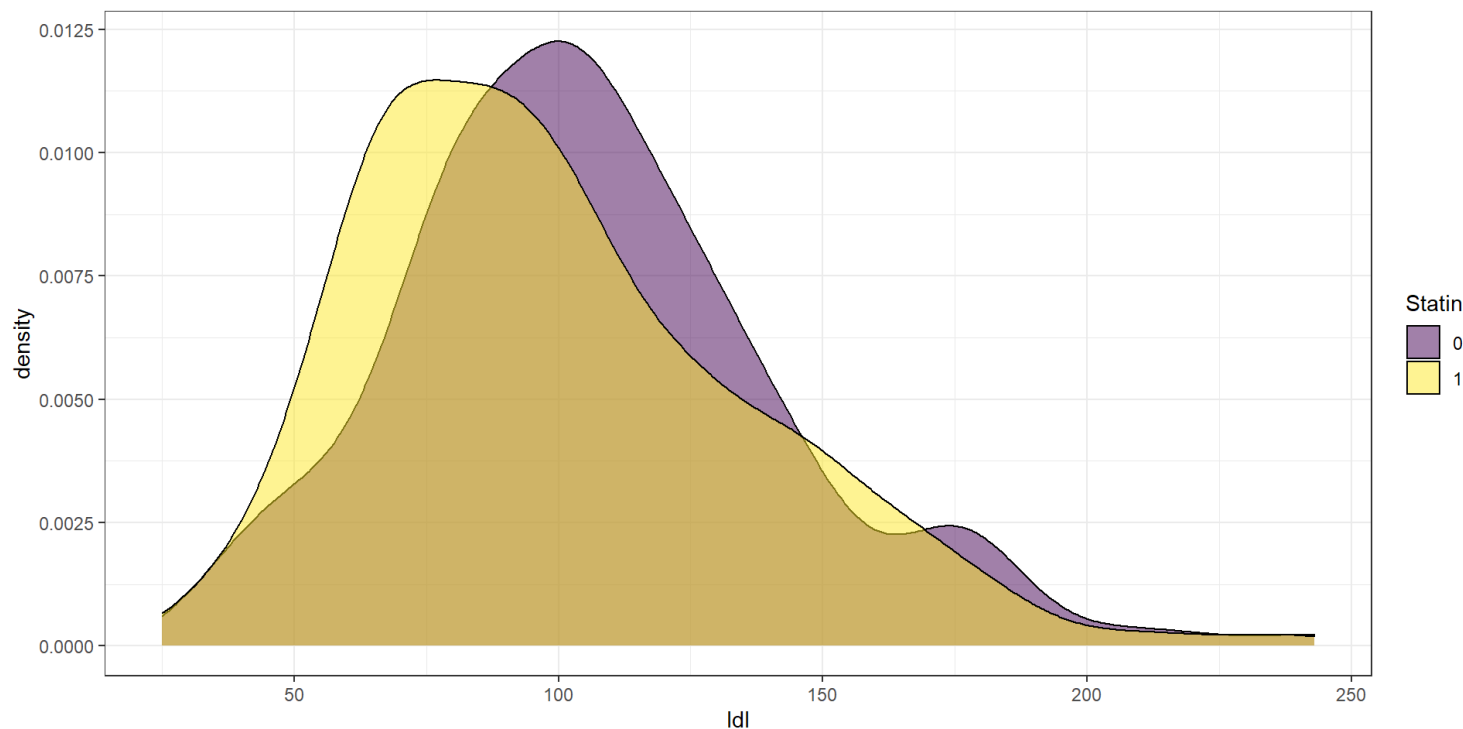
<https://r-graphics.org/> (Second Edition)



Comparison of densities

This plot ignores the relative frequencies.

```
1 tempdat <- dm1000 |> filter(complete.cases(ldl, statin))
2 ggplot(data = tempdat, aes(x = ldl, fill = factor(statin))) +
3   geom_density(alpha = 0.5) + scale_fill_viridis_d() +
4   labs(fill = "Statin")
```



Numerical Summaries for Two Groups

```

1 dm1000 |> filter(complete.cases(statin, ldl)) |>
2   group_by(statin) |>
3   summarize(n = n(), min = min(ldl), med = median(ldl),
4             max = max(ldl), mean = mean(ldl),
5             sd = sd(ldl)) |>
6   kbl(digits = 2)

```

statin	n	min	med	max	mean	sd
0	176	34	102	243	106.22	36.05
1	646	25	92	241	99.22	37.21

- Difference in mean(LDL) between the two samples?

Using **favstats** for LDL by Statin

```
1 mosaic::favstats(ldl ~ statin, data = dm1000)
```

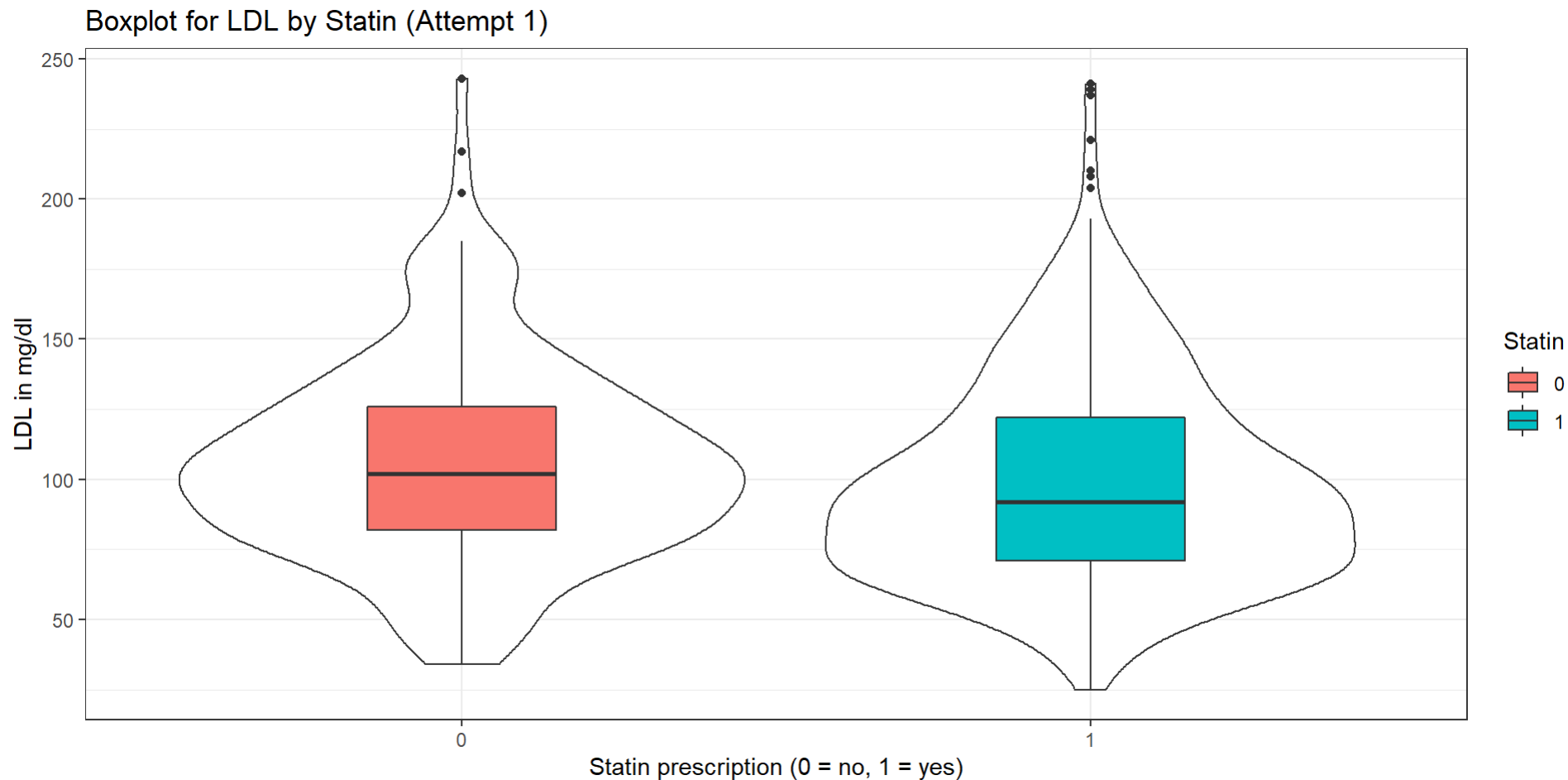
	statin	min	Q1	median	Q3	max	mean	sd	n	missing
1	0	34	82	102	126	243	106.22159	36.04619	176	66
2	1	25	71	92	122	241	99.22136	37.20972	646	112

Comparison Boxplot (LDL by statin)

Attempt 1

```
1 tempdat <- dm1000 |> filter(complete.cases(ldl, statin))
2
3 ggplot(data = tempdat, aes(x = factor(statin), y = ldl)) +
4   geom_violin() +
5   geom_boxplot(aes(fill = factor(statin)), width = 0.3) +
6   labs(x = "Statin prescription (0 = no, 1 = yes)",
7        y = "LDL in mg/dl", fill = "Statin",
8        title = "Boxplot for LDL by Statin (Attempt 1)")
```

Comparison Boxplot (LDL by statin)

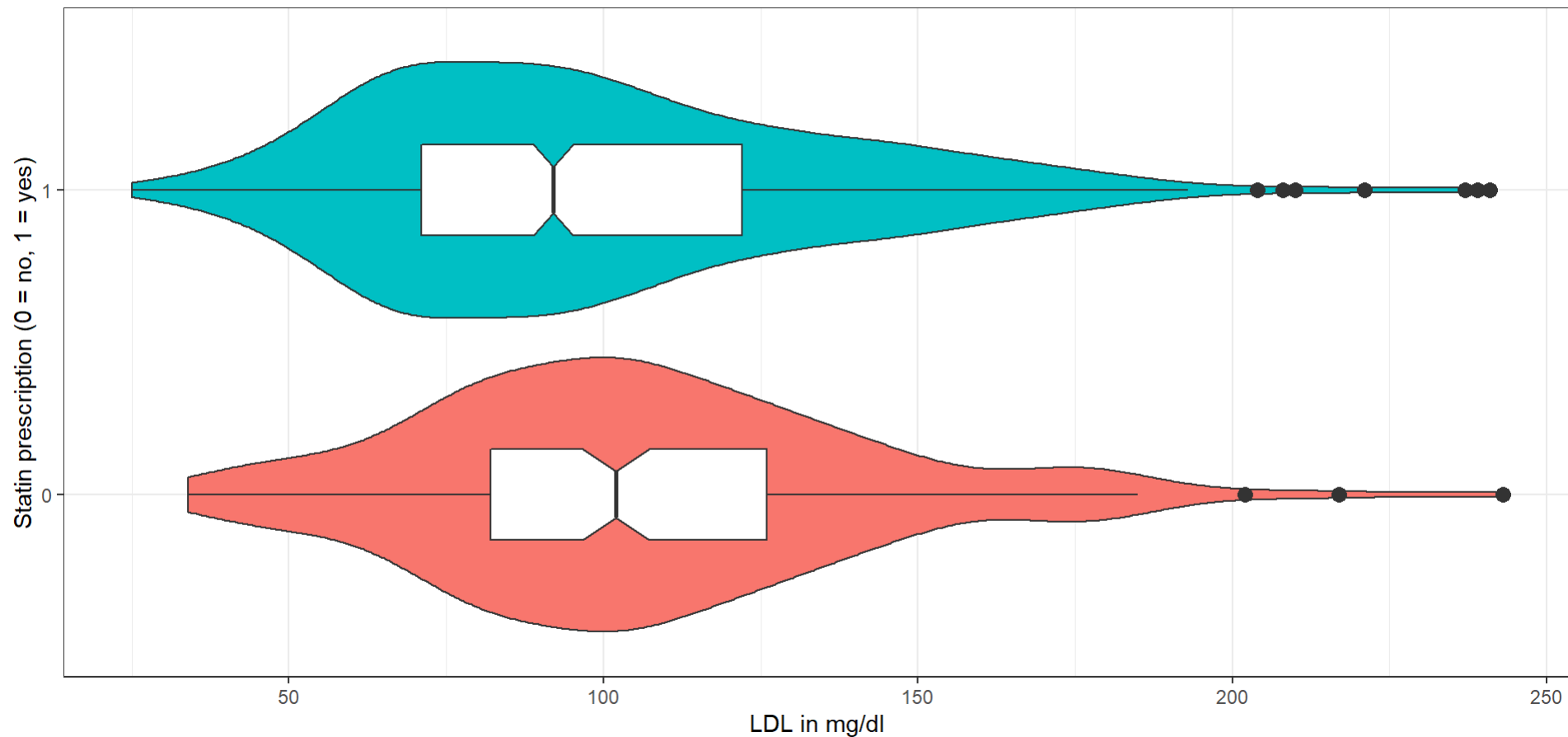


Try 2: Boxplot for LDL and statin

```
1 tempdat <- dm1000 |> filter(complete.cases(ldl, statin))
2
3 ggplot(data = tempdat, aes(x = factor(statin), y = ldl)) +
4   geom_violin(aes(fill = factor(statin))) +
5   geom_boxplot(width = 0.3, outlier.size = 3, notch = TRUE) +
6   coord_flip() +
7   guides(fill = "none") +
8   labs(x = "Statin prescription (0 = no, 1 = yes)",
9        y = "LDL in mg/dl",
10        title = "Boxplot for LDL by Statin (Attempt 2)")
```

Try 2: Boxplot for LDL and statin

Boxplot for LDL by Statin (Attempt 2)



Setting Up Third Try

```

1 dm_for_boxplot <- dm1000 |>
2   filter(complete.cases(statin, ldl)) |>
3   mutate(statin_f = fct_recode(factor(statin),
4                               "No Statin" = "0",
5                               "Statin" = "1")) |>
6   select(subject, ldl, statin_f, statin)
7
8 head(dm_for_boxplot, 3) # print first three rows

```

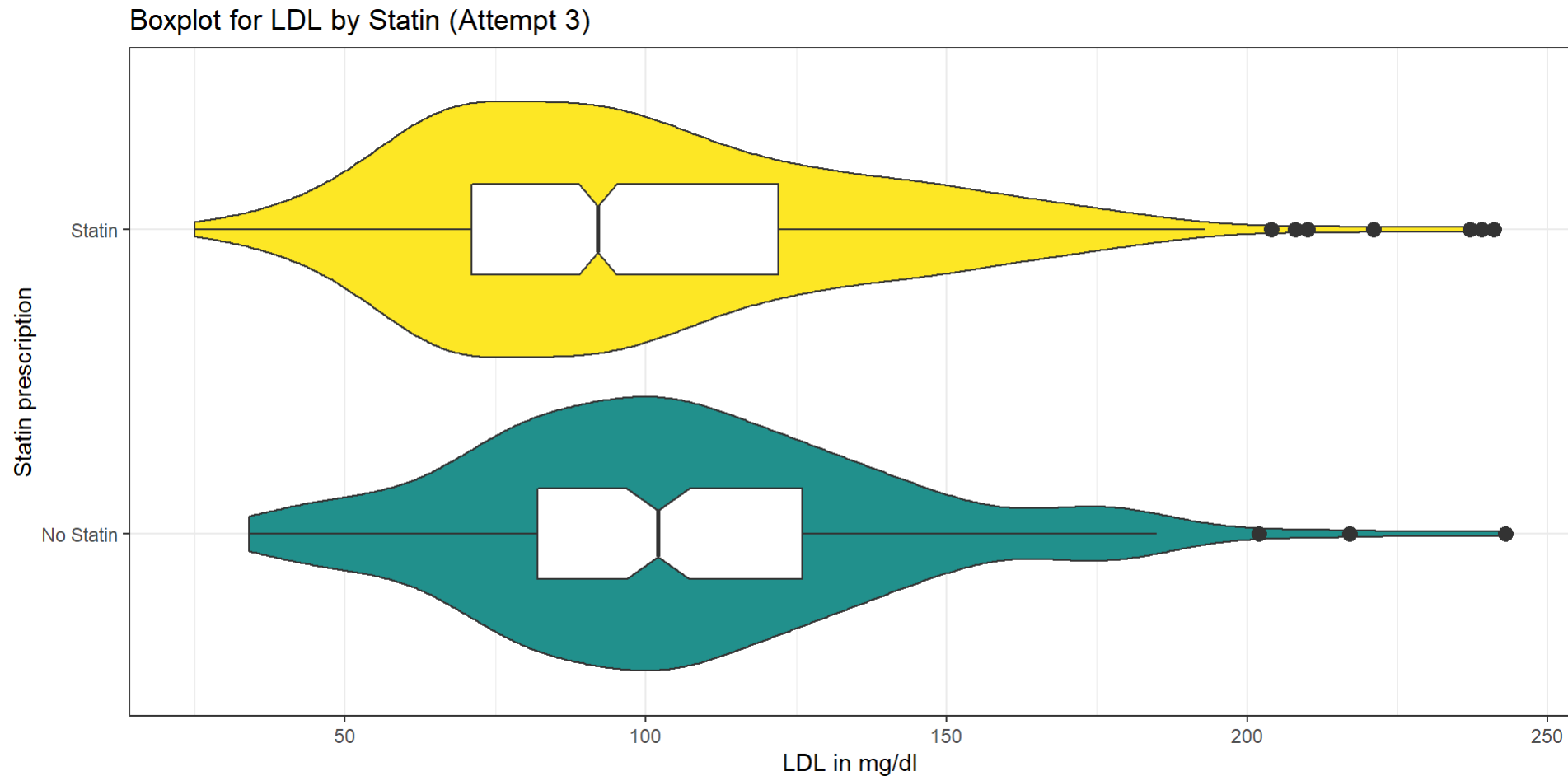
A tibble: 3 × 4

	subject	ldl	statin_f	statin
	<chr>	<dbl>	<fct>	<dbl>
1	M-0001	221	Statin	1
2	M-0002	116	No Statin	0
3	M-0003	52	Statin	1

Third Try on Boxplot for LDL by Statin Use

```
1 ggplot(data = dm_for_boxplot, aes(x = statin_f, y = ldl)) +  
2   geom_violin(aes(fill = statin_f)) +  
3   geom_boxplot(width = 0.3, outlier.size = 3, notch = TRUE) +  
4   coord_flip() + guides(fill = "none") +  
5   scale_fill_viridis_d(begin = 0.5, option = "D") +  
6   labs(x = "Statin prescription",  
7        y = "LDL in mg/dl",  
8        title = "Boxplot for LDL by Statin (Attempt 3)")
```

Third Try on Boxplot for LDL by Statin Use



95% CI for difference in means

We want to estimate the difference between the population mean LDL WITH statin and population mean LDL WITHOUT statin.

The sample means, you'll remember, are:

```
1 mosaic::favstats(ldl ~ statin, data = dm1000) |>  
2   select(statin, n, mean, sd, missing) |>  
3   kbl(digits = 2) |> kable_styling(font_size = 24)
```

statin	n	mean	sd	missing
0	176	106.22	36.05	66
1	646	99.22	37.21	112

95% CI for difference in means

- If we are willing to assume that LDL follows a Normal distribution in each statin group, then we can use a linear model with one predictor.

```
1 m2 <- lm(ldl ~ statin, data = dm1000)
```

Coefficients of Model **m2**

```
1 m2
```

Call:

```
lm(formula = ldl ~ statin, data = dm1000)
```

Coefficients:

(Intercept)	statin
106.2	-7.0

```
1 tidy(m2, conf.int = TRUE, conf.level = 0.95) |>
2   select(term, estimate, conf.low, conf.high)
```

A tibble: 2 × 4

	term	estimate	conf.low	conf.high
	<chr>	<dbl>	<dbl>	<dbl>
1	(Intercept)	106.	101.	112.
2	statin	-7.00	-13.2	-0.831

Using `t.test` to get same result

```
1 mosaic::favstats(ldl ~ statin, data = dm1000) |>
2   select(statin, n, mean, sd, missing) |>
3   kbl(digits = 2) |> kable_styling(font_size = 24)
```

statin	n	mean	sd	missing
0	176	106.22	36.05	66
1	646	99.22	37.21	112

```
1 tt <- t.test(ldl ~ statin, data = dm1000,
2             var.equal = TRUE, conf.level = 0.95)
3 tidy(tt) |> select(estimate, conf.low, conf.high) |>
4   kbl(digits = 3) |> kable_styling(font_size = 32)
```

estimate	conf.low	conf.high
7	0.831	13.17

95% CI for difference between population means via the bootstrap

If we are not willing to assume a Normal distribution for LDL in either the statin or the “no statin” group, then we could use a bootstrap approach.

```
1 source("c08/data/Love-boost.R")
2
3 set.seed(123123)
4 bootdif(y = dm1000$ldl, g = factor(dm1000$statin), conf.level = 0.95)
```

Mean Difference	0.025	0.975
-7.0002287	-13.3055407	-0.8186563

The `bootdif` function

from `Love-boost.R`

```
1 `bootdif` <-  
2   function(y, g, conf.level=0.95, B.reps = 2000) {  
3     lowq = (1 - conf.level)/2  
4     g <- as.factor(g)  
5     a <- attr(Hmisc::smean.cl.boot(y[g==levels(g)[1]],  
6                                   B=B.reps, reps=TRUE), 'reps')  
7     b <- attr(Hmisc::smean.cl.boot(y[g==levels(g)[2]],  
8                                   B=B.reps, reps=TRUE), 'reps')  
9     meandif <- diff(tapply(y, g, mean, na.rm=TRUE))  
10    a.b <- quantile(b-a, c(lowq, 1-lowq))  
11    res <- c(meandif, a.b)  
12    names(res) <- c('Mean Difference', lowq, 1-lowq)  
13    res  
14  }
```

Assumptions behind our intervals

Assumptions these intervals share:

- random samples from the populations of interest
- independent samples (samples aren't paired or matched)

Additional assumptions for linear model:

- Normal distribution in each group (statin and “no statin”)
- variance in each group (statin and “no statin”) is equal

95% confidence intervals for mean LDL

95% CIs for LDL $\mu_{NoStatin} - \mu_{Statin}$

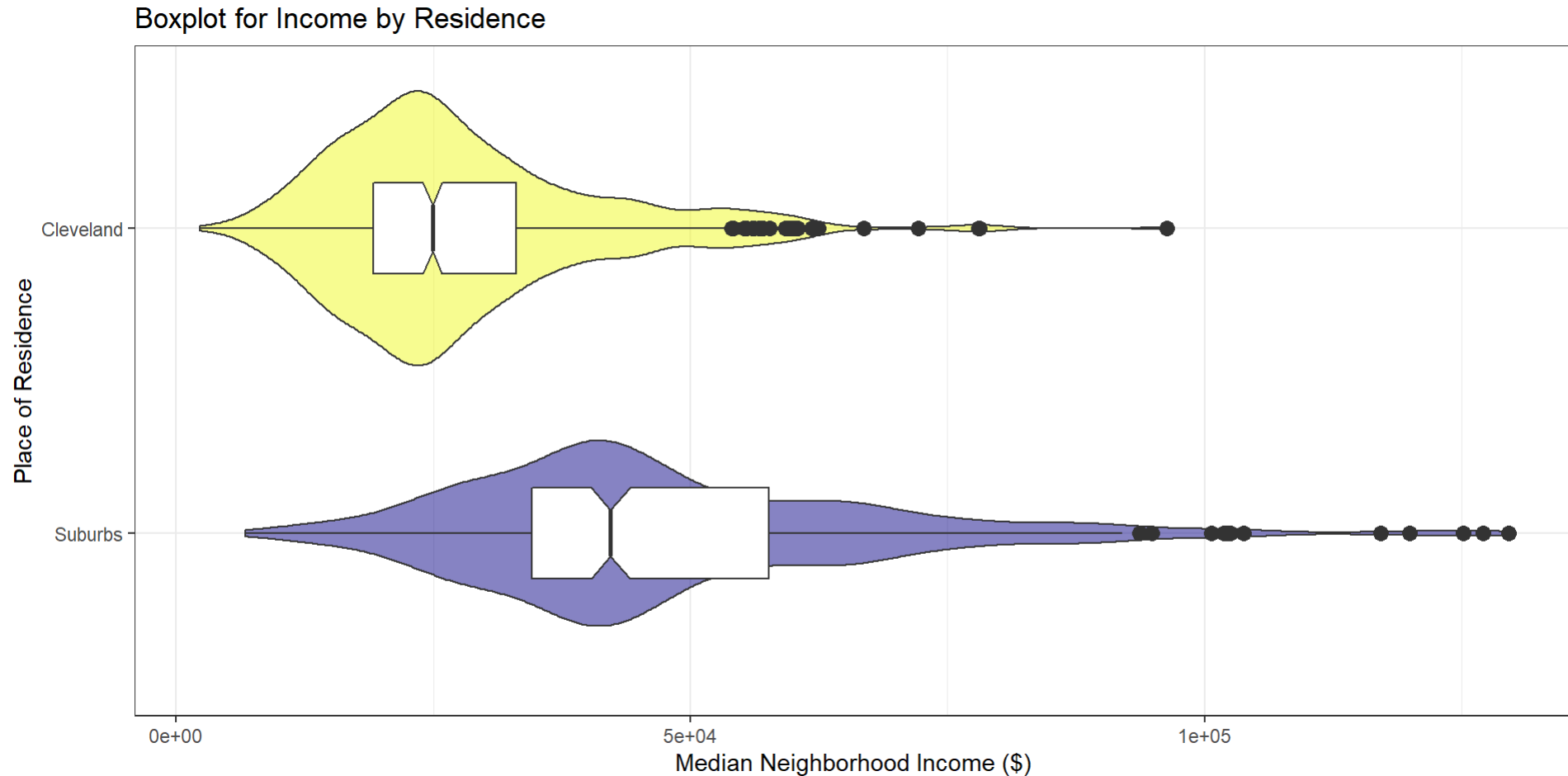
Approach	Estimate	95% CI
linear model	7.00	(0.83, 13.17)
bootstrap	7.00	(0.82, 13.31)

Are our conclusions meaningfully different if we do (or do not) assume Normal population distributions of LDL within each group (statin and no statin)?

Comparing Income by Residence

```
1 tempdat <- dm1000 |> filter(complete.cases(n_income, residence))
2
3 ggplot(data = tempdat, aes(x = residence, y = n_income)) +
4   geom_violin(aes(fill = residence)) +
5   geom_boxplot(width = 0.3, outlier.size = 3, notch = TRUE) +
6   coord_flip() + guides(fill = "none") +
7   scale_fill_viridis_d(alpha = 0.5, option = "C") +
8   labs(x = "Place of Residence",
9        y = "Median Neighborhood Income ($)",
10        title = "Boxplot for Income by Residence")
```

Comparing Income by Residence



Sample Means, Medians

```
1 mosaic::favstats(n_income ~ residence, data = dm1000) |>
2   select(residence, n, mean, median, sd, missing) |>
3   kbl(digits = 0) |> kable_styling(font_size = 32)
```

residence	n	mean	median	sd	missing
Suburbs	371	47251	42223	20333	0
Cleveland	601	27725	24907	13031	0

Estimating 90% CI for Difference in Means

Linear Model for Income by Residence

```
1 m3 <- lm(n_income ~ residence, data = dm1000)
2 tidy(m3, conf.int = TRUE, conf.level = 0.90) |>
3   select(term, estimate, conf.low, conf.high)
```

A tibble: 2 × 4

	term	estimate	conf.low	conf.high
	<chr>	<dbl>	<dbl>	<dbl>
1	(Intercept)	47251.	45866.	48637.
2	residenceCleveland	-19527.	-21289.	-17765.

Bootstrap Approach

```
1 set.seed(443322)
2 bootdif(y = dm1000$n_income, g = dm1000$residence,
3         conf.level = 0.90)
```

Mean Difference	0.05	0.95
-19526.68	-21468.71	-17545.30

90% CI for difference in mean Income

90% CIs for Income $\mu_{Suburbs} - \mu_{Cleveland}$

Approach	Estimate	90% CI
linear model	19527	(17765, 21289)
bootstrap	19527	(17545, 21469)

Are our conclusions meaningfully different if we do (or do not) assume Normal population distributions of neighborhood income within each residence group?

Save the **dm1000** tibble as an R data set

- Preserves all changes in your R work (factors, etc.)

We'll load this in when we work with these data in Class 09.

Session Information

```
1 sessionInfo()
```

```
R version 4.2.1 (2022-06-23 ucrt)  
Platform: x86_64-w64-mingw32/x64 (64-bit)  
Running under: Windows 10 x64 (build 22000)
```

```
Matrix products: default
```

```
locale:
```

```
[1] LC_COLLATE=English_United States.utf8  
[2] LC_CTYPE=English_United States.utf8  
[3] LC_MONETARY=English_United States.utf8  
[4] LC_NUMERIC=C  
[5] LC_TIME=English_United States.utf8
```

```
attached base packages:
```

```
[1] stats      graphics  grDevices  utils      datasets  methods    base
```