

Data Science for Smart Cities CE88

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Today



Variability of samples, confidence intervals

Variability of predictions

Minilab 8

Midterm planning

Statistics terminology



Inference: Making conclusions from random samples

Population: The entire set that is the subject of interest

Parameter: A quantity computed for the entire population

Sample: A subset of the population

In a **Random Sample**, we know the chance that any subset of the population will enter the sample, in advance

Statistic: A quantity computed for a particular sample

Parameters and intervals



A reasonable way to estimate a parameter such as the population average, max, or median is to compute the corresponding statistic for a sample.

Different samples will lead to different estimates.

Goal: Infer the variability of a statistic, using only a sample.

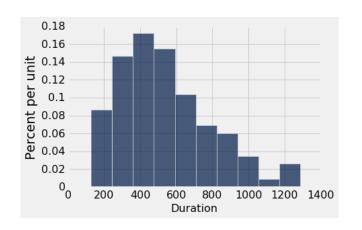
A possible solution: apply bootstrap resampling, as variability of the sample represents that of a population.

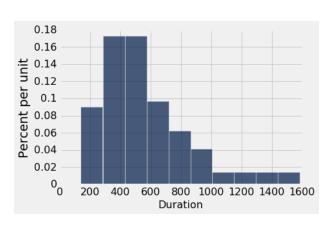
Confidence intervals



Estimation is a process with a random outcome

Population (fixed) → Sample (random) → Statistic (random)



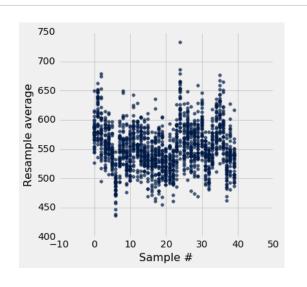


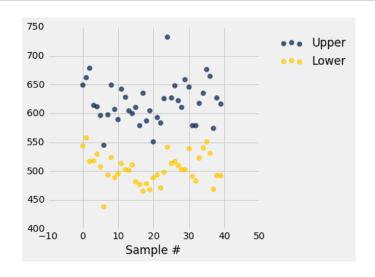
Instead of picking a single estimate of the parameter, we can pick a whole interval: lower bound to upper bound

A 95% Confidence Interval is an interval that will contain the parameter for (at least) 95% of samples

Confidence intervals







BTW, for a particular sample, it's right or wrong & you don't know ©

It's impossible to verify empirically whether an interval is correct when all you have is a sample.

But if you have the whole population, you can check if the intervals were correct

Confidence intervals



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- Study the variability of the sample mean
- Get a gut feeling on the uncertainty of predictions

N.B. We can get confidence intervals for any statistic we compute from a sample, not just the mean!

Recall the modelling framework



Set of explanatory variables (EVs) for the total population

Population data (geo-demographics)

Spatial data (system layout)

System performance data (travel times)

Individual level data on travel decisions

Set of EVs and the mode choices for a **sample** of population

Mode choice model development

Uncertainty propagates through the predictive models!

Prediction of modal split for the total population

Travel demand

A proper decision support framework must include uncertainty estimates (for example, confidence intervals) along with any inferred statistic.