Stat 5014 HW6

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Problem 2: Sums of Squares

In this problem, we are to compare traditional for loop style computing of sums of squares (SST) to the same computation using vector operations. The comparison is in timing and code pretty-ness. The data using in this problem is generated and included in the following code.

Times for the "for loop" method and the vectorized method are respectively. I had initially included the mean(y) inside the square term in the loop function. This was taking WAY to long, so I precalculated that saving a ton of redundant calculation of \bar{y} .

This one change resulted in a new time for the vectorized method of giving a -60.279617% reduction.

Problem 3: Dual nature for speed

In this problem, we are being asked to code up a gradient descent algorithm, again using for loop and matrix operations comparing the timings and code cleanliness.

First, the for loop version of gradient descent:

In this case, we greatly improved the code readibility. We did not see an improvement in speed and in fact are a bit slower: 0.352 vs 0.159 for matrix and for loops respectively.

Problem 5:

Here the goal is to compute a set of vector/matrix operations quickly. As a reminder, the operation we are to compute is:

$$y = p + AB^{-1}(q - r) \tag{1}$$

Without any improvements, a single iteration (i.e. single randomly populated B matrix) takes 10-20 min. Without going through the optimization strategy, here is the best I came up with:

```
A <- C[id, -id] # matrix of dimension 932 * 15068
B <- C[-id, -id] # matrix of dimension 15068 * 15068, still a block diagonal matrix, sparse
p <- runif(932, 0, 1)
r \leftarrow runif(15068, 0, 1)
C <- NULL
qr <- q - r # not really part of the compute as updates are to B
Bsp <- Matrix(B)</pre>
                 #if more than 1/2 entries are zero, cast as sparse = default
Asp <- Matrix(A) #probably don't need to do this, but it doesn't hurt
t6 <- system.time(z4 <- p + Asp %*% solve(Bsp, tol = 1e-19) %*%
    qr)
```

10 x 10 blocks along the diagonal with off diagonal elements as correlation values. Here is a tabulation of the

```
There was a question on the structure of B. B is a 15068 x 15068 matrix with 1 along the diagonal and
elements in the matrix. There should only be 100 different elements, so we can do this.;)
## quick view of diagonal elements
table(diag(B))
##
##
       1
## 15068
## quick view of all elements
table(B)
## B
     -0.0593434916659995
##
                             -0.0508276241929542
                                                     -0.0437017561156568
##
##
      -0.038750409534823
                             -0.0305274493319447
                                                     -0.0273326680743183
##
                     2846
                                             2846
                                                                     2840
##
     -0.0227720797133449
                             -0.0225580436431903
                                                     -0.0197143753612597
##
                      2838
                                             2778
                                                                     2786
     -0.0191550046699806
                                                     -0.0165529818525149
##
                             -0.0172044735203295
##
                     2818
                                             2864
                                                                     2826
##
     -0.0112268117618719
                            -0.00999895750295145
                                                    -0.00992443838738708
##
                     2834
                                             2880
                                                                     2852
    -0.00570913833279853
                            -0.00350732978899381
                                                    -0.00157798603174804
##
##
                     2890
                                             2832
                                                                     2840
   -0.000735565416207467
                           -0.000307894947901916
                                                                         0
##
##
                     2830
                                             2878
                                                                226901840
                             0.00440492064485365
                                                     0.00519764852786881
##
     0.00315488431358059
##
                     2850
                                             2856
                                                                     2862
                              0.0139231038084424
##
      0.0120457779053466
                                                      0.0156534798664632
##
                     2798
                                             2860
                                                                     2790
##
      0.0164999934196776
                              0.0178918023080869
                                                       0.019154353130133
##
                     2846
                                             2814
                                                                     2832
      0.0200073730433835
                              0.0207074777999135
                                                      0.0232835244473396
##
```

2876

2820

2850

2824

0.0274379741101879

0.0350875434242563

0.0382181912683319

2806

2876

2834

2860

0.0276659540361215

0.0358178330927301

0.04263912518562

##

##

##

##

##

##

##

2816

2830

2866

2836

0.0234085689443415

0.0328079464072214

0.0377559526370284

##	0.0499500699922705	0.052335886671229	0.0596711135806099
##	2860	2826	2806
##	0.0709580851423905	1	
##	2820	15068	