

Your task is simple. You are a drawing robot with the dream of drawing a diamond.

## Question 1: Find the roots

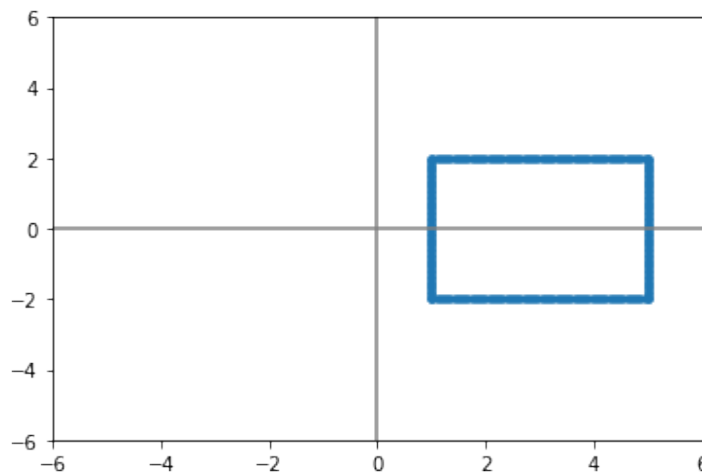
In order to draw the diamond. You first must draw a square. Find the roots of these two equations as they will be used to graph the square.

- a) Find the roots of  $x^2 - 10x + 29$
- b) Find the roots of  $x^2 - 2x + 5$

## Question 2: Draw the Square

Draw the 4 roots from part 1 on an Argand diagram (a plot where the x-axis represents real numbers such as 3 and the y-axis is imaginary numbers such as  $5i$ ). Make sure to label the axis as  $Im$  and  $Re$  (for real and imaginary numbers) as well as all of the points.

- a) Label the axis  $Im$  and  $Re$  (for real and imaginary numbers)
- b) Plot the 4 roots (should be  $5 \pm 2i$  and  $1 \pm 2i$ )
- c) Label the roots
- d) Check that it looks similar to the plot below



### Question 3: Making the diamond

We are going to rotate the square by 45 degrees.

- a) Multiply the 4 points by  $(1 + i)$ . This is effectively a complex number that specifies a 45 degree rotation around  $0 + 0i$ .
- b) Plot the result on your original Argand diagram with the square
- c) Notice how the diamond (orange shape) looks a little bit bigger than the original square. This is because we are scaling the square by  $\sqrt{2}$ .
- d) Good work! You have fulfilled your lifelong goal of drawing a diamond!

