CS 61C:
Great Ideas in Computer Architecture
Synchronous Digital Systems

Instructors:

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http://inst.eecs.berkeley.edu/~cs61c/sp15
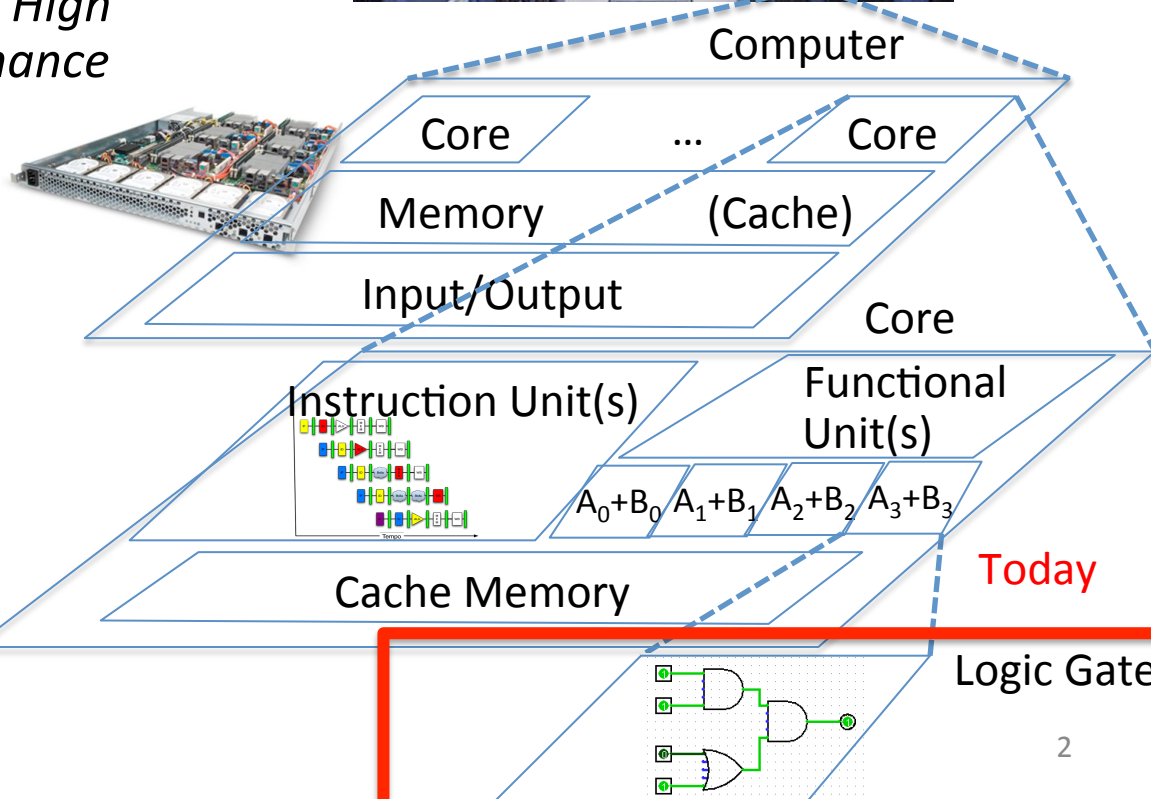
You are Here!

Software   *Hardware*

- **Parallel Requests**
  Assigned to computer
  e.g., Search "Katz"

- **Parallel Threads**
  Assigned to core
  e.g., Lookup, Ads

- **Parallel Instructions**
  >1 instruction @ one time
  e.g., 5 pipelined instructions

- **Parallel Data**
  >1 data item @ one time
  e.g., Add of 4 pairs of words

- **Hardware descriptions**
  All gates @ one time

- **Programming Languages**

Harness Parallelism & Achieve High Performance

Warehouse Scale Computer

Smart Phone

Computer

Core   ...   Core

Memory   (Cache)

Input/Output

Core

Instruction Unit(s)

Functional Unit(s)

A_0+B_0 A_1+B_1 A_2+B_2 A_3+B_3

Today

Cache Memory

Logic Gates

2

Levels of Representation/ Interpretation

High Level Language Program (e.g., C)

Compiler

Assembly Language Program (e.g., MIPS)

Assembler

Machine Language Program (MIPS)

Machine Interpretation

Hardware Architecture Description (e.g., block diagrams)

Architecture Implementation

Logic Circuit Description (Circuit Schematic Diagrams)

```
temp = v[k];
v[k] = v[k+1];
v[k+1] = temp;
```

```
lw    $t0, 0($2)
lw    $t1, 4($2)
sw    $t1, 0($2)
sw    $t0, 4($2)
```

Anything can be represented as a *number*, i.e., data or instructions

```
0000 1001 1100 0110 1010 1111 0101 1000
1010 1111 0101 1000 0000 1001 1100 0110
1100 0110 1010 1111 0101 1000 0000 1001
0101 1000 0000 1001 1100 0110 1010 1111
```

Register File

ALU
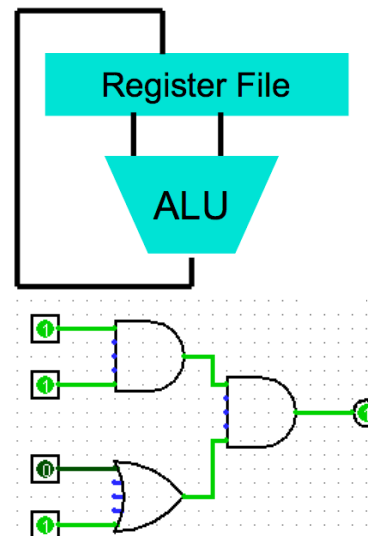
Hardware Design

- Next several weeks: how a modern processor is built, starting with basic elements as building blocks

- Why study hardware design?
  - Understand capabilities and limitations of HW in general and processors in particular
  - What processors can do fast and what they can't do fast (avoid slow things if you want your code to run fast!)
  - Background for more in-depth HW courses (CS 150, CS 152)
  - Hard to know what you'll need for next 30 years
  - There is only so much you can do with standard processors: you may need to design own custom HW for extra performance
    - Even some commercial processors today have customizable hardware!

Synchronous Digital Systems

Hardware of a processor, such as the MIPS, is an example of a Synchronous Digital System

Synchronous:

- All operations coordinated by a central clock
 - "Heartbeat" of the system!

Digital:

- Represent all values by discrete values
- Two binary digits: 1 and 0
- Electrical signals are treated as 1's and 0's
  - 1 and 0 are complements of each other
- High /low voltage for true / false, 1 / 0

Switches: Basic Element of Physical Implementations

- Implementing a simple circuit (arrow shows action if wire changes to "1" or is *asserted*):
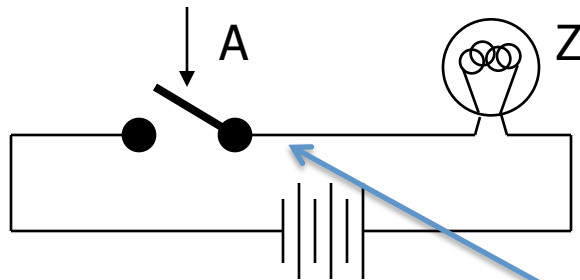
Close switch (if A is "1" or asserted) and turn on light bulb (Z)
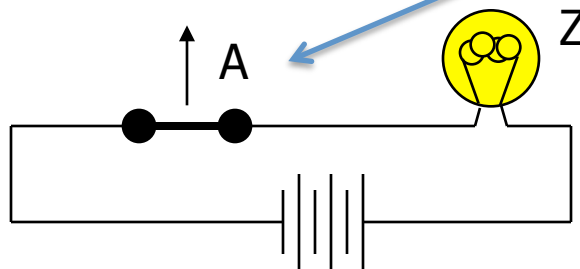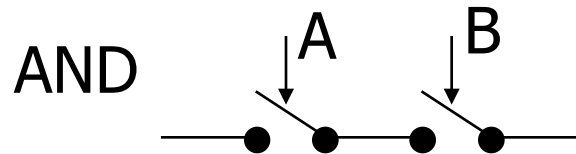
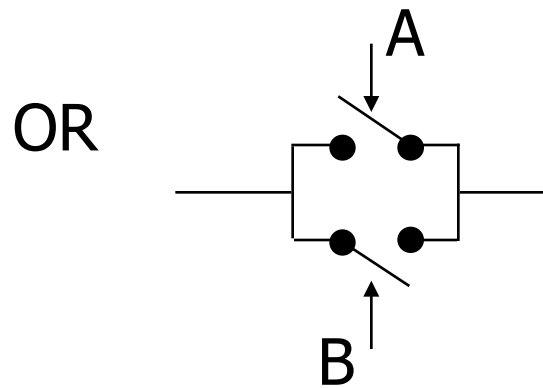*Open* switch (if A is "0" or unasserted) and turn off light bulb (Z)

$$Z \equiv A$$

Switches (cont'd)

- Compose switches into more complex ones (Boolean functions):

AND

$Z \equiv$ A $\underline{\text{and}}$ B

OR

$Z \equiv$ A $\underline{\text{or}}$ B

Historical Note

- Early computer designers built ad hoc circuits from switches

- Began to notice common patterns in their work: ANDs, ORs, …

- Master's thesis (by Claude Shannon) made link between work and 19th Century Mathematician George Boole
  - Called it "Boolean" in his honor

- Could apply math to give theory to hardware design, minimization, …
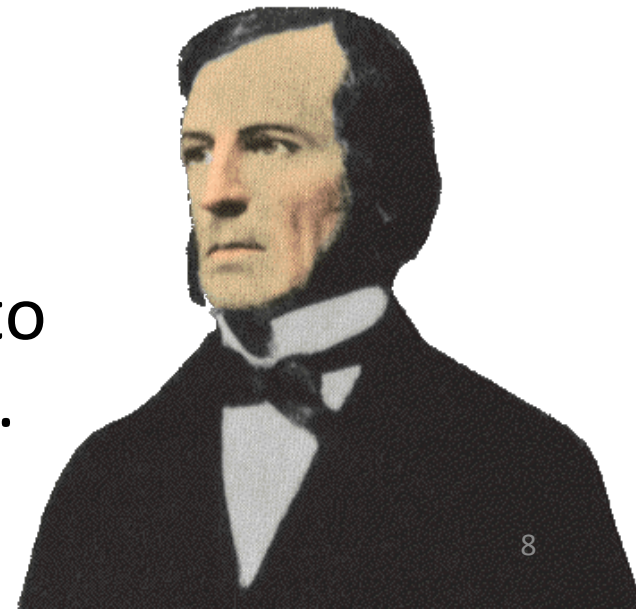
Transistors

- High voltage (V_{dd}) represents 1, or true
  - In modern microprocessors, Vdd ~ 1.0 Volt
- Low voltage (0 Volt or Ground) represents 0, or false
- Pick a midpoint voltage to decide if a 0 or a 1
  - Voltage greater than midpoint = 1
  - Voltage less than midpoint = 0
  - This removes noise as signals propagate – a big advantage of digital systems over analog systems
- If one switch can control another switch, we can build a computer!
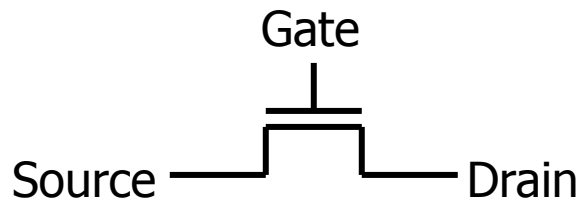- Our switches: CMOS transistors

CMOS Transistor Networks

- Modern digital systems designed in CMOS
  - MOS: Metal-Oxide on Semiconductor
  - C for complementary: use *pairs* of normally-open and normally-closed switches
    - Used to be called COS-MOS for complementary-symmetry - MOS

- CMOS transistors act as voltage-controlled switches
  - Similar, though easier to work with, than electro-mechanical relay switches from earlier era
  - Use energy primarily when switching

CMOS Transistors
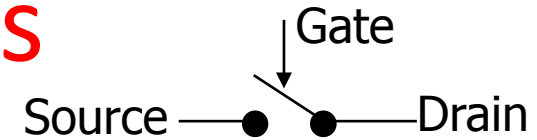
Gate
Source ———● ●———Drain

- Three terminals: source, gate, and drain
  - Switch action:
    if voltage on gate terminal is (some amount) higher/lower than source terminal then conducting path established between drain and source terminals (switch is closed)
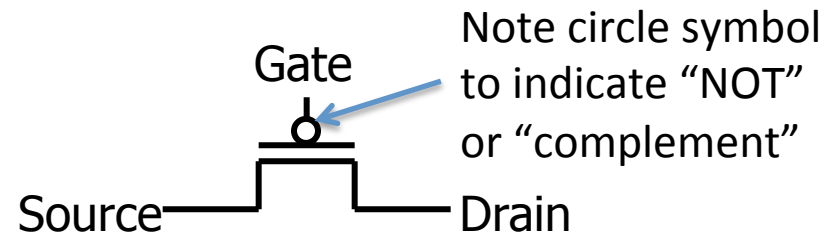
Gate
Source ——⊓——Drain

Gate
Source ——⊓——Drain

Note circle symbol to indicate "NOT" or "complement"

n-channel transitor
open when voltage at Gate is low
closes when:
voltage(Gate) > voltage (Threshold)
(High resistance when gate voltage Low, Low resistance when gate voltage High)

p-channel transistor
closed when voltage at Gate is low
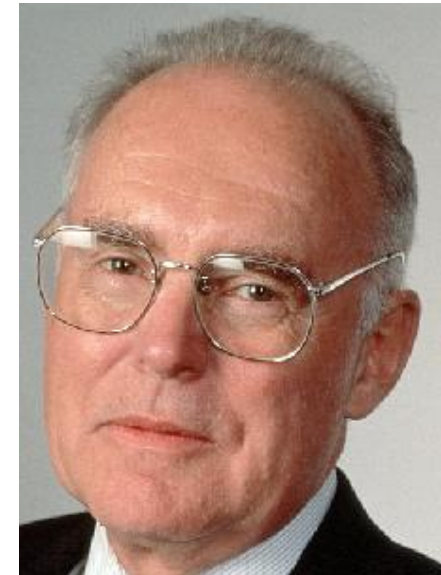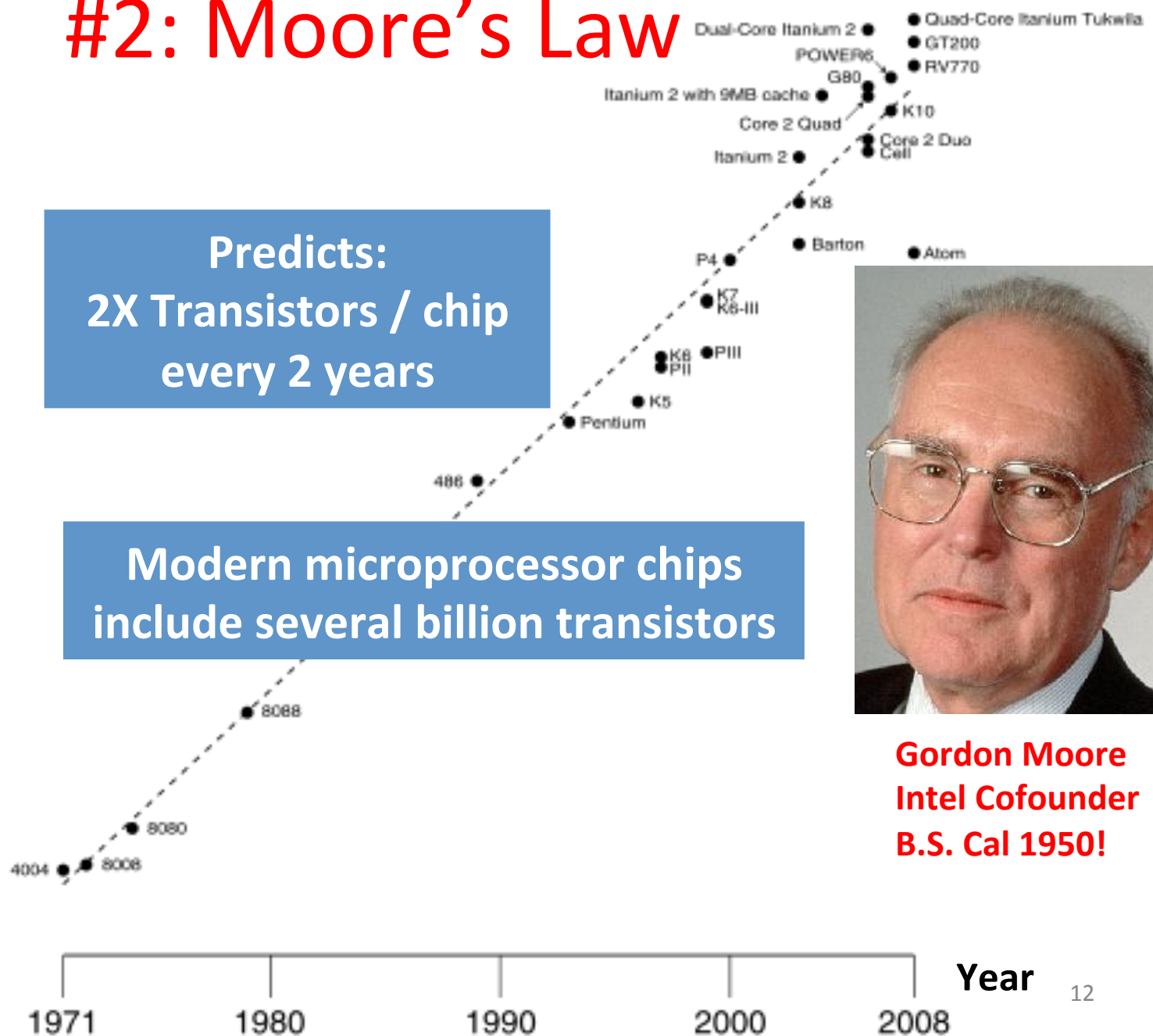opens when:
voltage(Gate) > voltage (Threshold)
(Low resistance when gate voltage Low, High resistance when gate voltage High)

#2: Moore's Law

# of transistors on an integrated circuit (IC)

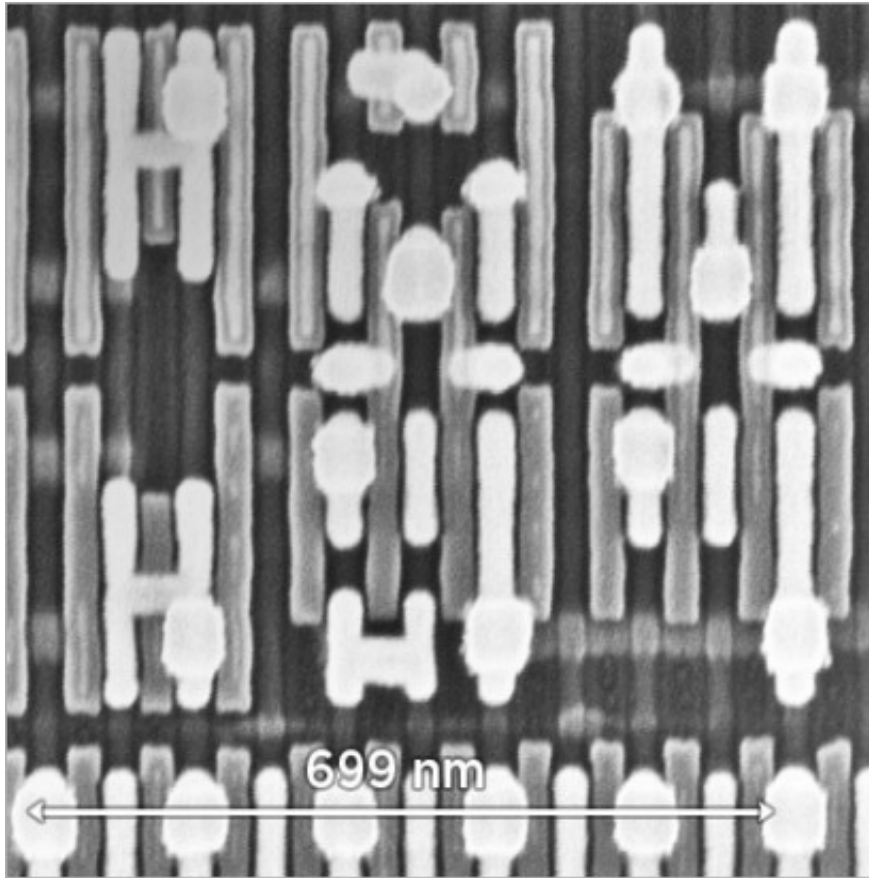**Predicts:
2X Transistors / chip
every 2 years**

**Modern microprocessor chips
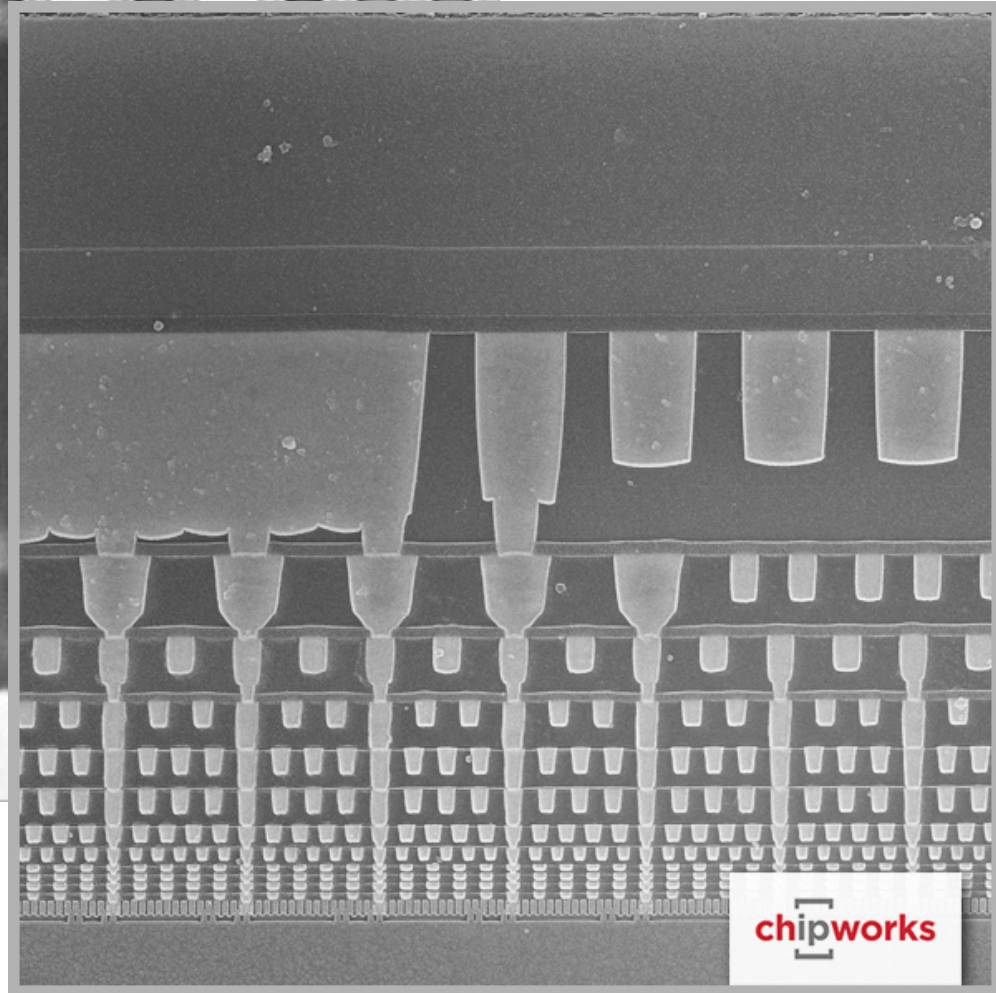include several billion transistors**

**Gordon Moore
Intel Cofounder
B.S. Cal 1950!**

Year

12

Intel 14nm Technology

Plan view of transistors

Side view of wiring layers

CMOS Circuit Rules

- Don't pass weak values => Use Complementary Pairs
  - N-type transistors pass weak 1's (V_{dd} - V_{th})
  - N-type transistors pass strong 0's (ground)
  - Use N-type transistors only to pass 0's (N for negative)
  - Converse for P-type transistors: Pass weak 0s, strong 1s
    - Pass weak 0's (V_{th}), strong 1's (V_{dd})
    - Use P-type transistors only to pass 1's (P for positive)
  - Use pairs of N-type and P-type to get strong values
- Never leave a wire undriven
  - Make sure there's always a path to V_{dd} or GND
- Never create a path from V_{dd} to GND (ground)
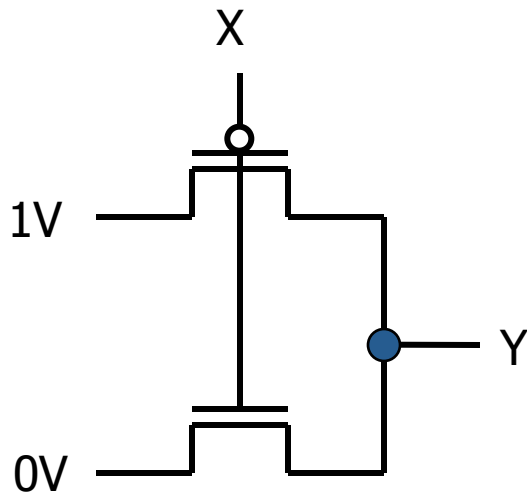 - This would short-circuit the power supply!

CMOS Networks

p-channel transistor
closed when voltage at Gate is low
opens when:
voltage(Gate) > voltage (Threshold)

X

1V

Y

0V

n-channel transitor
open when voltage at Gate is low
closes when:
voltage(Gate) > voltage (Threshold)

what is the
relationship
between x and y?

x	y
0 Volt (GND)	1 Volt (Vdd)
1 Volt (Vdd)	0 Volt (GND)

Called an *inverter* or *not gate*

Two-Input Networks
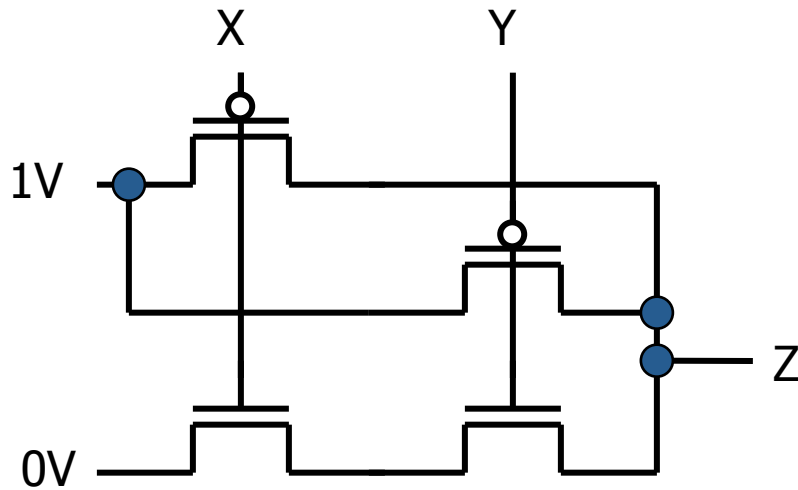
what is the
relationship between x, y and z?

x	y	z
0 Volt	0 Volt	1 Volt
0 Volt	1 Volt	1 Volt
1 Volt	0 Volt	1 Volt
1 Volt	1 Volt	0 Volt

Called a *NAND gate*
(NOT AND)

Clickers/Peer Instruction
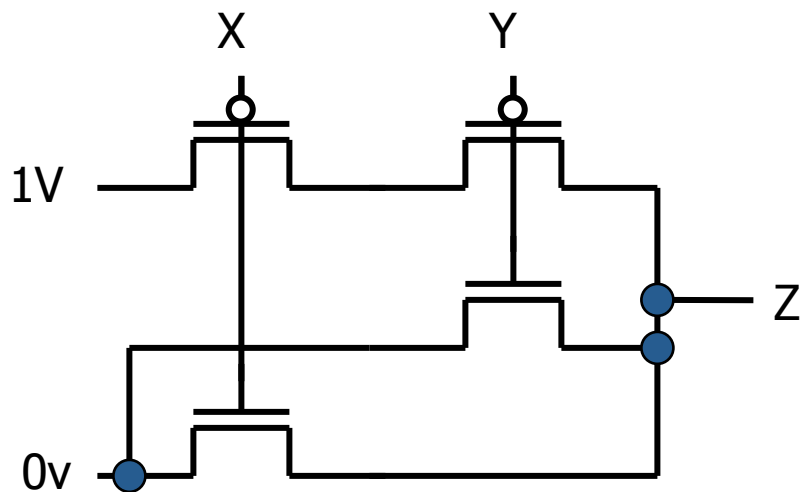
Administrivia

- Project 1-1 is out - due 3/01
  - See Sagar @ end of lec. if you still don't have team
- Midterm is next Thursday 2/26, in class
  - Covers up to and including the previous lecture
  - 1 handwritten, double sided, 8.5"x11" cheat sheet
  - We'll give you MIPS green sheet
  - DSP: Should have received email from Sagar this morning
 - Conflicts/DSP must email/respond by tomorrow (Weds.) @ 23:59:59
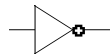
Administrivia

- Review Sessions:
  - TA: Probably 2/23, 6-8pm, waiting for room reservation
  - HKN: Saturday 2/21, 1-4pm, 100 GPB

Combinational Logic Symbols

- Common combinational logic systems have standard symbols called logic gates

    - Buffer, NOT

        A ─▷─ Z   ─▷○─

    - AND, NAND

        A ─┐
        B ─┘ ⊃─ Z   ─⊃○─

    - OR, NOR

        A ─┐
        B ─┘ ⊃─ Z   ─⊃○─
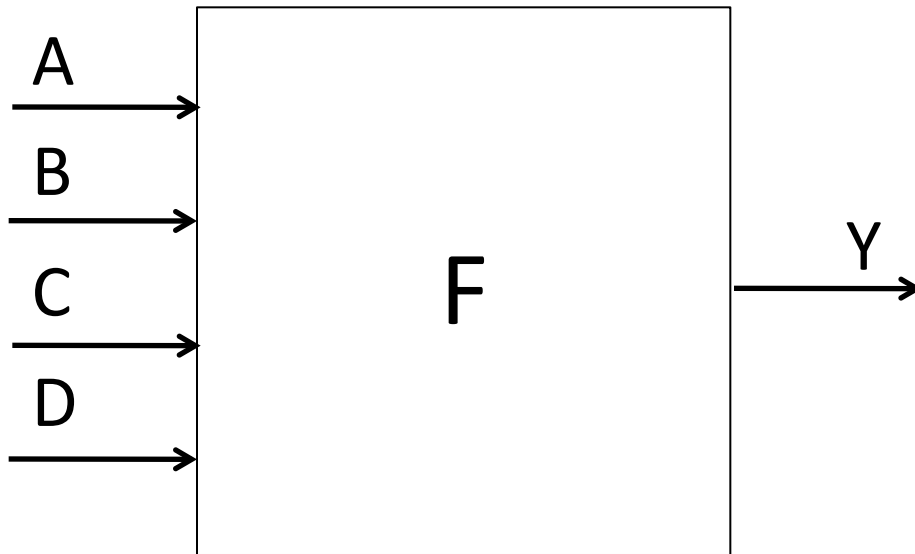
Inverting versions (NOT, NAND, NOR) easiest to implement with CMOS transistors (the switches we have available and use most)

Truth Tables
for Combinational Logic

a	b	c	d	y
0	0	0	0	F(0,0,0,0)
0	0	0	1	F(0,0,0,1)
0	0	1	0	F(0,0,1,0)
0	0	1	1	F(0,0,1,1)
0	1	0	0	F(0,1,0,0)
0	1	0	1	F(0,1,0,1)
0	1	1	0	F(0,1,1,0)
0	1	1	1	F(0,1,1,1)
1	0	0	0	F(1,0,0,0)
1	0	0	1	F(1,0,0,1)
1	0	1	0	F(1,0,1,0)
1	0	1	1	F(1,0,1,1)
1	1	0	0	F(1,1,0,0)
1	1	0	1	F(1,1,0,1)
1	1	1	0	F(1,1,1,0)
1	1	1	1	F(1,1,1,1)

A

B

C

D

F

Y

Exhaustive list of the output value generated for each combination of inputs

Truth Table Example #1:
$y = F(a,b)$: 1 iff $a \neq b$

a	b	y
0	0	0
0	1	1
1	0	1
1	1	0

Truth Table Example #2: 2-bit Adder

A $a_1 a_0$	B $b_1 b_0$	C $c_2 c_1 c_0$
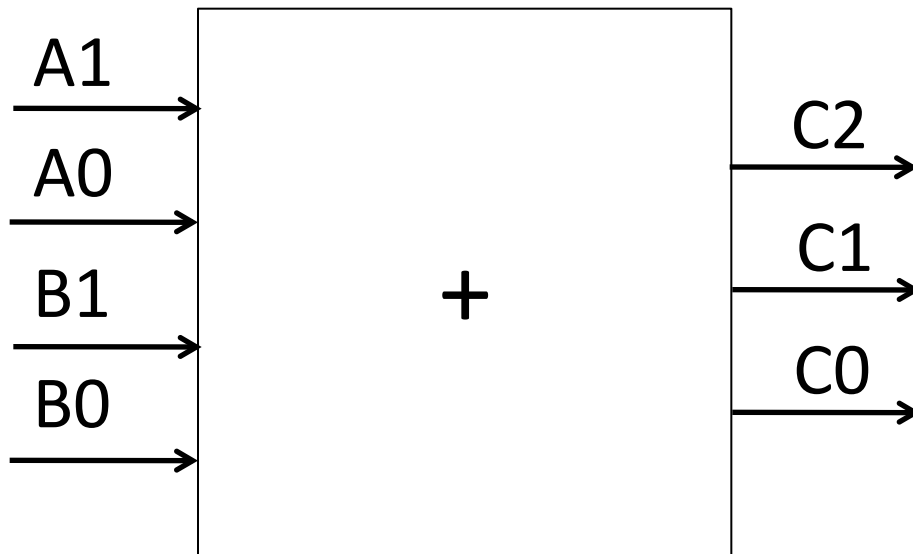
How Many Rows?

A1

A0

B1

B0

+

C2

C1

C0

Truth Table Example #3: 32-bit Unsigned Adder

A	B	C
000 ... 0	000 ... 0	000 ... 00
000 ... 0	000 ... 1	000 ... 01
.	.	.
.	.	.
.	.	.
111 ... 1	111 ... 1	111 ... 10

How Many Rows?

Truth Table Example #4: 3-input Majority Circuit

a	b	c	y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

Y =

This is called *Sum of Products* form; Just another way to represent the TT as a logical expression

More simplified forms (fewer gates and wires)

Boolean Algebra

- Use plus "+" for OR
  - "logical sum"
- Use product for AND (a•b or implied via ab)
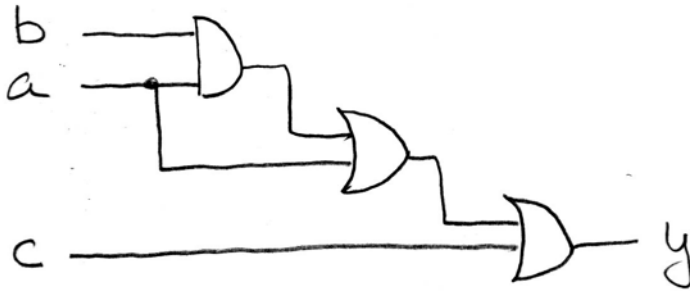 - "logical product"
- "Hat" to mean complement (NOT)
- Thus

$ab + a + \bar{c}$

$= a•b + a + \bar{c}$

$=$ (a AND b) OR a OR (NOT c)

Boolean Algebra: Circuit & Algebraic Simplification

original circuit

$$y = ((ab) + a) + c$$

equation derived from original circuit

$$= ab + a + c$$
$$= a(b + 1) + c$$
$$= a(1) + c$$
$$= a + c$$

algebraic simplification
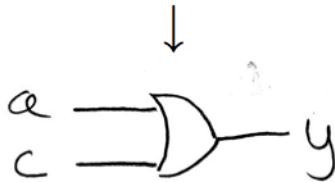
simplified circuit

Laws of Boolean Algebra

$X \overline{X} = 0$ $X + \overline{X} = 1$ Complementarity

$X \, 0 = 0$ $X + 1 = 1$ Laws of 0's and 1's

$X \, 1 = X$ $X + 0 = X$ Identities

$X \, X = X$ $X + X = X$ Idempotent Laws

$X \, Y = Y \, X$ $X + Y = Y + X$ Commutativity

$(X \, Y) \, Z = Z \, (Y \, Z)$ $(X + Y) + Z = Z + (Y + Z)$ Associativity

$X \, (Y + Z) = X \, Y + X \, Z$ $X + Y \, Z = (X + Y) \, (X + Z)$ Distribution

$X \, Y + X = X$ $(X + Y) \, X = X$ Uniting Theorem

$\overline{X} \, Y + X = X + Y$ $(\overline{X} + Y) \, X = X \, Y$ United Theorem v. 2

$\overline{X \, Y} = \overline{X} + \overline{Y}$ $\overline{X + Y} = \overline{X} \, \overline{Y}$ DeMorgan's Law

Boolean Algebraic Simplification Example

$$y = ab + a + c$$

Boolean Algebraic Simplification Example

$$y = ab + a + c$$

a b c y

0 0 0 0

0 0 1 1

0 1 0 0

0 1 1 1

1 0 0 1

1 0 1 1

1 1 0 1

1 1 1 1

$$= a(b + 1) + c \quad \text{distribution, identity}$$

$$= a(1) + c \quad \text{law of 1's}$$

$$= a + c \quad \text{identity}$$

Clickers/Peer Instruction

- Simplify $Z = A + BC + \overline{A}.(\overline{BC})$

- A: $Z = 0$

- B: $Z = A(1 + BC)$

- C: $Z = \overline{(A + BC)}$
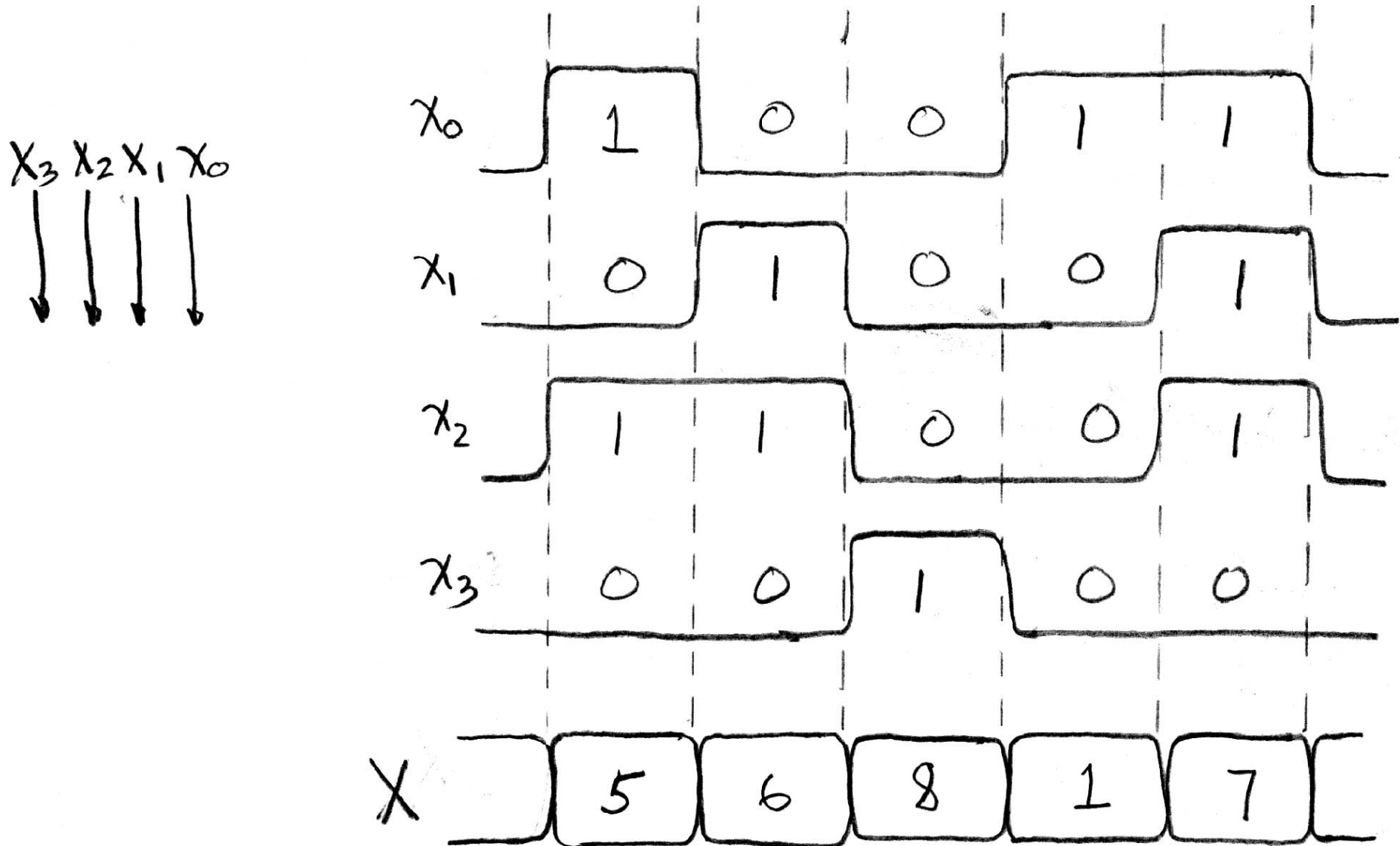
- D: $Z = BC$

- E: $Z = 1$

In the News: Spy Games

- Russian security firm claims US spy agencies insert code into disk drive firmware to snoop on foreign computers

- Also, attacks computers not connected to internet by secreting hardware that can listen to long-wave radio broadcasts
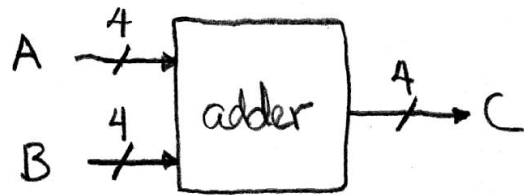
- Or through infected USB drives

Signals and Waveforms
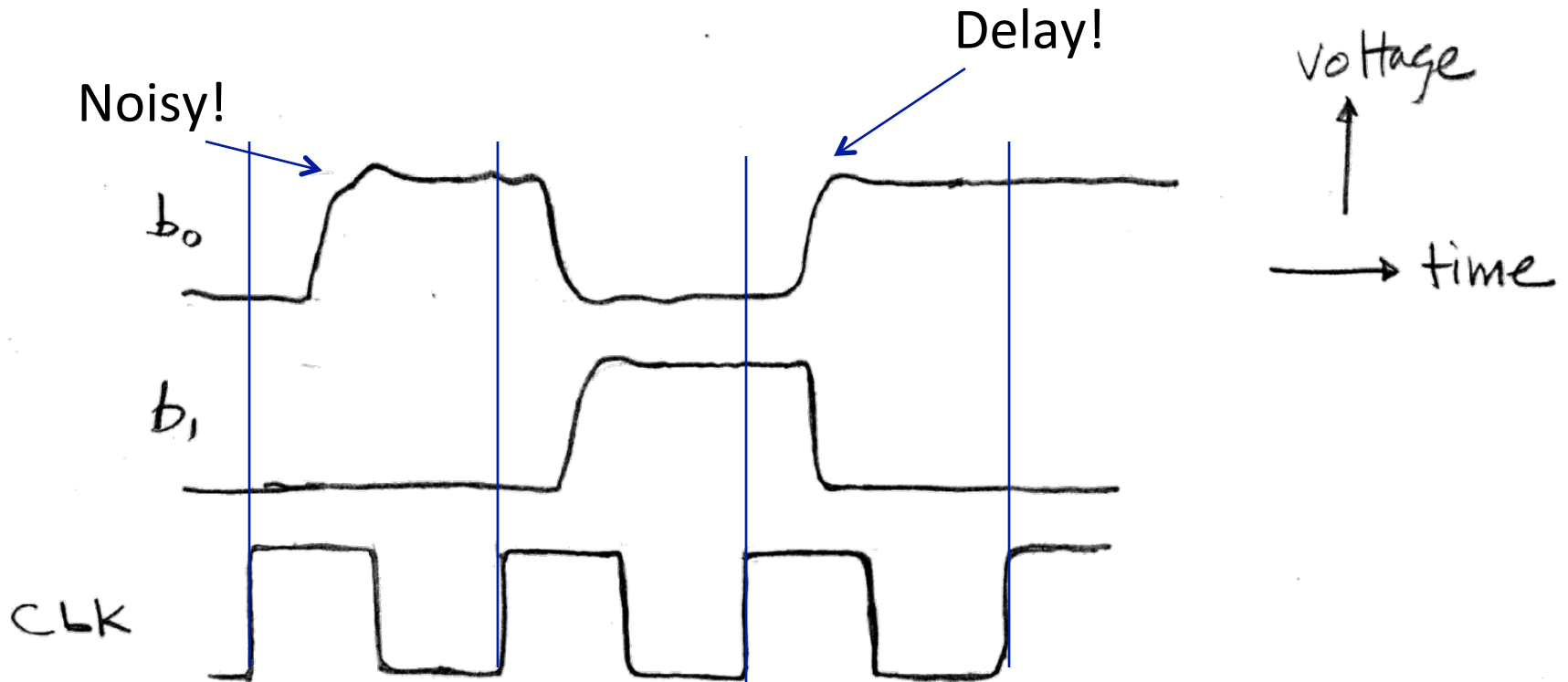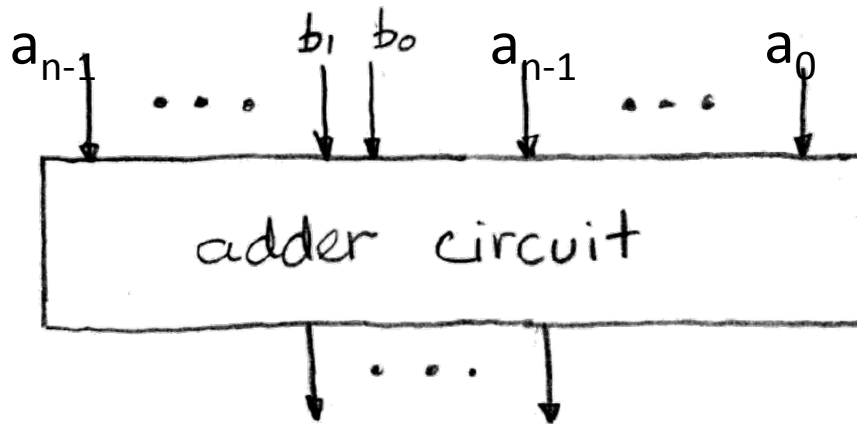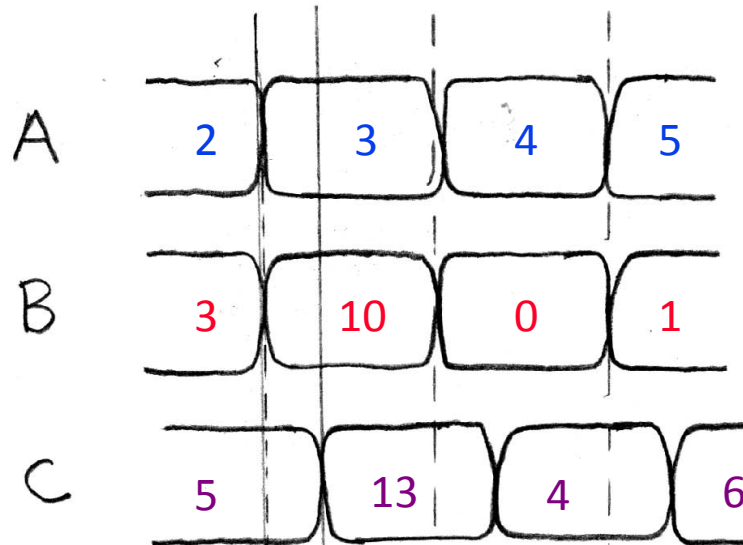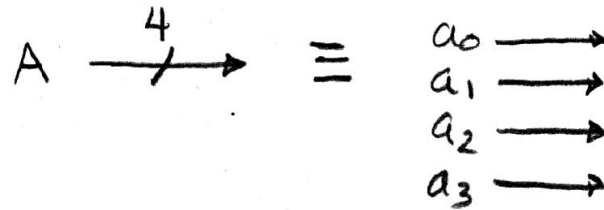
Signals and Waveforms: Grouping
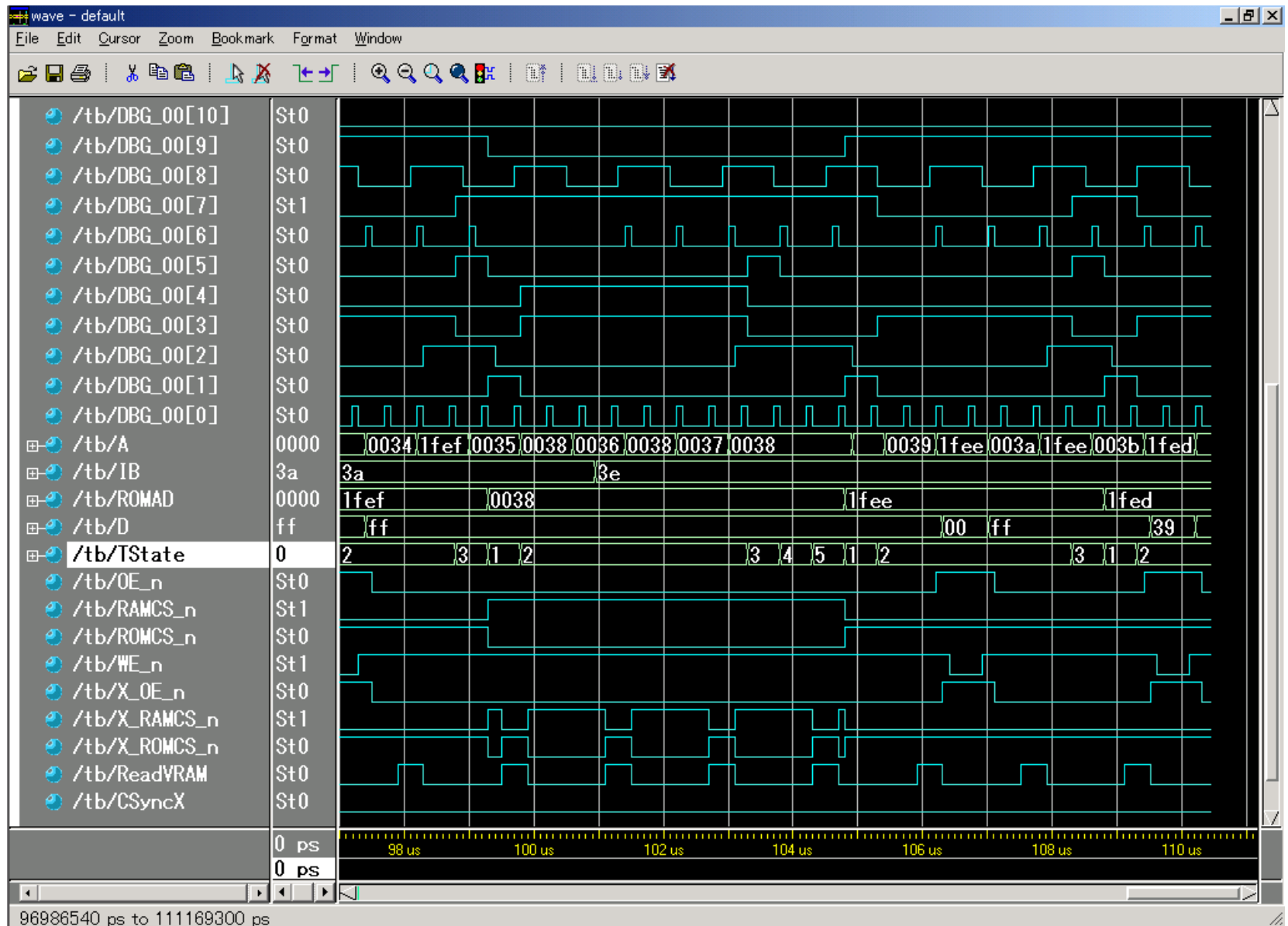
Signals and Waveforms: Circuit Delay

A $\xrightarrow{4}$ [adder] $\xrightarrow{4}$ C

$A = [a_3, a_2, a_1, a_0]$

$B = [b_3, b_2, b_1, b_0]$

A $\xrightarrow{4}$ $\equiv$
$a_0 \longrightarrow$
$a_1 \longrightarrow$
$a_2 \longrightarrow$
$a_3 \longrightarrow$

A | 2 | 3 | 4 | 5

B | 3 | 10 | 0 | 1

C | 5 | 13 | 4 | 6

$\rightarrow$ |← adder propagation delay

Sample Debugging Waveform

Type of Circuits

- *Synchronous Digital Systems* consist of two basic types of circuits:
  - Combinational Logic (CL) circuits
    - Output is a function of the inputs only, not the history of its execution
    - E.g., circuits to add A, B (ALUs)
  - Sequential Logic (SL)
    - Circuits that "remember" or store information
    - aka "State Elements"
    - E.g., memories and registers (Registers)

Uses for State Elements

- Place to store values for later re-use:
  - Register files (like $1-$31 in MIPS)
  - Memory (caches and main memory)
- *Help control flow of information between combinational logic blocks*
  - State elements hold up the movement of information at input to combinational logic blocks to allow for orderly passage

Accumulator Example
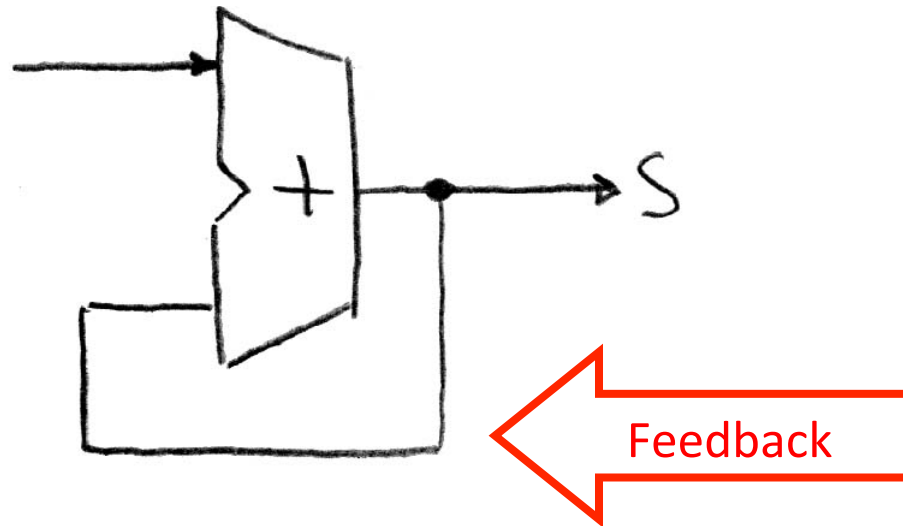
Why do we need to control the flow of information?

x_i ——/——> **SUM** ——/——> S
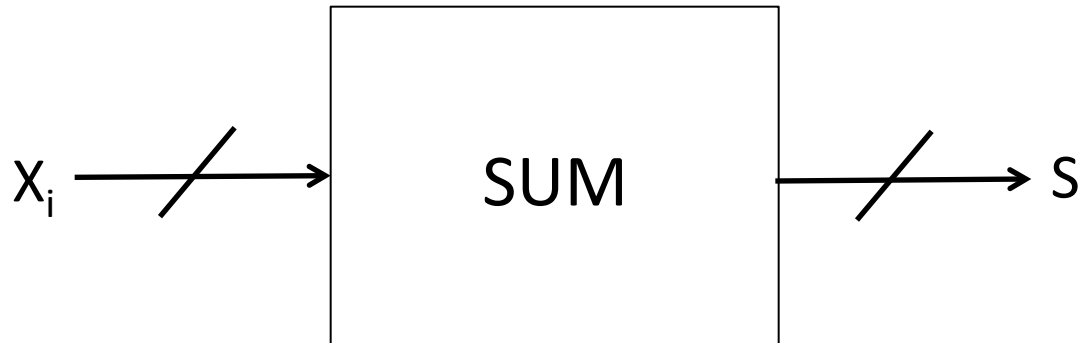
Want: `S=0;`
            `for (i=0;i<n;i++)`
                `S = S + X`$_i$

Assume:
- Each X value is applied in succession, one per cycle
- After n cycles the sum is present on S
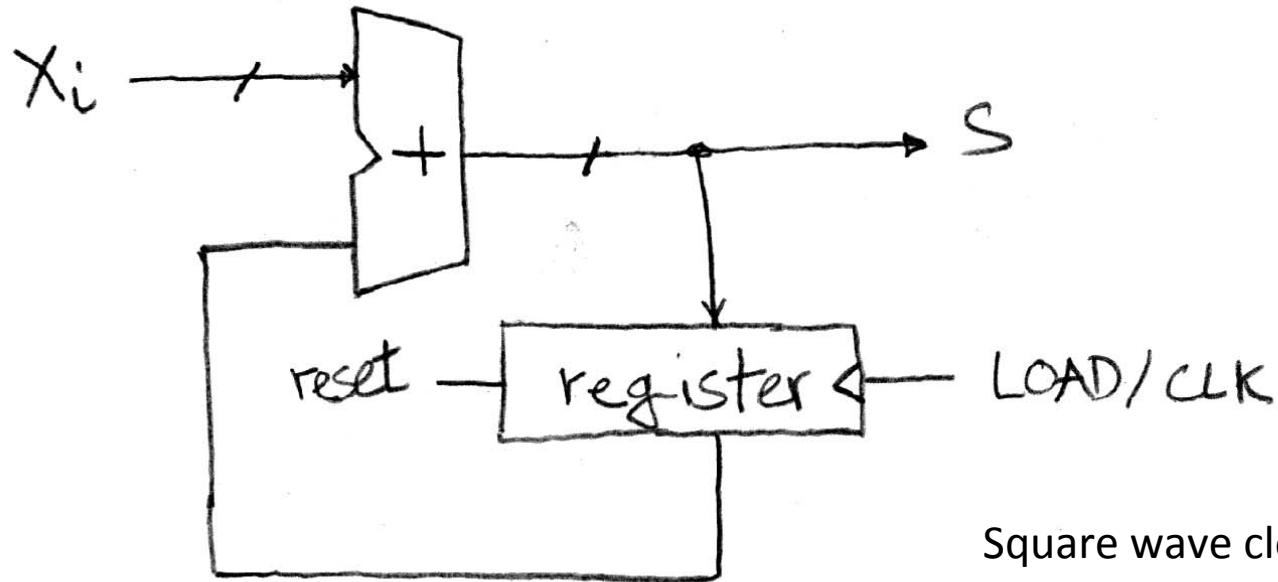
First Try: Does this work?

Feedback

No!

Reason #1: How to control the next iteration of the 'for' loop?

Reason #2: How do we say: 'S=0'?

Second Try: How About This?

Register is used to hold up the transfer of data to adder
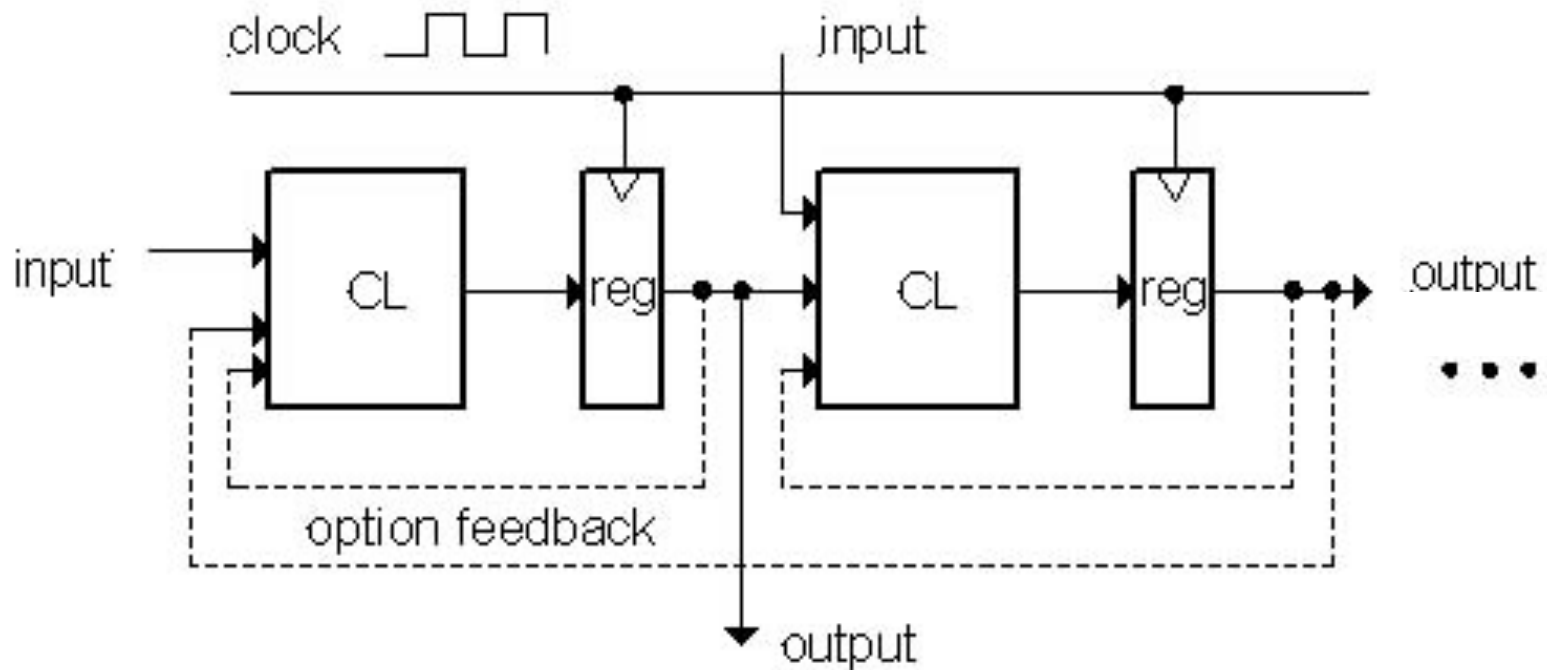
Square wave clock sets when things change

Rough timing …

Rounded Rectangle per clock means could be 1 or 0

Xi must be ready **before** clock edge due to adder delay

Model for Synchronous Systems

- Collection of Combinational Logic blocks separated by registers
- Feedback is optional
- Clock signal(s) connects only to clock input of registers
- Clock (CLK): steady square wave that synchronizes the system
- Register: several bits of state that samples on rising edge of CLK (positive edge-triggered) or falling edge (negative edge-triggered)

Register Internals
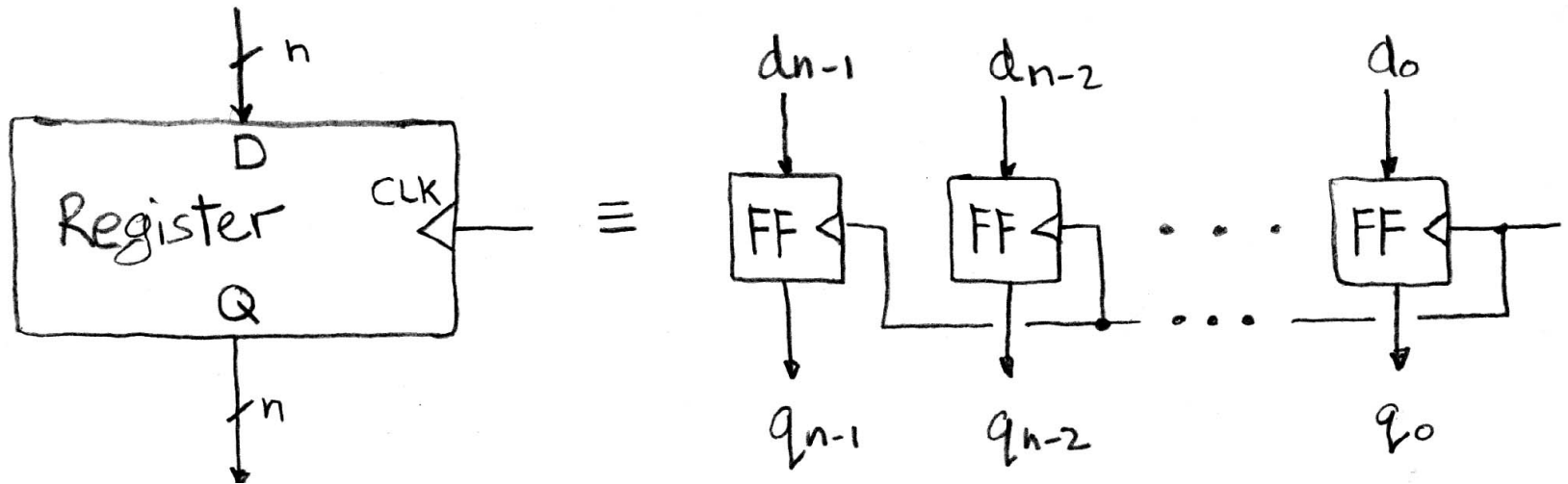
- n instances of a "Flip-Flop"

- Flip-flop name because the output flips and flops between 0 and 1

- D is "data input", Q is "data output"

- Also called "D-type Flip-Flop"

Camera Analogy Timing Terms

- Want to take a portrait – timing right before and after taking picture

- *Set up time* – don't move since about to take picture (open camera shutter)

- *Hold time* – need to hold still after shutter opens until camera shutter closes

- *Time click to data* – time from open shutter until can see image on output (viewscreen)

Hardware Timing Terms

- Setup Time: when the input must be stable *before* the edge of the CLK

- Hold Time: when the input must be stable *after* the edge of the CLK

- "CLK-to-Q" Delay: how long it takes the output to change, measured from the edge of the CLK

Maximum Clock Frequency

- What is the maximum frequency of this circuit?
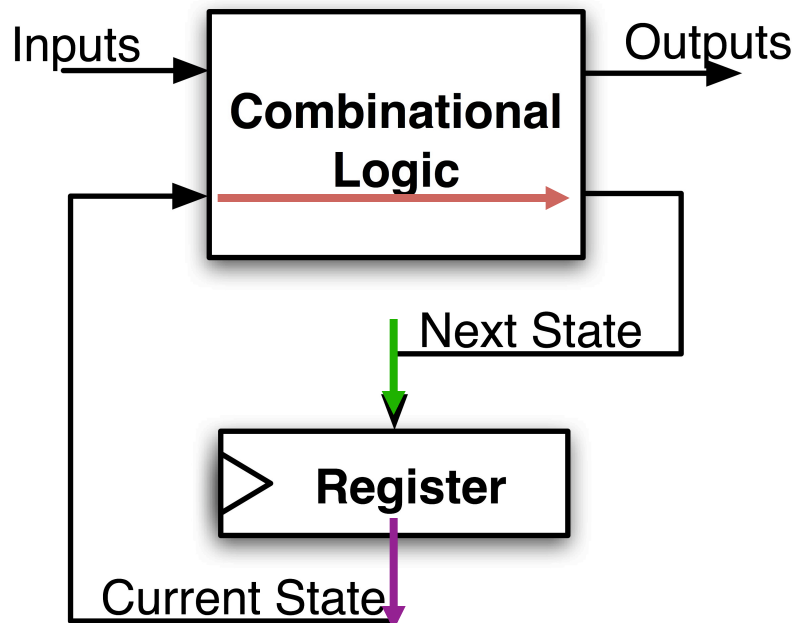
Hint:
Frequency = 1/Period

Max Delay =   Setup Time + CLK-to-Q Delay + CL Delay

And in Conclusion, …

- Multiple Hardware Representations
  - Analog voltages quantized to represent logic 0 and logic 1
  - Transistor switches form gates: AND, OR, NOT, NAND, NOR
  - Truth table mapped to gates for combinational logic design
  - Boolean algebra for gate minimization
- State Machines
  - Finite State Machines: made from *Stateless* combinational logic and *Stateful* "Memory" Logic (aka Registers)
  - Clocks synchronize D-FF change (Setup and Hold times important!)