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How to Implement Bagging From Scratch With Python

by Jason Brownlee on November 11, 2016 in Algorithms From Scratch









Decision trees are a simple and powerful predictive modeling technique, but they suffer from high-variance.

This means that trees can get very different results given different training data.

A technique to make decision trees more robust and to achieve better performance is called bootstrap aggregation or bagging for short.

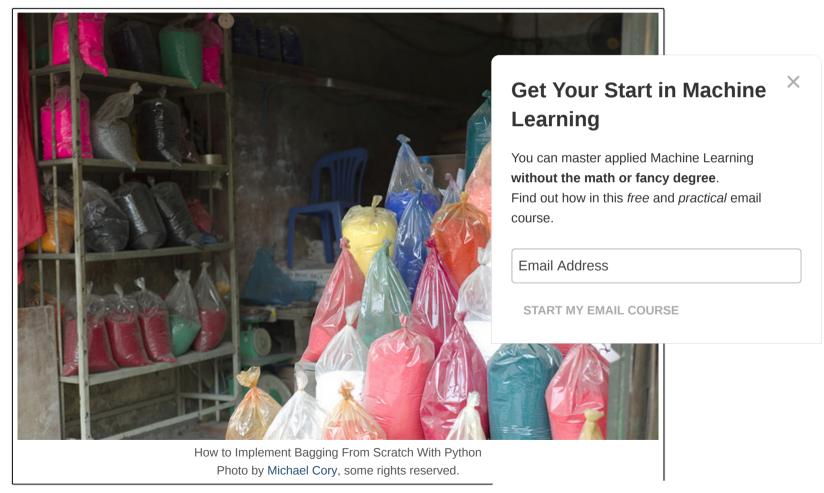
In this tutorial, you will discover how to implement the bagging procedure with decision trees from scratch with Python.

After completing this tutorial, you will know:

- How to create a bootstrap sample of your dataset.
- How to make predictions with bootstrapped models.
- How to apply bagging to your own predictive modeling problems.

Let's get started.

- Update Jan/2017: Changed the calculation of fold_size in cross_validation_split() to always be an integer. Fixes issues with Python 3.
- Update Feb/2017: Fixed a bug in build tree.
- Update Aug/2017: Fixed a bug in Gini calculation, added the missing weighting of group Gini scores by group size (thanks Michael!).



Descriptions

This section provides a brief description to Bootstrap Aggregation and the Sonar dataset that will be used in this tutorial.

Bootstrap Aggregation Algorithm

A bootstrap is a sample of a dataset with replacement.

This means that a new dataset is created from a random sample of an existing dataset where a given row may be selected and added more than once to the sample.

It is a useful approach to use when estimating values such as the mean for a broader dataset, when you only have a limited dataset available. By

creating samples of your dataset and estimating the mean from those samples, you can take the avertue mean of the underlying problem.

This same approach can be used with machine learning algorithms that have a high variance, such a each bootstrap sample of data and the average output of those models used to make predictions. The bagging for short.

Variance means that an algorithm's performance is sensitive to the training data, with high variance changed, the more the performance of the algorithm will vary.

The performance of high variance machine learning algorithms like unpruned decision trees can be average of their predictions. Results are often better than a single decision tree.

Another benefit of bagging in addition to improved performance is that the bagged decision trees cal added until a maximum in performance is achieved.

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Sonar Dataset

The dataset we will use in this tutorial is the Sonar dataset.

This is a dataset that describes sonar chirp returns bouncing off different surfaces. The 60 input variables are the strength of the returns at different angles. It is a binary classification problem that requires a model to differentiate rocks from metal cyl **Get Your Start in Machine Learning**

ne

It is a well-understood dataset. All of the variables are continuous and generally in the range of 0 to 1. The output variable is a string of normal and "R" for rock, which will need to be converted to integers 1 and 0.

By predicting the class with the most observations in the dataset (M or mines) the Zero Rule Algorithm can achieve an accuracy of 53%.

You can learn more about this dataset at the UCI Machine Learning repository.

Download the dataset for free and place it in your working directory with the filename sonar.all-data.csv.

Tutorial

This tutorial is broken down into 2 parts:

- 1. Bootstrap Resample.
- 2. Sonar Dataset Case Study.

These steps provide the foundation that you need to implement and apply bootstrap aggregation wit problems.

1. Bootstrap Resample

Let's start off by getting a strong idea of how the bootstrap method works.

We can create a new sample of a dataset by randomly selecting rows from the dataset and adding the number of rows or until the size of the new dataset matches a ratio of the size of the original dataset

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We can allow sampling with replacement by not removing the row that was selected so that it is available for future selections.

Below is a function named **subsample()** that implements this procedure. The **randrange()** function from the random module is used to select a random row index to add to the sample each iteration of the loop. The default size of the sample is the size of the original dataset.

1 # Create a random subsample from the dataset with replacement
2 def subsample(dataset, ratio=1.0):
3 sample = list()
4 n_sample = round(len(dataset) * ratio)
5 while len(sample) < n_sample:</pre>

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X

13

14

15

18

19 20

21 seed(1)
22 # True mean

```
index = randrange(len(dataset))
sample.append(dataset[index])
return sample
```

We can use this function to estimate the mean of a contrived dataset.

First, we can create a dataset with 20 rows and a single column of random numbers between 0 and 9 and calculate the mean value.

We can then make bootstrap samples of the original dataset, calculate the mean, and repeat this process until we have a list of means. Taking the average of these sample means should give us a robust estimate of the mean of the entire dataset.

The complete example is listed below.

return sample

17 def mean(numbers):

25 # Estimated means 26 ratio = 0.10

27 for size in [1, 10, 100]:

Each bootstrap sample is created as a 10% sample of the original 20 observation dataset (or 2 observations). We then experiment by creating 1, 10, 100 bootstrap samples of the original dataset, calculate their mean value, then average all of those estimates the control of the original dataset, calculate their mean value, then average all of those estimates the control of the original dataset, calculate their mean value, then average all of those estimates the control of the original dataset. **Get Your Start in Machine** from random import seed Learning from random import random from random import randrange You can master applied Machine Learning without the math or fancy degree. # Create a random subsample from the dataset with replacement Find out how in this free and practical email def subsample(dataset, ratio=1.0): course. sample = list() 9 n_sample = round(len(dataset) * ratio) 10 while len(sample) < n_sample:</pre> 11 index = randrange(len(dataset)) **Email Address** 12 sample.append(dataset[index])

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16 # Calculate the mean of a list of numbers

23 dataset = [[randrange(10)] for i in range(20)]

return sum(numbers) / float(len(numbers))

24 print('True Mean: %.3f' % mean([row[0] for row in dataset]))

```
sample_means = list()
for i in range(size):
sample = subsample(dataset, ratio)
sample_mean = mean([row[0] for row in sample])
sample_means.append(sample_mean)
print('Samples=%d, Estimated Mean: %.3f' % (size, mean(sample_means)))
```

Running the example prints the original mean value we aim to estimate.

We can then see the estimated mean from the various different numbers of bootstrap samples. We can see that with 100 samples we achieve a good estimate of the mean.

```
1 True Mean: 4.450
2 Samples=1, Estimated Mean: 4.500
3 Samples=10, Estimated Mean: 3.300
4 Samples=100, Estimated Mean: 4.480
```

Instead of calculating the mean value, we can create a model from each subsample.

Next, let's see how we can combine the predictions from multiple bootstrap models.

2. Sonar Dataset Case Study

In this section, we will apply the Random Forest algorithm to the Sonar dataset.

The example assumes that a CSV copy of the dataset is in the current working directory with the file

The dataset is first loaded, the string values converted to numeric and the output column is converte achieved with helper functions load_csv(), str_column_to_float() and str_column_to_int() to load

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We will use k-fold cross validation to estimate the performance of the learned model on unseen data. This means that we will construct and evaluate k models and estimate the performance as the mean model error. Classification accuracy will be used to evaluate each model. These behaviors are provided in the cross_validation_split(), accuracy_metric() and evaluate_algorithm() helper functions.

We will also use an implementation of the Classification and Regression Trees (CART) algorithm adapted for bagging including the helper functions test_split() to split a dataset into groups, gini_index() to evaluate a split point, get_split() to find an optimal split point, to_terminal(), split() and build tree() used to create a single decision tree, predict() to make a prediction with a decision tree

previous step to make a subsample of the training dataset

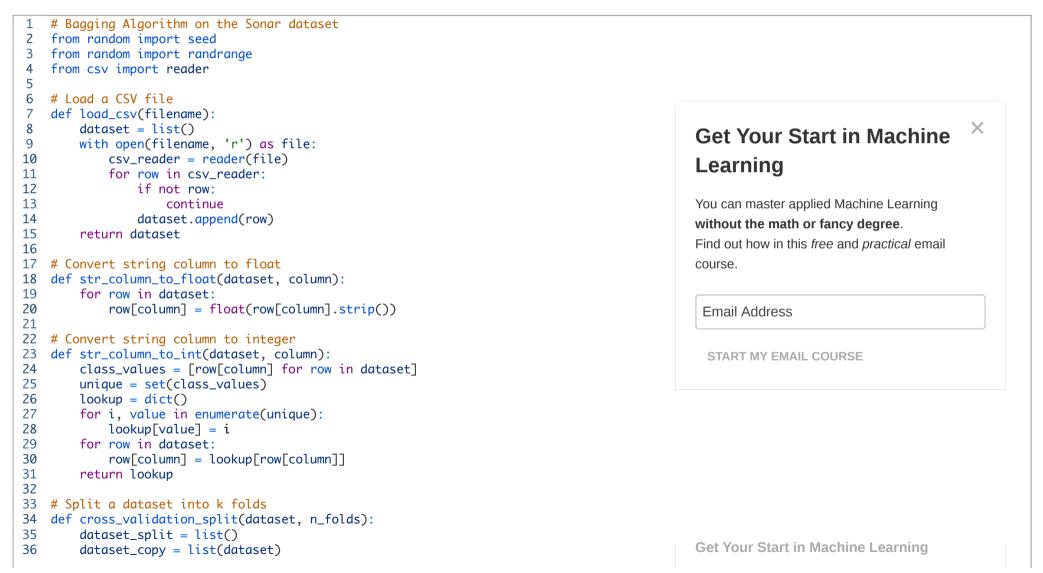
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is

A new function named **bagging_predict()** is developed that is responsible for making a prediction with each decision tree and combining the predictions into a single return value. This is achieved by selecting the most common prediction from the list of predictions made by the bagged trees.

Finally, a new function named **bagging()** is developed that is responsible for creating the samples of the training dataset, training a decision tree on each, then making predictions on the test dataset using the list of bagged trees.

The complete example is listed below.



```
37
        fold_size = int(len(dataset) / n_folds)
38
        for i in range(n folds):
            fold = list()
39
            while len(fold) < fold size:</pre>
40
                index = randrange(len(dataset_copy))
41
                fold.append(dataset_copy.pop(index))
42
43
            dataset_split.append(fold)
44
        return dataset_split
45
46
   # Calculate accuracy percentage
    def accuracy_metric(actual, predicted):
48
        correct = 0
        for i in range(len(actual)):
49
50
            if actual[i] == predicted[i]:
51
                correct += 1
52
        return correct / float(len(actual)) * 100.0
53
54 # Evaluate an algorithm using a cross validation split
   def evaluate_algorithm(dataset, algorithm, n_folds, *args):
56
        folds = cross_validation_split(dataset, n_folds)
57
        scores = list()
58
        for fold in folds:
59
            train_set = list(folds)
60
            train_set.remove(fold)
            train_set = sum(train_set, [])
61
62
            test_set = list()
63
            for row in fold:
64
                row_copy = list(row)
65
                test_set.append(row_copy)
                row\_copy[-1] = None
66
            predicted = algorithm(train_set, test_set, *args)
67
68
            actual = [row[-1]] for row in fold]
69
            accuracy = accuracy_metric(actual, predicted)
70
            scores.append(accuracy)
71
        return scores
72
73 # Split a dataset based on an attribute and an attribute value
   def test_split(index, value, dataset):
75
        left, right = list(), list()
76
        for row in dataset:
77
            if row[index] < value:</pre>
78
                left.append(row)
79
            else:
80
                right.append(row)
81
        return left, right
82
83 # Calculate the Gini index for a split dataset
```

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```
84 def gini_index(groups, classes):
85
        # count all samples at split point
        n_instances = float(sum([len(group) for group in groups]))
86
        # sum weighted Gini index for each group
87
        aini = 0.0
88
89
        for group in groups:
90
            size = float(len(group))
91
            # avoid divide by zero
92
            if size == 0:
93
                continue
94
            score = 0.0
95
            # score the group based on the score for each class
            for class_val in classes:
96
97
                p = [row[-1]] for row in group].count(class_val) / size
98
                score += p * p
99
            # weight the group score by its relative size
            qini += (1.0 - score) * (size / n_instances)
100
101
        return aini
102
103 # Select the best split point for a dataset
104 def get_split(dataset):
        class_values = list(set(row[-1] for row in dataset))
105
106
        b_index, b_value, b_score, b_groups = 999, 999, 999, None
        for index in range(len(dataset[0])-1):
107
            for row in dataset:
108
109
            # for i in range(len(dataset)):
            # row = dataset[randrange(len(dataset))]
110
                groups = test_split(index, row[index], dataset)
111
112
                qini = qini_index(qroups, class_values)
                if gini < b_score:</pre>
113
114
                    b_index, b_value, b_score, b_groups = index, row[index], gini, groups
        return {'index':b_index, 'value':b_value, 'groups':b_groups}
115
116
117 # Create a terminal node value
118 def to_terminal(group):
        outcomes = [row[-1] for row in group]
119
120
        return max(set(outcomes), key=outcomes.count)
121
122 # Create child splits for a node or make terminal
123 def split(node, max_depth, min_size, depth):
        left, right = node['groups']
124
        del(node['groups'])
125
        # check for a no split
126
127
        if not left or not right:
            node['left'] = node['right'] = to_terminal(left + right)
128
129
            return
130
        # check for max depth
```

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```
131
        if depth >= max depth:
132
            node['left'], node['right'] = to terminal(left), to terminal(right)
133
134
        # process left child
135
        if len(left) <= min size:</pre>
            node['left'] = to_terminal(left)
136
137
        else:
138
            node['left'] = get_split(left)
            split(node['left'], max_depth, min_size, depth+1)
139
140
        # process right child
        if len(right) <= min_size:</pre>
141
142
            node['right'] = to_terminal(right)
143
        else:
            node['right'] = get_split(right)
144
            split(node['right'], max_depth, min_size, depth+1)
145
146
147 # Build a decision tree
148 def build_tree(train, max_depth, min_size):
        root = get_split(train)
149
150
        split(root, max_depth, min_size, 1)
        return root
151
152
153 # Make a prediction with a decision tree
154 def predict(node, row):
155
        if row[node['index']] < node['value']:</pre>
156
            if isinstance(node['left'], dict):
157
                 return predict(node['left'], row)
158
            else:
159
                 return node['left']
160
        else:
161
            if isinstance(node['right'], dict):
162
                 return predict(node['right'], row)
163
            else:
164
                 return node['riaht']
165
166 # Create a random subsample from the dataset with replacement
167 def subsample(dataset, ratio):
168
        sample = list()
        n_sample = round(len(dataset) * ratio)
169
170
        while len(sample) < n_sample:</pre>
171
            index = randrange(len(dataset))
            sample.append(dataset[index])
172
173
        return sample
174
175 # Make a prediction with a list of bagged trees
176 def bagging_predict(trees, row):
177
        predictions = [predict(tree, row) for tree in trees]
```

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```
178
         return max(set(predictions), key=predictions.count)
179
180 # Bootstrap Aggregation Algorithm
181 def bagging(train, test, max_depth, min_size, sample_size, n_trees):
182
        trees = list()
        for i in range(n_trees):
183
184
            sample = subsample(train, sample_size)
            tree = build_tree(sample, max_depth, min_size)
185
186
            trees.append(tree)
        predictions = [bagging_predict(trees, row) for row in test]
187
        return(predictions)
188
189
190 # Test bagging on the sonar dataset
191 seed(1)
192 # load and prepare data
193 filename = 'sonar.all-data.csv'
194 dataset = load_csv(filename)
195 # convert string attributes to integers
196 for i in range(len(dataset[0])-1):
                                                                                                 Get Your Start in Machine
        str_column_to_float(dataset, i)
197
198 # convert class column to integers
                                                                                                 Learning
199 str_column_to_int(dataset, len(dataset[0])-1)
200 # evaluate algorithm
201 \text{ n_folds} = 5
                                                                                                 You can master applied Machine Learning
202 \text{ max\_depth} = 6
                                                                                                 without the math or fancy degree.
203 \text{ min size} = 2
                                                                                                 Find out how in this free and practical email
204 sample_size = 0.50
205 for n_{\text{trees}} in [1, 5, 10, 50]:
                                                                                                 course.
        scores = evaluate_algorithm(dataset, bagging, n_folds, max_depth, min_size, sample_
206
        print('Trees: %d' % n_trees)
207
        print('Scores: %s' % scores)
208
                                                                                                  Email Address
        print('Mean Accuracy: %.3f%' % (sum(scores)/float(len(scores))))
209
```

A k value of 5 was used for cross-validation, giving each fold 208/5 = 41.6 or just over 40 records to

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Deep trees were constructed with a max depth of 6 and a minimum number of training rows at each node of 2. Samples of the training dataset were created with 50% the size of the original dataset. This was to force some variety in the dataset subsamples used to train each tree. The default for bagging is to have the size of sample datasets match the size of the original training dataset.

A series of 4 different numbers of trees were evaluated to show the behavior of the algorithm.

The accuracy from each fold and the mean accuracy for each configuration are printed. We can see a trend of some minor lift in performance as the number of trees is increased. **Get Your Start in Machine Learning**

```
Trees: 1

Scores: [87.8048780487805, 65.85365853658537, 65.85365853658537, 65.85365853658537, 73.17073170731707]

Mean Accuracy: 71.707%

Trees: 5

Scores: [60.97560975609756, 80.48780487804879, 78.04878048780488, 82.92682926829268, 63.41463414634146]

Mean Accuracy: 73.171%

Trees: 10

Scores: [60.97560975609756, 73.17073170731707, 82.92682926829268, 80.48780487804879, 68.29268292682927]

Mean Accuracy: 73.171%

Trees: 50

Scores: [63.41463414634146, 75.60975609756098, 80.48780487804879, 75.60975609756098, 85.36585365853658]

Mean Accuracy: 76.098%
```

A difficulty of this method is that even though deep trees are constructed, the bagged trees that are created are very similar. In turn, the predictions made

by these trees are also similar, and the high variance we desire among the trees trained on different

This is because of the greedy algorithm used in the construction of the trees selecting the same or s

The tutorial tried to re-inject this variance by constraining the sample size used to train each tree. At that may be evaluated when creating each split point. This is the method used in the Random Forest

Extensions

- **Tune the Example**. Explore different configurations for the number of trees and even individual results.
- Bag Another Algorithm. Other algorithms can be used with bagging. For example, a k-nearest high variance and is a good candidate for bagging.
- **Regression Problems**. Bagging can be used with regression trees. Instead of predicting the most common class value from the set of predictions, you can return the average of the predictions from the bagged trees. Experiment on regression problems.

Did you try any of these extensions?

Share your experiences in the comments below.

Review

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In this tutorial, you discovered how to implement bootstrap aggregation from scratch with Python.

Specifically, you learned:

- How to create a subsample and estimate bootstrap quantities.
- How to create an ensemble of decision trees and use them to make predictions.
- How to apply bagging to a real world predictive modeling problem.

Do you have any questions?

Ask your questions in the comments below and I will do my best to answer.

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About Jason Brownlee

Dr. Jason Brownlee is a husband, proud father, academic researcher, author, professional developer and a machine learning practitioner. He is dedicated to helping developers get started and get good at applied machine learning. Learn more.

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< How To Implement The Decision Tree Algorithm From Scratch In Python

6 Responses to How to Implement Bagging From Scratch With Python



skorzec January 18, 2017 at 4:30 am #

Thanks for this example in python from scratch. I think the reason your score stays the same is your split attributes. This leads to similar trees and thus a small variance of the ensemble set. If you chain the trees, you will see an increase in performance of the ensemble. One solution is to alter this code s

Build a decision tree
def build_tree(train, max_depth, min_size):
root = get_split(train)
split(root, max_depth, min_size, 1)
return root

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Jason Brownlee January 18, 2017 at 10:17 am #



Thanks for the tip!





Jovan Sardinha June 25, 2017 at 9:41 am #

thanks for the great tutorial!

I have re-written this script using sklearn for easy implementation: https://gist.github.com/JovanSardinha/2c58bd1e7e3aa4c02affedfe7abe8a29



Jason Brownlee June 26, 2017 at 6:04 am #

Nice work!



Alex Godfrey August 31, 2017 at 6:43 am #

Hi Jason,

Minor tip – In the string to integer conversion – I found that the unique set gets created in somev scripts that use this function. To avoid this I have changed the line to read-

unique = sorted(set(class_values))

This results in creating the same lookup dictionary every time. I ran across this when I was using the lookup dictionary every time. I ran across this when I was using the lookup dictionary every time. I ran across this when I was using the lookup dictionary every time. I ran across this when I was using the lookup dictionary every time. I ran across this when I was using the lookup dictionary every time. I ran across this when I was using the lookup dictionary every time. I ran across this when I was using the lookup dictionary every time. I ran across this when I was using the lookup dictionary every time. I ran across this when I was using the lookup dictionary every time. I ran across this when I was using the lookup dictionary every time.

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Jason Brownlee September 1, 2017 at 6:38 am #

Great tip, thanks Alex!

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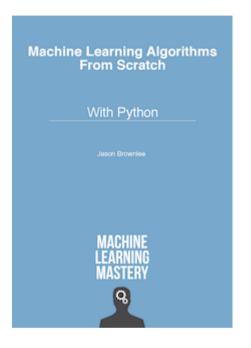
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