

Gentlest Intro to Tensorflow (Part 3)

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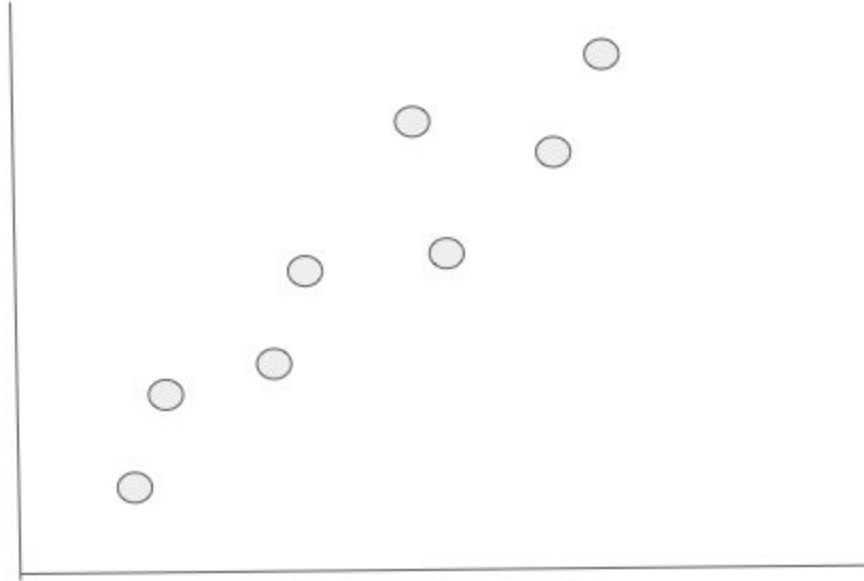
Overview

- Multi-feature Linear Regression
- Logistic Regression
 - Multi-class prediction
 - Cross-entropy
 - Softmax
- Tensorflow Cheatsheet #1

Review: Predict from Single Feature with Linear Regression

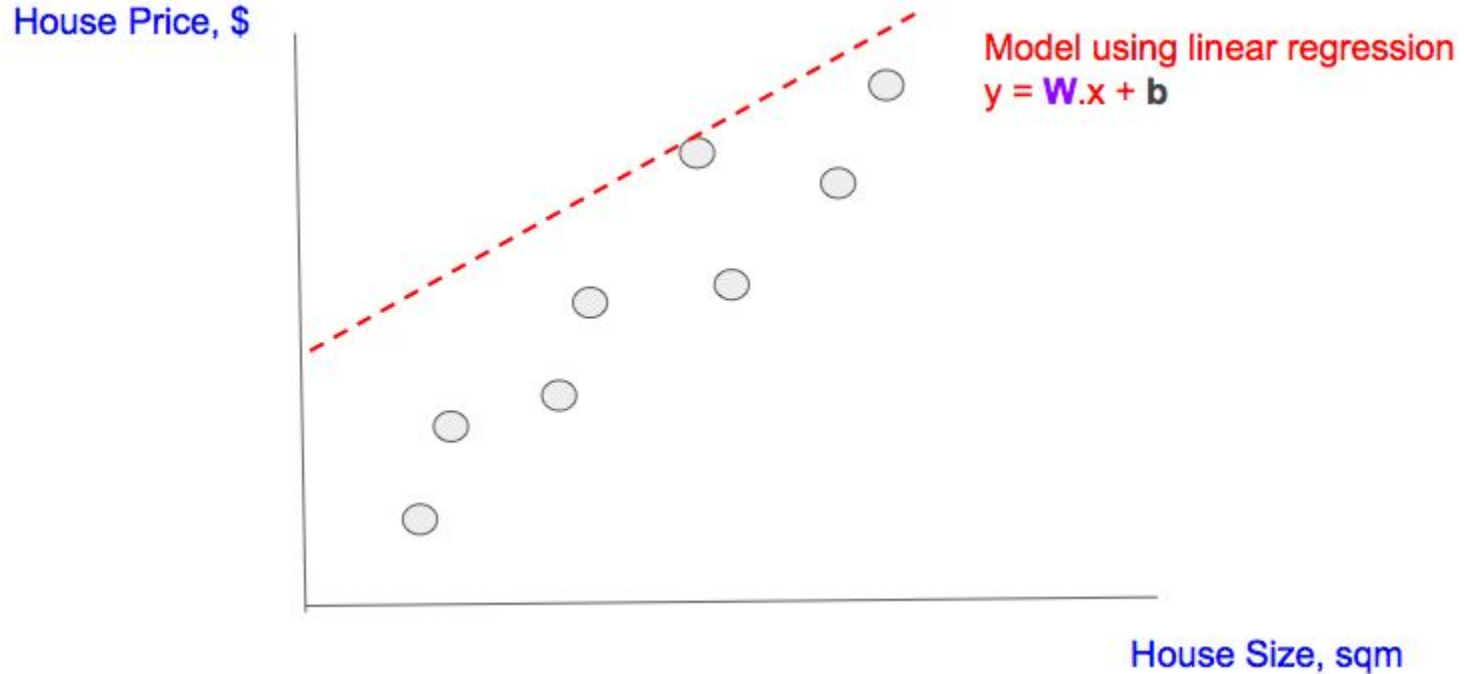
Quick Review: Predict from Single Feature (House Size)

House Price, \$

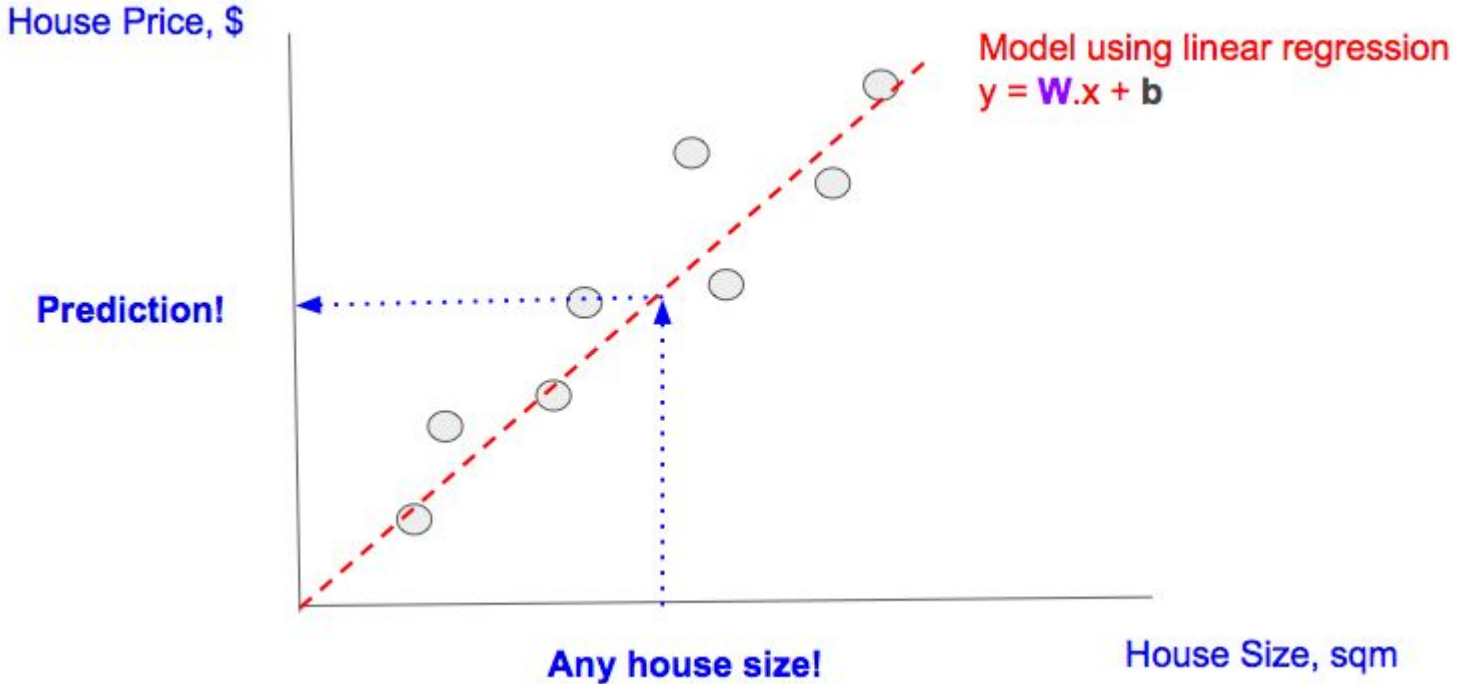


House Size, sqm

Quick Review: Use Linear Regression

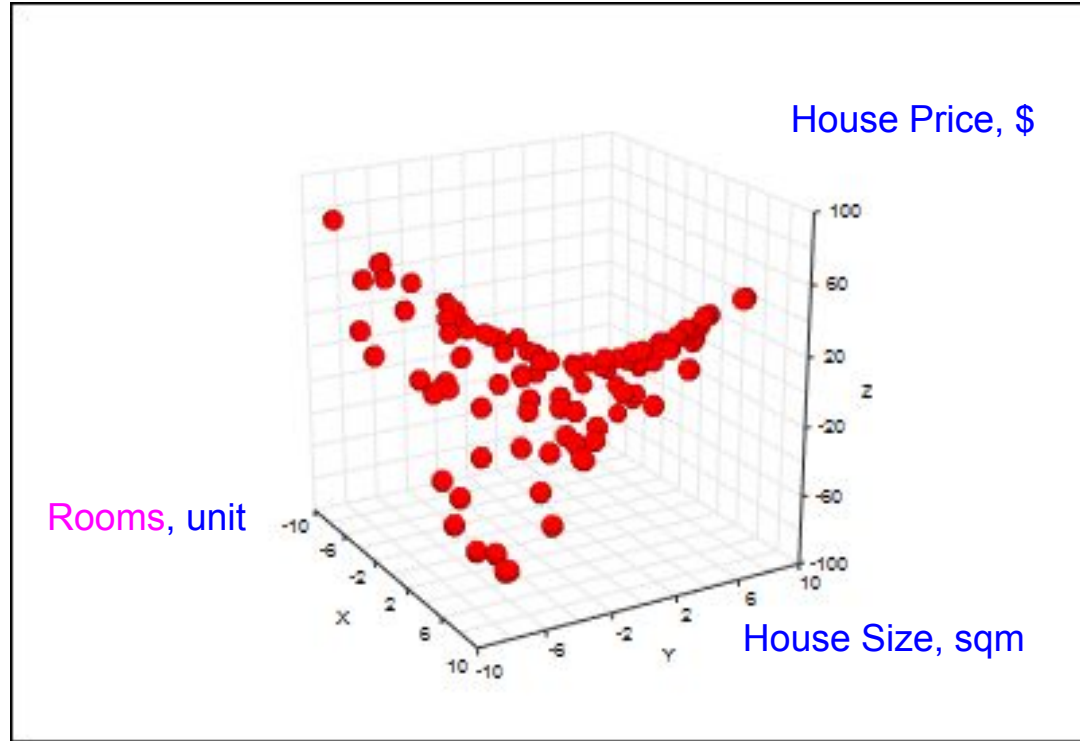


Quick Review: Predict using Linear Regression

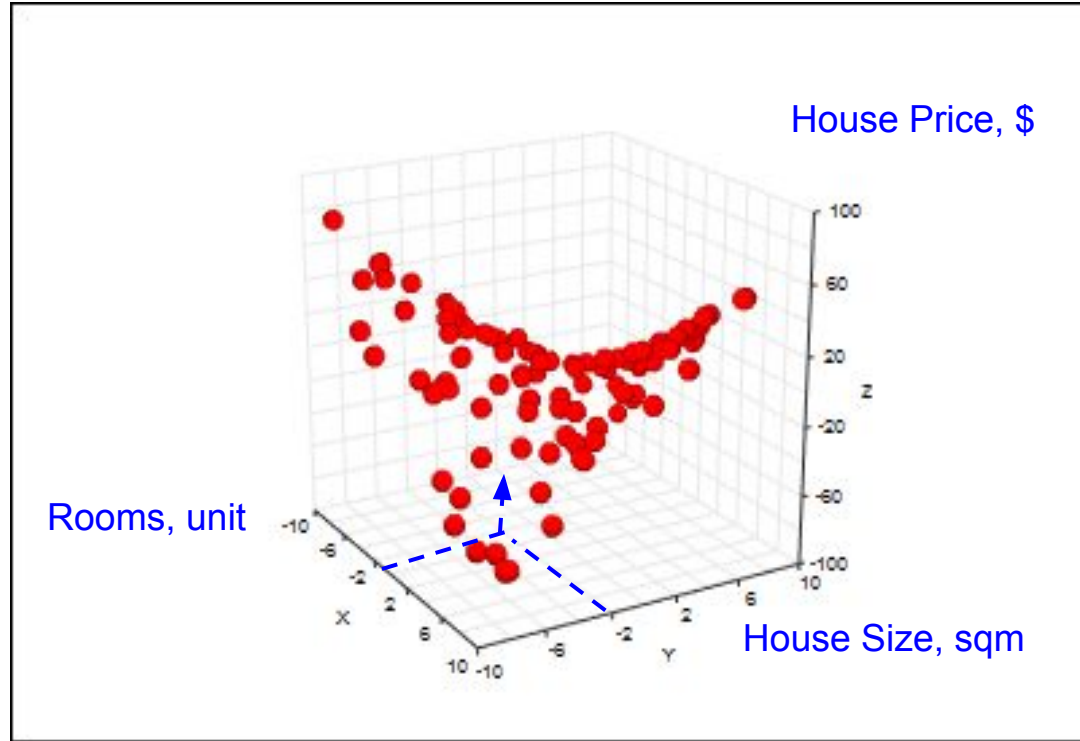


Linear Regression: Predict from Two (or More) Features

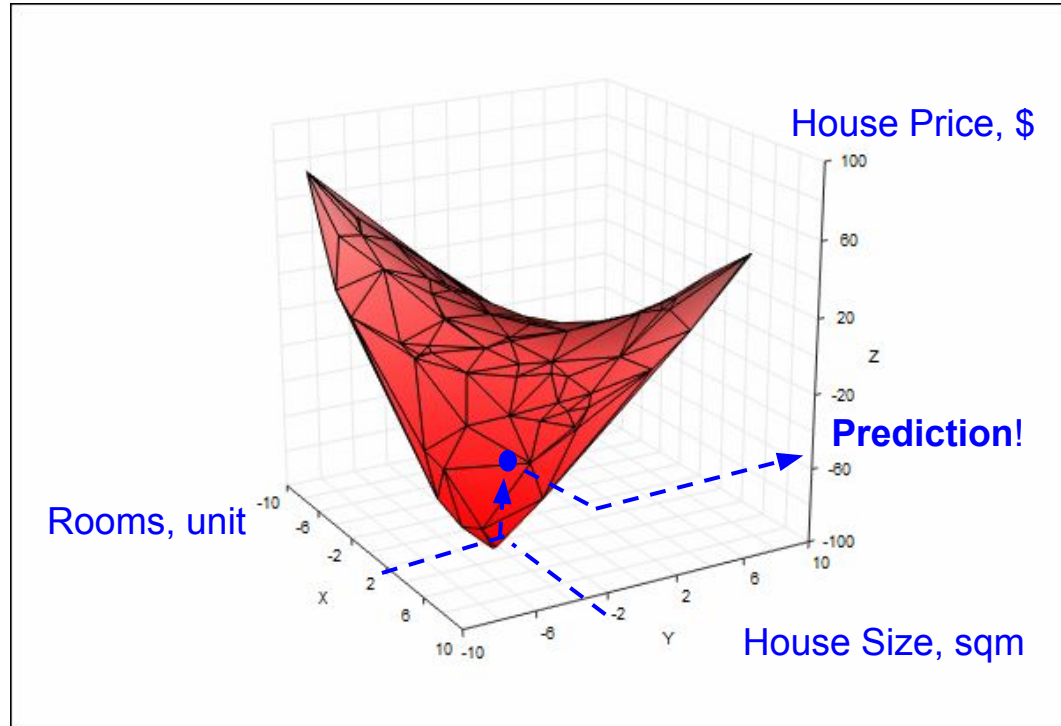
Two Features: House Size, Rooms



Same Issue: Predict for Values without Datapoint



Same Solution: Find Best-Fit



Review: Tensorflow Code

Tensorflow Code

```
# Model linear regression  $y = Wx + b$   
x = tf.placeholder(tf.float32, [None, 1])  
W = tf.Variable(tf.zeros([1,1]))  
b = tf.Variable(tf.zeros([1]))  
product = tf.matmul(x,W)  
y = product + b  
y_ = tf.placeholder(tf.float32, [None, 1])
```

```
# Cost function  $1/n * \sum((y_-y)**2)$   
cost = tf.reduce_mean(tf.square(y_-y))
```

```
# Training using Gradient Descent to minimize cost  
train_step = tf.train.GradientDescentOptimizer(0.0000001).minimize(cost)
```

Multi-feature: Change in Model & Cost Function

Model

1 Feature

$$y = W.x + b$$

y: House price prediction

x: House size

Goal: Find scalars **W,b**

Model

1 Feature

$$y = W.x + b$$

y: House price prediction

x: House size

Goal: Find scalars **W**, **b**

2 Features

$$y = W.x + W2.x2 + b$$

y: House price prediction

x: House size

x2: Rooms

Goal: Find scalars **W**, **W2**, **b**

Tensorflow Graph

1 Feature

```
y = tf.matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```


Tensorflow Graph

1 Feature

```
y = tf.matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

2 Features

```
y = matmul(x, W) + matmul(x2, W2) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
x2 = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

Tensorflow Graph: Train

1 Feature

`y = tf.matmul(x, W) + b`

`W = tf.Variable(tf.zeros[1,1])`

`b = tf.Variable(tf.zeros[1])`

`x = tf.placeholder(tf.float, [None, 1])`
`y_ = tf.placeholder(tf.float, [None, 1])`

Train: feed = { `x`: ..., `y_`: ... }

2 Features

`y = matmul(x, W) + matmul(x2, W2) + b`

`W = tf.Variable(tf.zeros[1,1])`

`W2 = tf.Variable(tf.zeros[1,1])`

`b = tf.Variable(tf.zeros[1])`

`x = tf.placeholder(tf.float, [None, 1])`
`x2 = tf.placeholder(tf.float, [None, 1])`
`y_ = tf.placeholder(tf.float, [None, 1])`

Train: feed = { `x`: ..., `x2`: ..., `y_`: ... }

Tensorflow Graph: Scalability Issue

Model gets messy!

1 Feature

```
y = tf.matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

Train: feed = { x: ..., y_: ... }

2 Features

```
y = tf.matmul(x, W) + tf.matmul(x2,  
W2) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
x2 = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

Train: feed = { x: ..., x2: ..., y_: ... }

3 Features

```
y = tf.matmul(x, W) + tf.matmul(x2,  
W2) + tf.matmul(x3, W3) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
W3 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
x2 = tf.placeholder(tf.float, [None, 1])
```

```
x3 = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

Train: feed = { x: ..., x2: ..., x3: ..., y_: ... }

Data Representation

	Feature values		Actual outcome
House #1	Size_1	Rooms_1	Price_1
House #2	Size_2	Rooms_2	Price_2
...
House #m	Size_m	Rooms_m	Price_m

Lots of Data Manipulation

House #1	Size_1	Rooms_1	Price_1
House #2	Size_2	Rooms_2	Price_2
...
House #m	Size_m	Rooms_m	Price_m

2 Features

```
y = tf.matmul(x, W) + tf.matmul(x2,  
W2) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])  
x2 = tf.placeholder(tf.float, [None, 1])  
y_ = tf.placeholder(tf.float, [None, 1])
```

Train: feed = { x: ..., x2: ..., y_: ... }

Lots of Data Manipulation 2

House #1	Size_1	Rooms_1	Price_1
House #2	Size_2	Rooms_2	Price_2
...
House #m	Size_m	Rooms_m	Price_m

2 Features

```
y = tf.matmul(x, W) + tf.matmul(x2, W2) + b
```

```
W = tf.Variable(tf.zeros([1,1]))
```

```
W2 = tf.Variable(tf.zeros([1,1]))
```

```
b = tf.Variable(tf.zeros([1]))
```

```
x = tf.placeholder(tf.float, [None, 1])  
x2 = tf.placeholder(tf.float, [None, 1])  
y_ = tf.placeholder(tf.float, [None, 1])
```

```
Train: feed = { x: ..., x2: ..., y_: ... }
```

Lots of Data Manipulation 3

House #1	Size_1	Rooms_1	Price_1
House #2	Size_2	Rooms_2	Price_2
...
House #m	Size_m	Rooms_m	Price_m

2 Features

```
y = tf.matmul(x, W) + tf.matmul(x2, W2) + b
```

```
W = tf.Variable(tf.zeros([1,1]))
```

```
W2 = tf.Variable(tf.zeros([1,1]))
```

```
b = tf.Variable(tf.zeros([1]))
```

```
x = tf.placeholder(tf.float, [None, 1])  
x2 = tf.placeholder(tf.float, [None, 1])  
y_ = tf.placeholder(tf.float, [None, 1])
```

```
Train: feed = { x: ..., x2: ..., y_: ... }
```

Lots of Data Manipulation 4

House #1
House #2
...
House #m

Size_1
Size_2
...
Size_m

Rooms_1
Rooms_2
...
Rooms_m

Price_1
Price_2
...
Price_m

Data manipulation
gets messy!

2 Features

```
y = tf.matmul(x, W) + tf.matmul(x2, W2) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])  
x2 = tf.placeholder(tf.float, [None, 1])  
y_ = tf.placeholder(tf.float, [None, 1])
```

Train: feed = { x: ..., x2: ..., y_: ... }

Lots of Data Manipulation 4

House #1
House #2
...
House #m

Size_1
Size_2
...
Size_m

Rooms_1
Rooms_2
...
Rooms_m

Price_1
Price_2
...
Price_m

2 Features

Find better way

$$y = W.x + W2.x2 + b$$

```
y = tf.matmul(x, W) + tf.matmul(x2,  
W2) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])  
x2 = tf.placeholder(tf.float, [None, 1])  
y_ = tf.placeholder(tf.float, [None, 1])
```

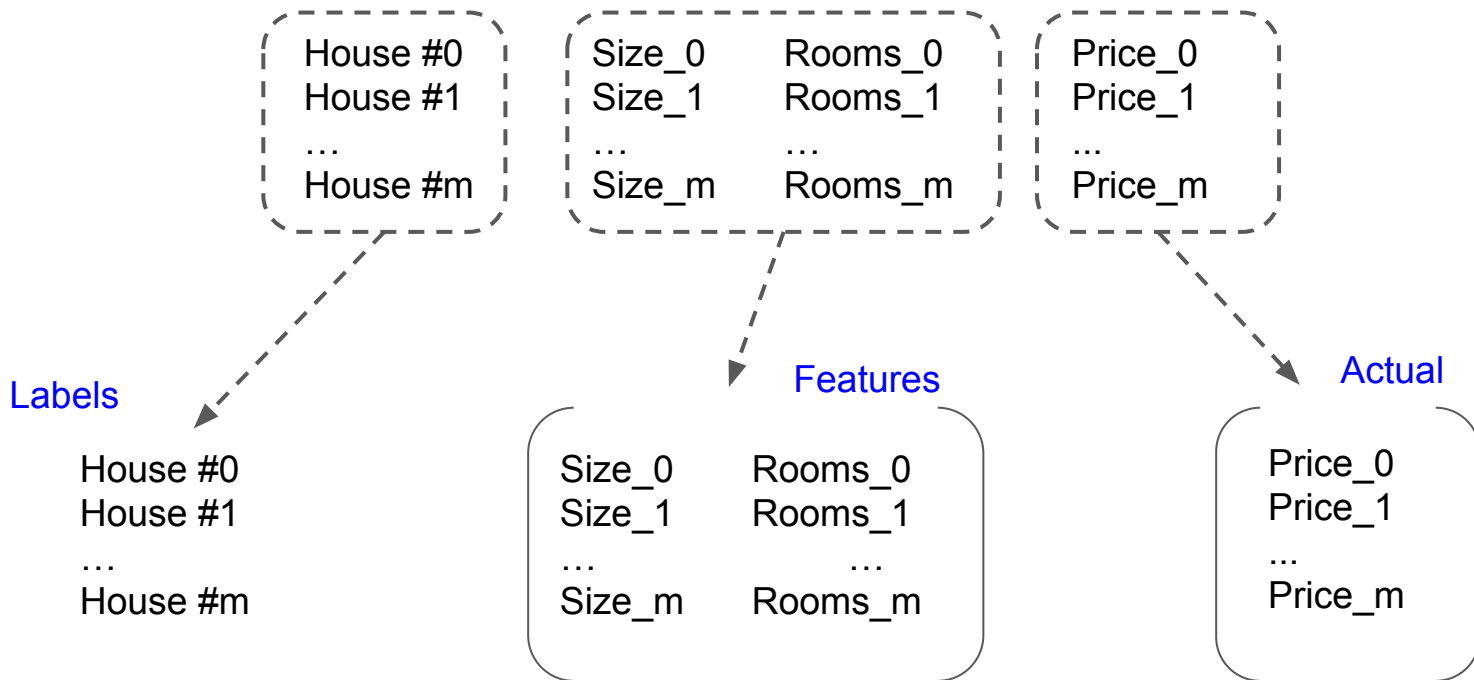
Train: feed = { x: ..., x2: ..., y_: ... }

Matrix: Cleaning Up Representations

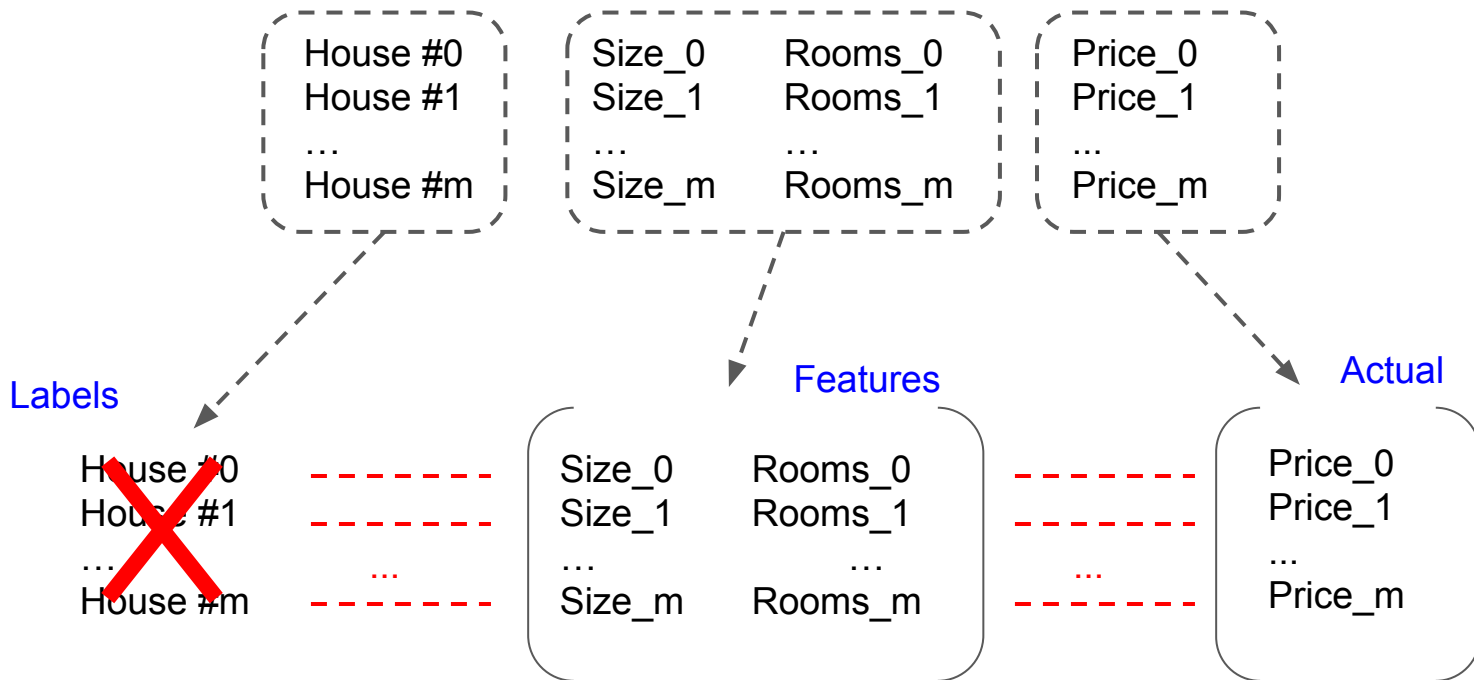
Matrix Representation

House #0	Size_0	Rooms_0	Price_0
House #1	Size_1	Rooms_1	Price_1
...
House #m	Size_m	Rooms_m	Price_m

Matrix Representation

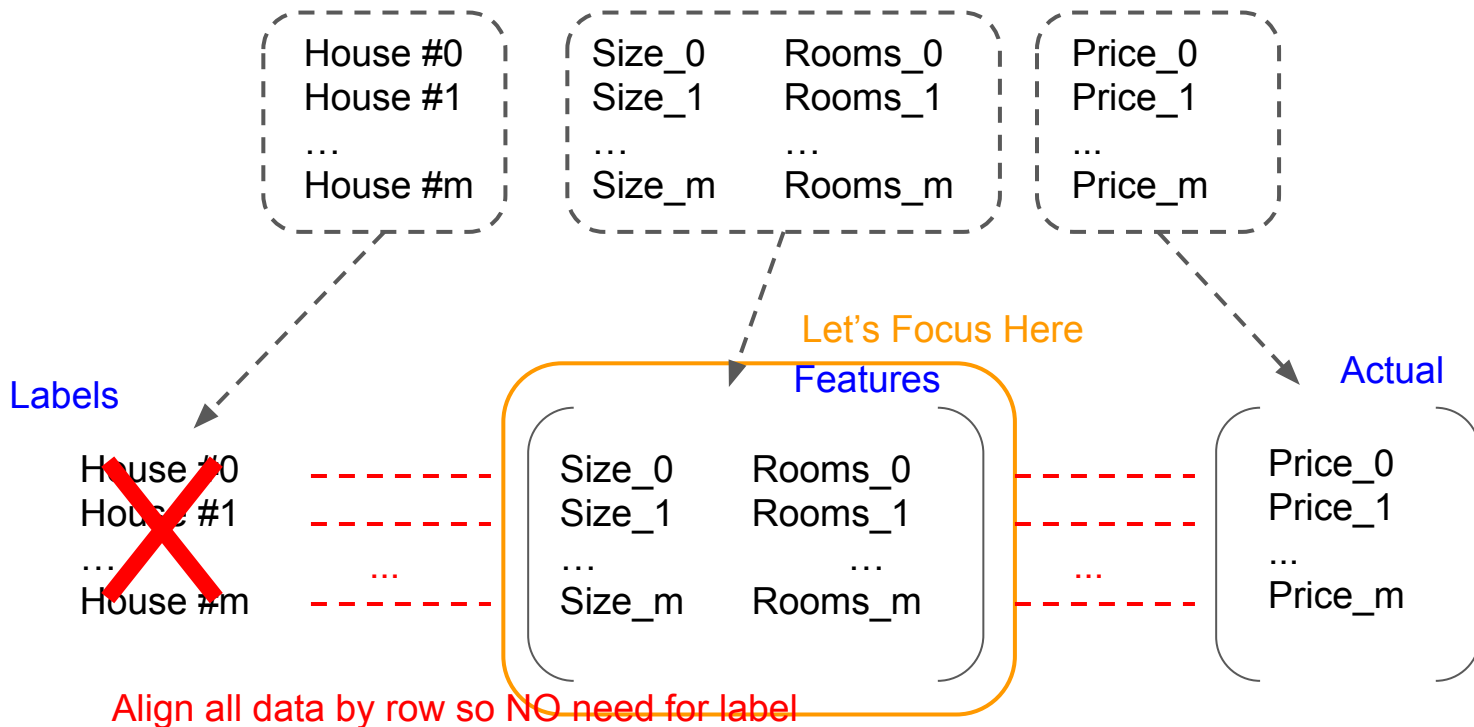


Matrix Representation



Align all data by row so NO need for label

Matrix Representation



Matrix: Cleaning Up Models

Better Model Equation

House #1
House #2
...
House #m

Size_1
Size_2
...
Size_m

Rooms_1
Rooms_2
...
Rooms_m

Price_1
Price_2
...
Price_m

2 Features

Find better way

$$y = W.x + W2.x2 + b$$

```
y = tf.matmul(x, W) + tf.matmul(x2, W2) + b
```

```
W = tf.Variable(tf.zeros([1,1]))
```

```
W2 = tf.Variable(tf.zeros([1,1]))
```

```
b = tf.Variable(tf.zeros([1]))
```

```
x = tf.placeholder(tf.float, [None, 1])  
x2 = tf.placeholder(tf.float, [None, 1])  
y_ = tf.placeholder(tf.float, [None, 1])
```

```
Train: feed = { x: ..., x2: ..., y_: ...  
}
```


Better Model Equation

House #1
House #2
...
House #m

Size_1
Size_2
...
Size_m

Rooms_1
Rooms_2
...
Rooms_m

Price_1
Price_2
...
Price_m

2 Features

$y = \text{tf.matmul}(x, W) + \text{tf.matmul}(x2, W2) + b$

$W = \text{tf.Variable}(\text{tf.zeros}[1,1])$

$W2 = \text{tf.Variable}(\text{tf.zeros}[1,1])$

$b = \text{tf.Variable}(\text{tf.zeros}[1])$

$x = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 1])$

$x2 = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 1])$

$y_ = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 1])$

Train: feed = { x: ..., x2: ..., y_: ... }

Find better way

$$y = W.x + W2.x2 + b$$

Better Model Equation

House #1
House #2
...
House #m

Size_1
Size_2
...
Size_m

Rooms_1
Rooms_2
...
Rooms_m

Price_1
Price_2
...
Price_m

Find better way

$$y = W.x + W2.x2 + b$$

2 Features

```
y = tf.matmul(x, W) + tf.matmul(x2, W2) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
x2 = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

Train: feed = { x: [size_i, rooms_i], ..., ~~x2~~: ..., y_: ... }

Better Model Equation

House #1
House #2
...
House #m

Size_1
Size_2
...
Size_m

Rooms_1
Rooms_2
...
Rooms_m

Price_1
Price_2
...
Price_m

Find better way

$$y = W.x + W2.x2 + b$$

2 Features

```
y = tf.matmul(x, W) + tf.matmul(x2, W2) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 2])
```

```
x2 = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

```
Train: feed = { x: [size_i, rooms_i], ..., x2: ..., y_: ... }
```

Better Model Equation

House #1
House #2
...
House #m

Size_1
Size_2
...
Size_m

Rooms_1
Rooms_2
...
Rooms_m

Price_1
Price_2
...
Price_m

Find better way

$$y = W.x + W2.x2 + b$$

2 Features

```
y = tf.matmul(x, W) + tf.matmul(x2, W2) + b
```

```
W = tf.Variable(tf.zeros[2,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 2])
```

```
x2 = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

```
Train: feed = { x: [size_i, rooms_i], ..., x2: ..., y_: ... }
```

Better Model Equation

House #1
House #2
...
House #m

Size_1
Size_2
...
Size_m

Rooms_1
Rooms_2
...
Rooms_m

Price_1
Price_2
...
Price_m

Find better way

$$y = W.x + W2.x2 + b$$

2 Features

```
y = tf.matmul(x, W) + tf.matmul(x2,  
W2) + b
```

```
W = tf.Variable(tf.zeros[2,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 2])
```

```
x2 = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

```
Train: feed = { x: [size_i, rooms_i], ..., x2: ..., y_: ...  
}
```

Better Model Equation

House #1
House #2
...
House #m

Size_1
Size_2
...
Size_m

Rooms_1
Rooms_2
...
Rooms_m

Price_1
Price_2
...
Price_m

2 Features

```
y = tf.matmul(x, W) + tf.matmul(x2,  
W2) + b
```

```
W = tf.Variable(tf.zeros[2,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 2])
```

```
x2 = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

```
Train: feed = { x: [size_i, rooms_i], ..., x2: ..., y_: ...  
}
```

Find better way

$$y = W.x + \cancel{W2.x2} + b$$

Tensorflow Graph (Messy)

1 Feature

```
y = tf.matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

2 Features

```
y = matmul(x, W) + matmul(x2, W2) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
x2 = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

Tensorflow Graph (Clean)

1 Feature

```
y = tf.matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

2 Features

```
y = matmul(x, W) + matmul(x2, W2) + b
```

```
W = tf.Variable(tf.zeros[2,1])
```

```
W2 = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 2])
```

```
x2 = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```


Tensorflow Graph (Clean and Formatted)

1 Feature

```
y = tf.matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

2 Features

```
y = matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[2,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 2])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

Tensorflow Graph (Illustration)

1 Feature

```
y = tf.matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

scalar { .. 1 feature .. } $\left\{ \begin{array}{c} \text{.. 1 coeff ..} \end{array} \right\}$ scalar

2 Features

```
y = matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[2,1])
```

```
b = tf.Variable(tf.zeros[1])
```

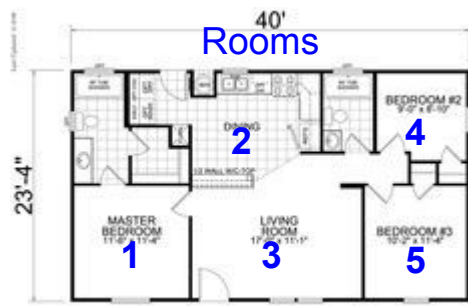
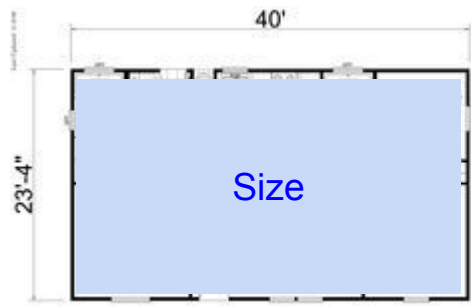
```
x = tf.placeholder(tf.float, [None, 2])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

scalar { .. 2 features .. } $\left\{ \begin{array}{c} \text{.. 2 coeffs ..} \end{array} \right\}$ scalar

Logistic Regression

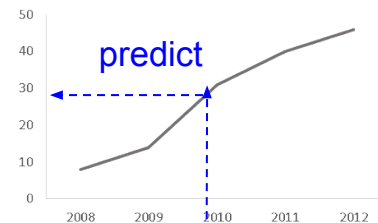
Linear vs. Logistic Regression



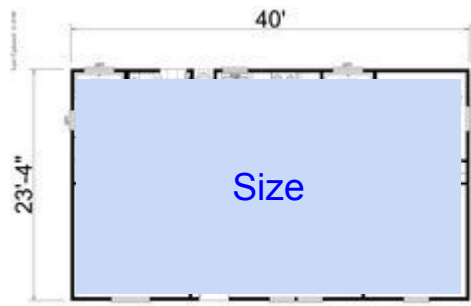
ML

Linear Regression

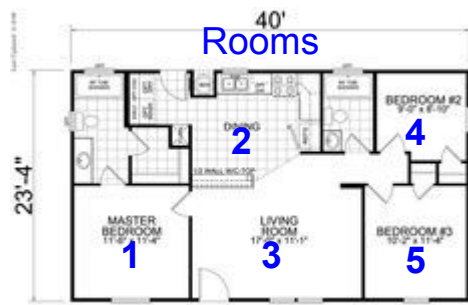
price (scalar)



Linear vs. Logistic Regression

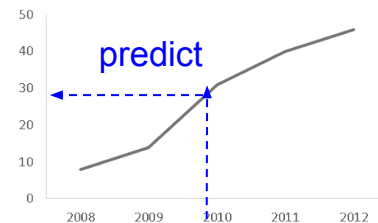


+

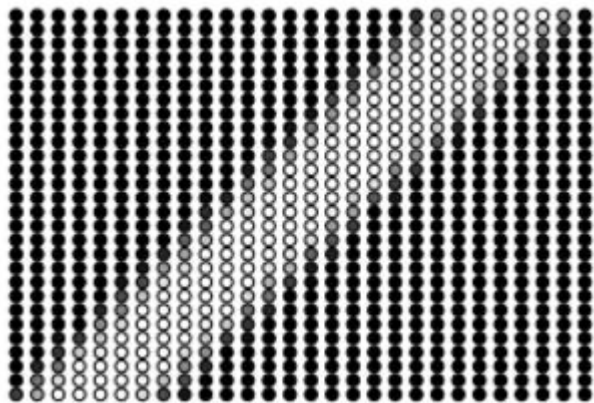


Linear Regression

price (scalar)



Image



Logistic Regression

number (discrete classes)

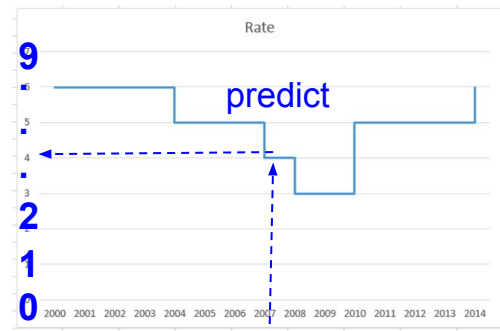


Image Features

Image Features 1

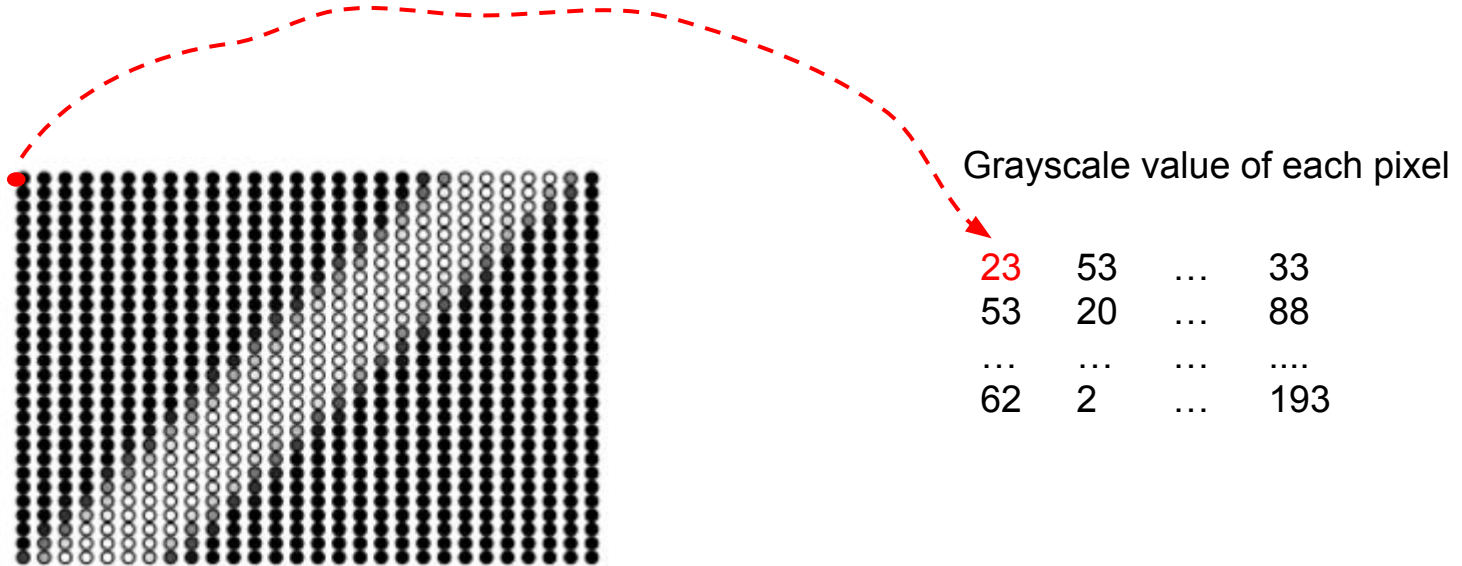


Image Features 2

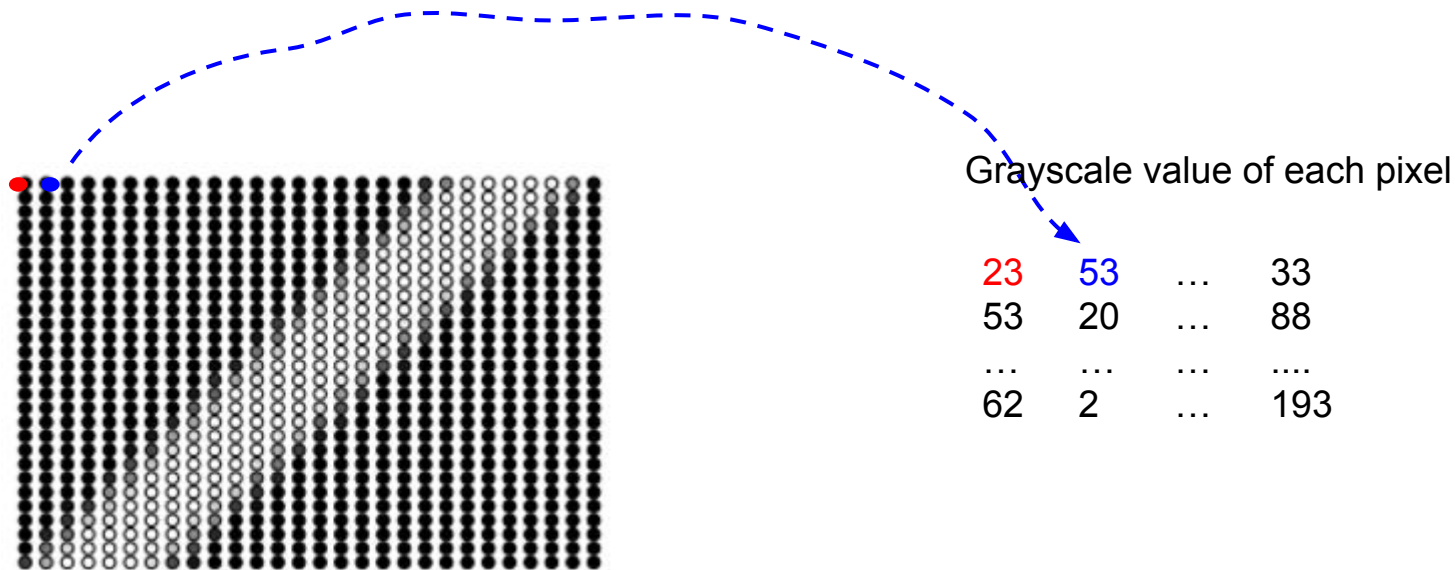
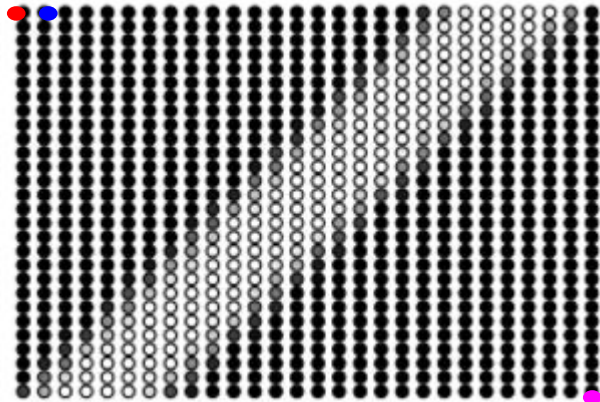
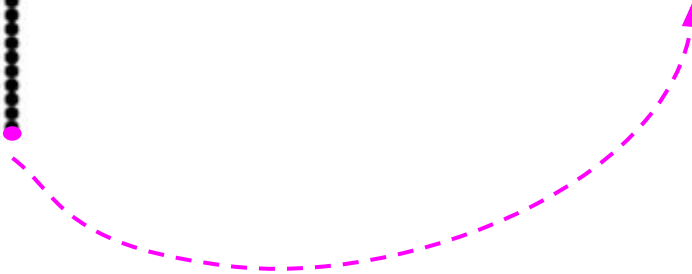


Image Features 3



Grayscale value of each pixel

23	53	...	33
53	20	...	88
...
62	2	...	193



Logistic Regression: Change in Models

Model

Linear Regression

$$y = W.x + b$$

y: House price (scalar) prediction

x: [House size, Rooms]

Goal: Find scalars **W, b**

Logistic Regression

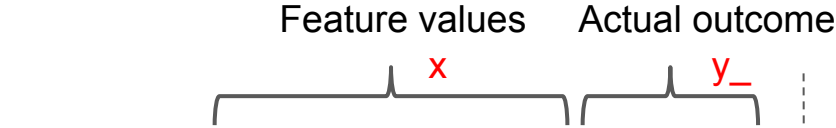
$$y = W.x + b$$

y: Discrete class [0,1,...9] prediction

x: [2-Dim pixel grayscale colors]

Goal: Find scalars **W, b**

Data Representation Comparison



House #1	Size_1	Rooms_1	Price_1
House #2	Size_2	Rooms_2	Price_2
...
House #m	Size_m	Rooms_m	Price_m



Image #1	23	53	...	33	5
	53	20	...	88	
	
	62	2	...	193	
Image #2	250	10	...	33	2
	103	5	...	88	
	
	5	114	...	193	
Image #m	...				3

Data Representation Comparison

	Feature values x		Actual outcome y_{-}
	2 Features 1-Dim		
House #1	Size_1	Rooms_1	Price_1
House #2	Size_2	Rooms_2	Price_2
...
House #m	Size_m	Rooms_m	Price_m

	Feature values x				Actual outcome y_{-}
	X x Y 2-Dim Features				
Image #1	23	53	...	33	5
	53	20	...	88	
	
	62	2	...	193	
Image #2	250	10	...	33	2
	103	5	...	88	
	
	5	114	...	193	
Image #m	...				3

Data Representation Comparison

	Feature values x		Actual outcome y_{-}
	2 Features 1-Dim		
House #1	Size_1	Rooms_1	Price_1
House #2	Size_2	Rooms_2	Price_2
...
House #m	Size_m	Rooms_m	Price_m

	Feature values x				Actual outcome y_{-}
	X x Y 2-Dim Features				
Image #1	23	53	...	33	5
	53	20	...	88	
	
	62	2	...	193	
Image #2	250	10	...	33	2
	103	5	...	88	
	
	5	114	...	193	
Image #m	...				3

Data Representation Comparison

Feature values			Actual outcome
x			y_{-}
2 Features 1-Dim			
House #1	Size_1	Rooms_1	Price_1
House #2	Size_2	Rooms_2	Price_2
...
House #m	Size_m	Rooms_m	Price_m

Feature values			Actual outcome
x			y_{-}
Generalize into a multi-feature problem			
Image #1	X.Y	1-Dim Features	
	23 53 ... 33 53 20 ... 88 ... 62 2 ... 193		5
Image #2	250 10 ... 33 103 5 ... 88 ... 5 114 ... 193		2
Image #m	...		3

Model

Linear Regression

$$y = W.x + b$$

y: House price (scalar) prediction

x: [House size, Rooms]

Goal: Find scalars **W, b**

Logistic Regression

$$y = W.x + b$$

y: Discrete class [0,1,...9] prediction

~~x: [2-Dim pixel grayscale colors]~~

x: [Pixel 1, Pixel 2, ..., Pixel X.Y]

Goal: Find scalars **W, b**

Model

Linear Regression

$$y = W.x + b$$

This needs change as well!

y: House price (scalar) prediction

x: [House size, Rooms]

Goal: Find scalars **W, b**

Logistic Regression

$$y = W.x + b$$

y: Discrete class [0,1,...9] prediction

~~x: [2-Dim pixel grayscale colors]~~

x: [Pixel 1, Pixel 2, ..., Pixel X.Y]

Goal: Find scalars **W, b**

Why Can't 'y' be left as scalar of 0-9?

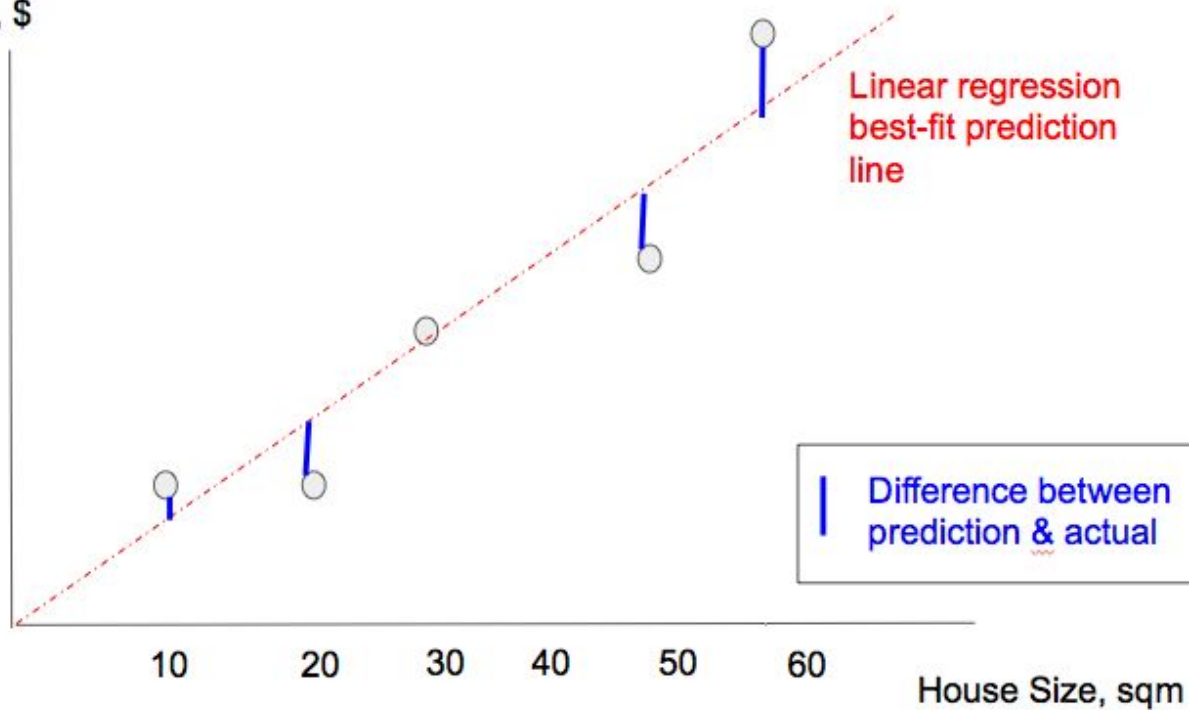
HINT: Beside the model, when doing ML we need this function!

Logistic Regression: Change in Cost Function

Linear Regression: Cost

Scalar

House Price, \$



Linear Regression: Cost, **NOT**

Discrete

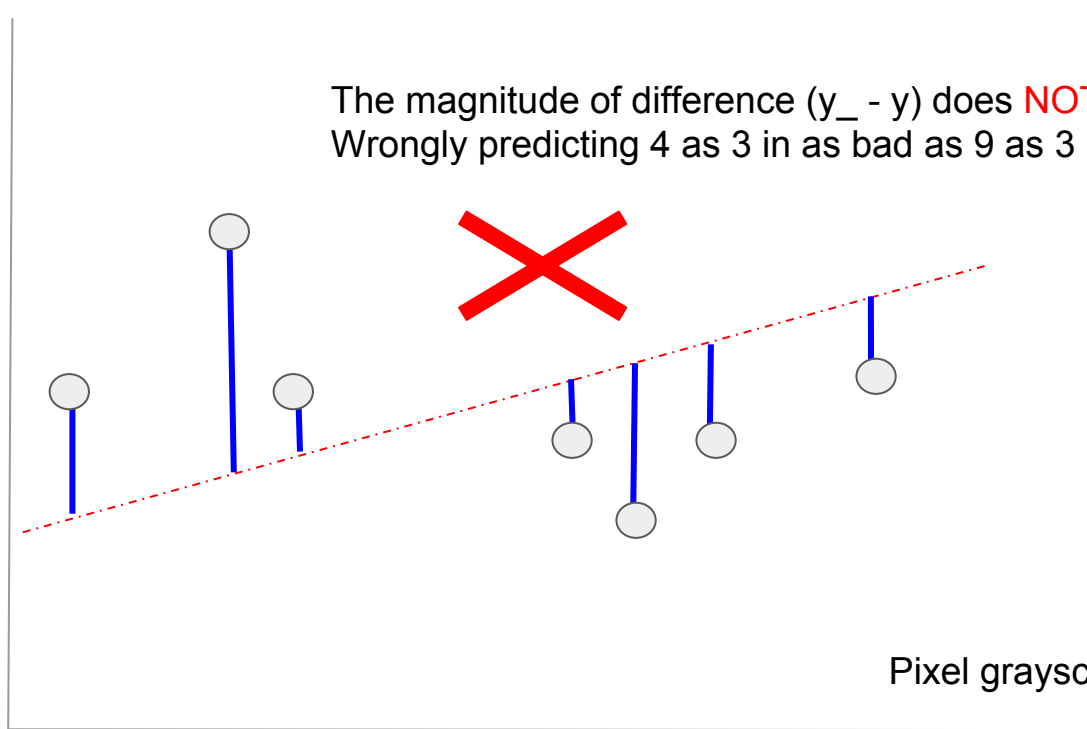
Number

9
8
7
6
5
4
3
2
1
0

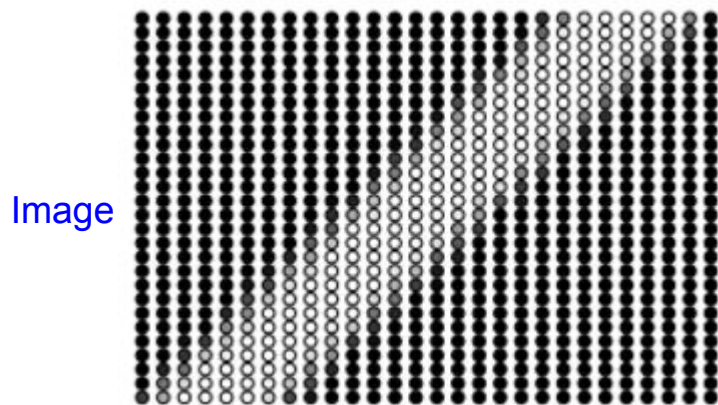
The magnitude of difference ($y_{\text{pred}} - y$) does **NOT** matter
Wrongly predicting 4 as 3 is as bad as 9 as 3



Pixel grayscale values

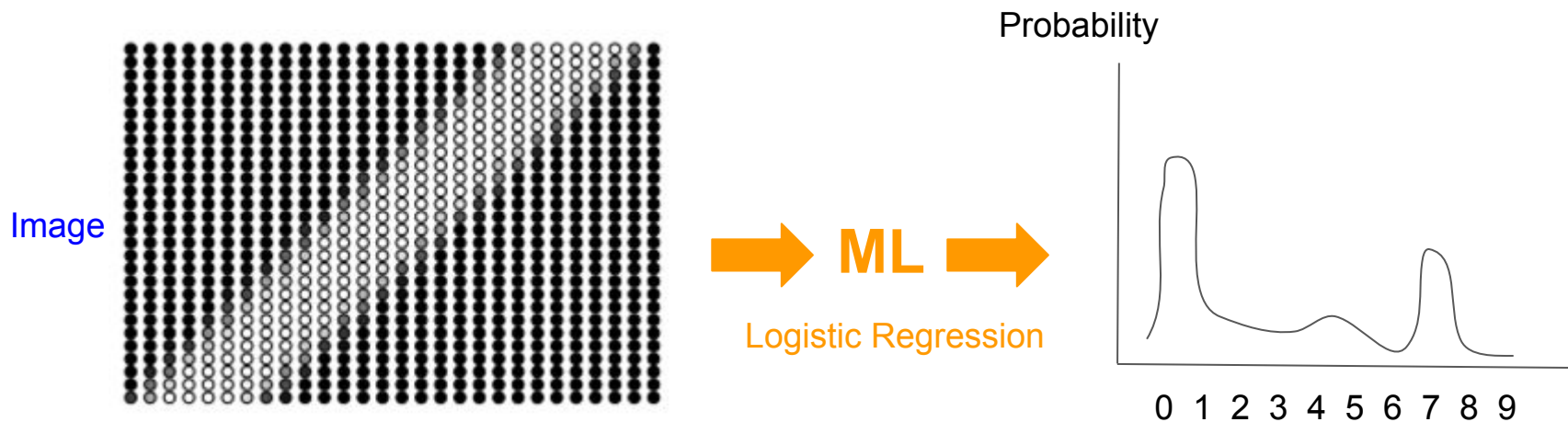


Logistic Regression: Prediction

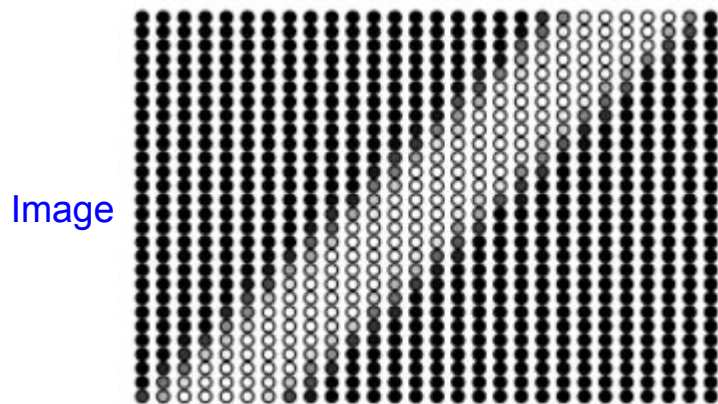


1

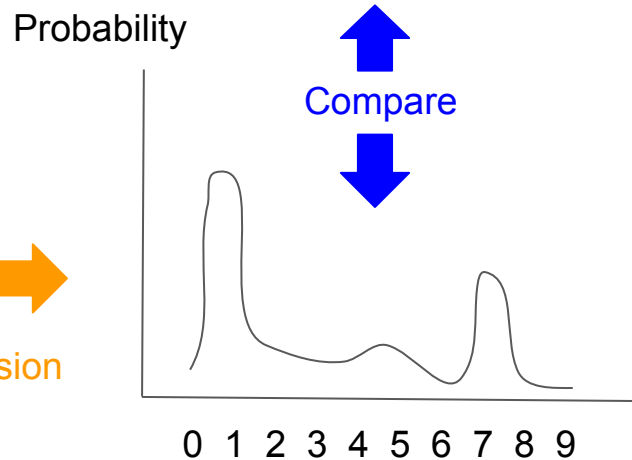
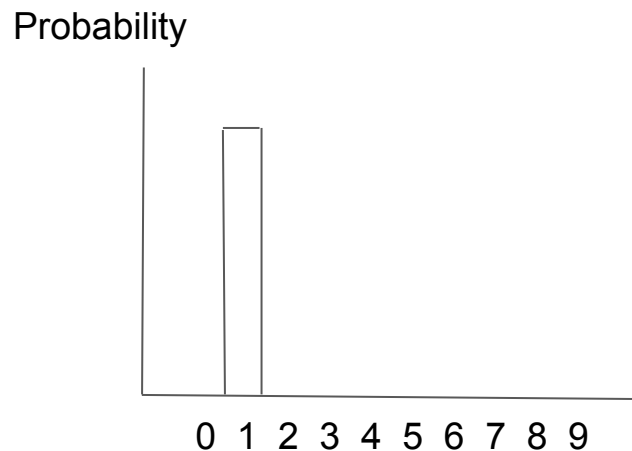
Logistic Regression: Prediction



Logistic Regression: Prediction



Actual



Compare

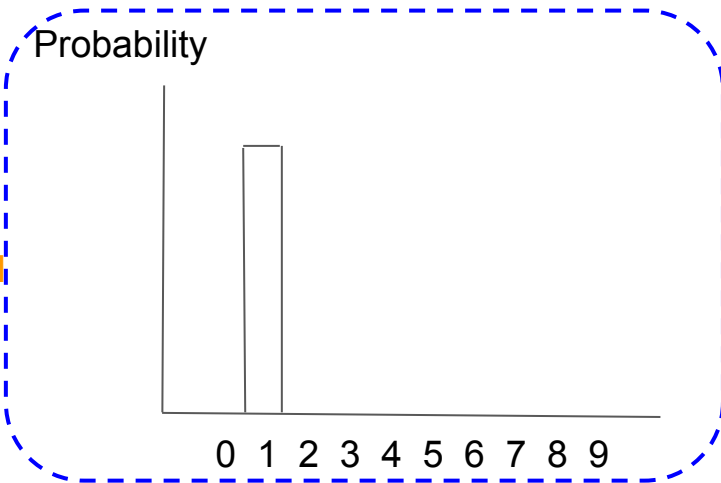
Cross-Entropy: Cost Function 1

$$H_{y'}(y) = - \sum_i y'_i \log(y_i)$$

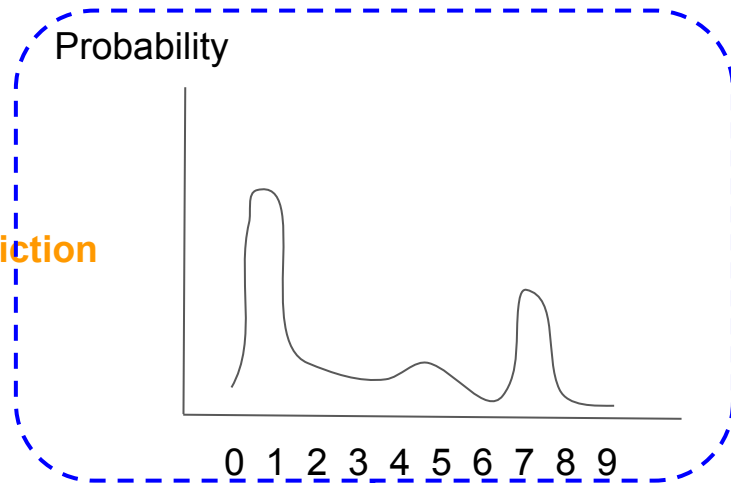
```
cross_entropy = -tf.reduce_sum(y_*tf.log(y))
```

Cross-Entropy: Cost Function 2

Actual



Prediction

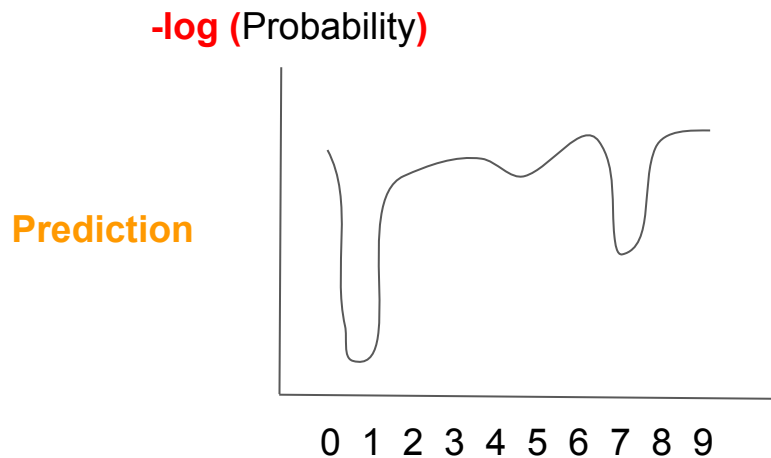
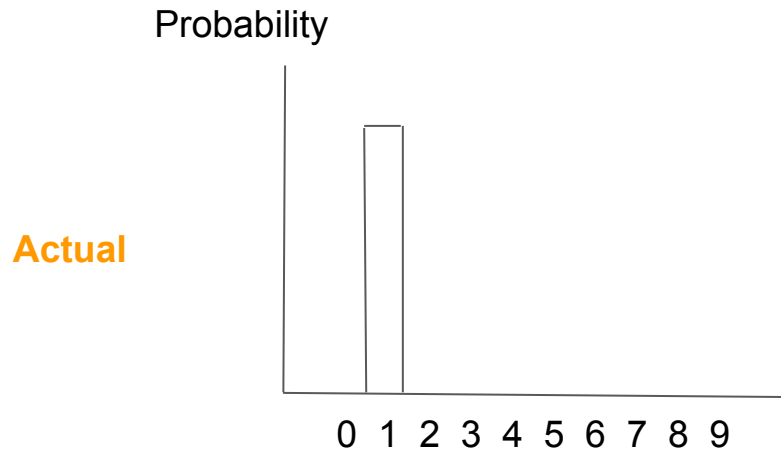


$$H_{y'}(y) = - \sum_i y'_i \log(y_i)$$

`cross_entropy = -tf.reduce_sum(y_*tf.log(y))`

Cross-Entropy: Cost Function 3

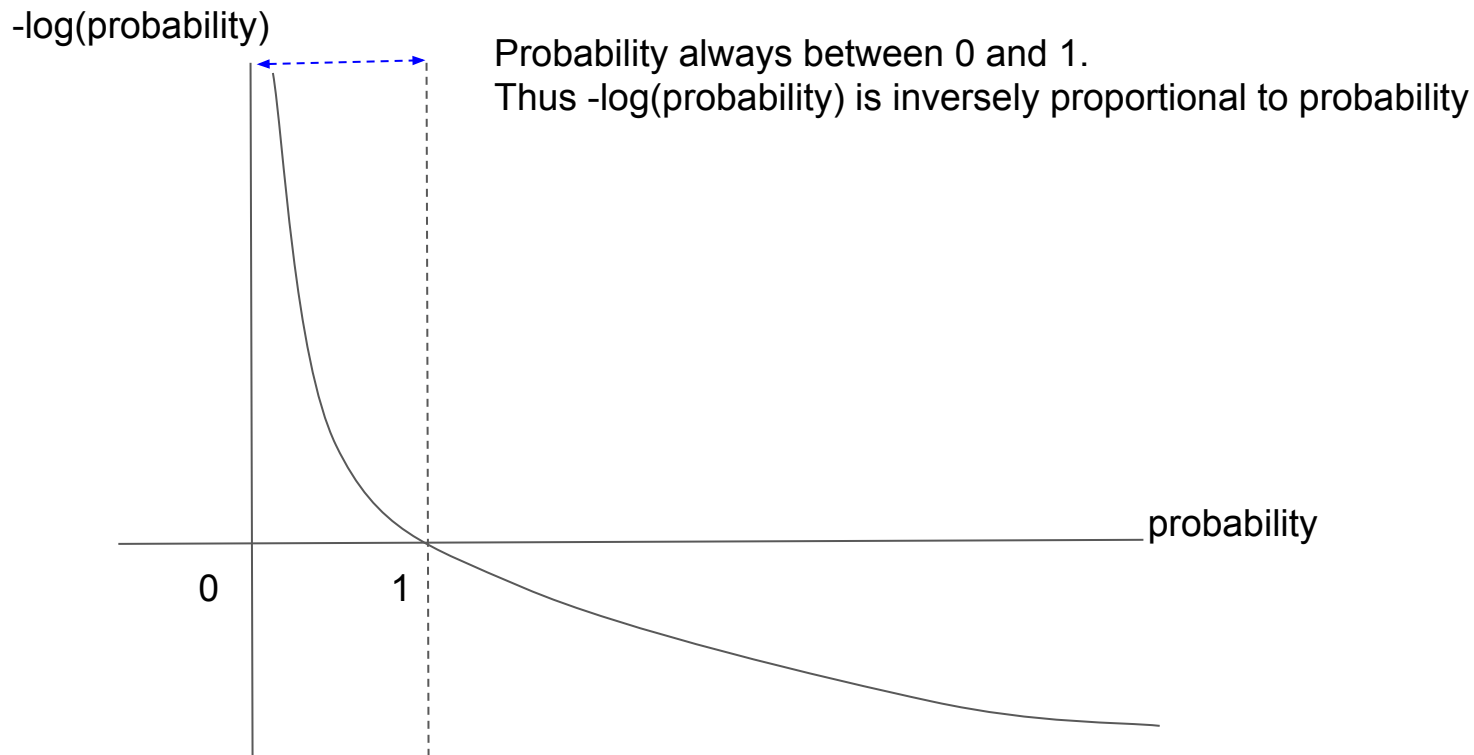
Almost inverse because Probability < 1



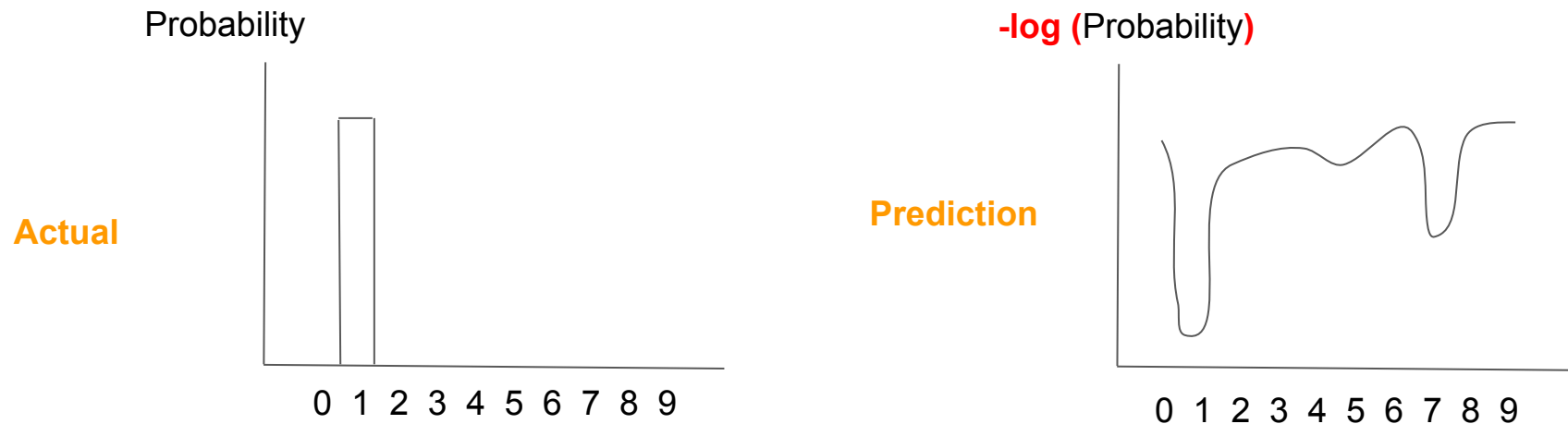
$$H_{y'}(y) = - \sum_i y'_i \log(y_i)$$

```
cross_entropy = -tf.reduce_sum(y_*tf.log(y))
```

Graph: $-\log(\text{probability})$



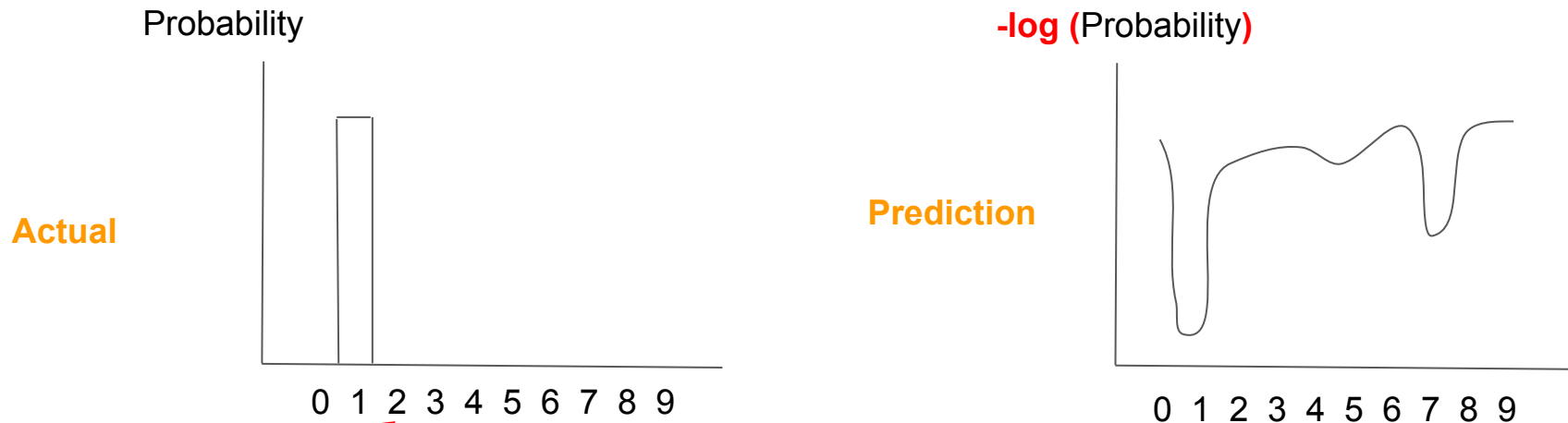
Cross-Entropy: Cost Function x x xx



$$H_{y'}(y) = - \sum_i y'_i \log(y_i)$$

`cross_entropy = -tf.reduce_sum(y_*tf.log(y))`

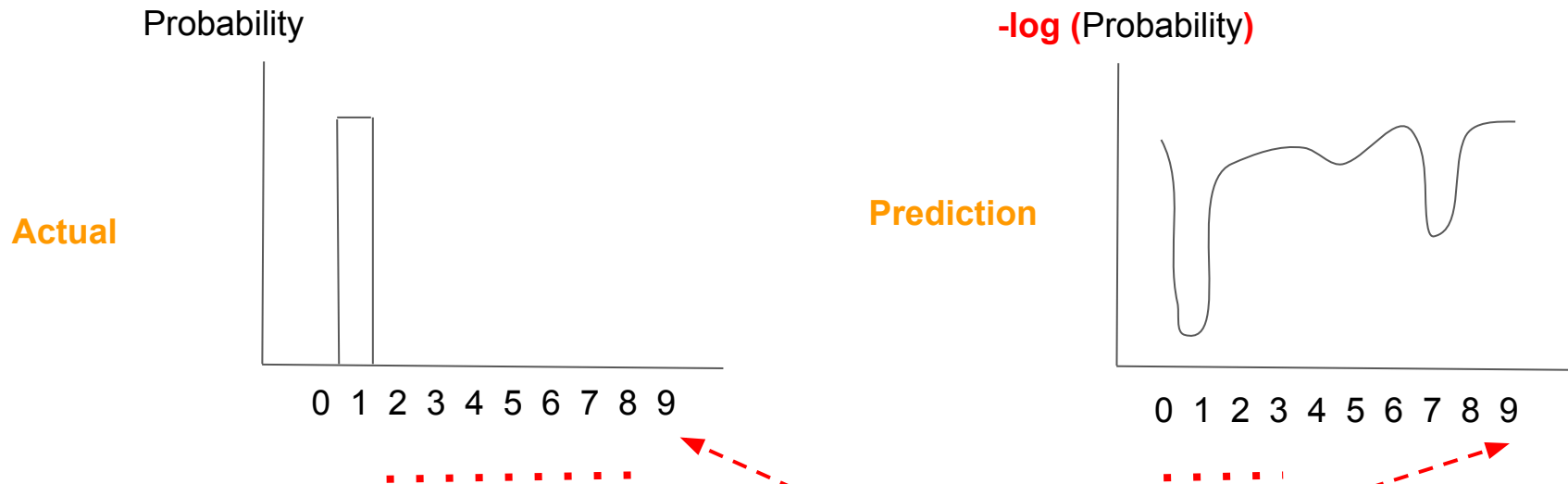
Cross-Entropy: Cost Function



$$H_{y'}(y) = - \sum_i y'_i \log(y_i)$$

`cross_entropy = -tf.reduce_sum(y_*tf.log(y))`

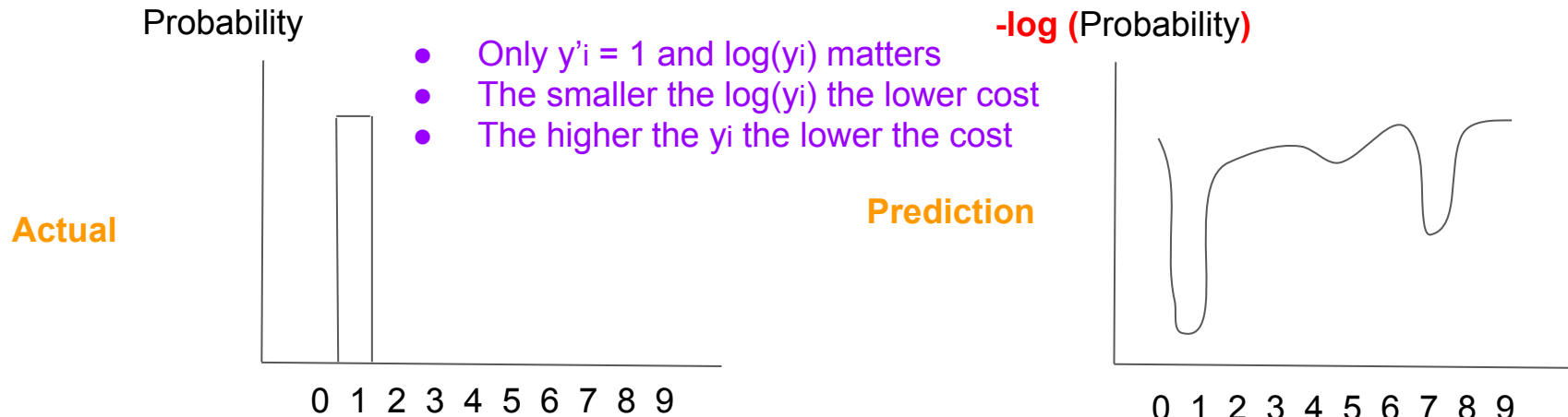
Cross-Entropy: Cost Function



$$H_{y'}(y) = - \sum_i y'_i \log(y_i)$$

`cross_entropy = -tf.reduce_sum(y_*tf.log(y))`

Cross-Entropy: Cost Function

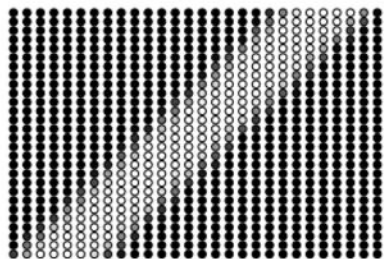


$$H_{y'}(y) = - \sum_i y'_i \log(y_i)$$

`cross_entropy = -tf.reduce_sum(y_*tf.log(y))`

Logistic Regression: Prediction

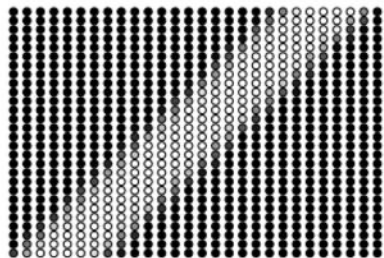
Image



Linear Regression

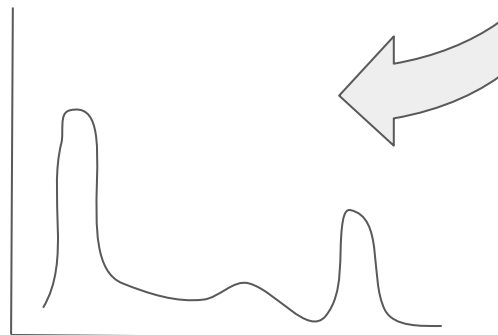
1

Image

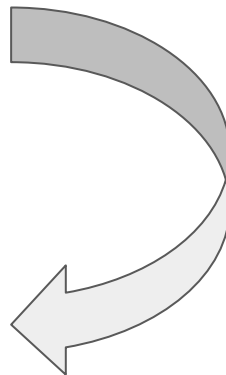


Logistic Regression

Probability



0 1 2 3 4 5 6 7 8 9



Tensorflow Graph (Review)

1 Feature

$y = \text{tf.matmul}(x, W) + b$

$W = \text{tf.Variable}(\text{tf.zeros}[1,1])$

$b = \text{tf.Variable}(\text{tf.zeros}[1])$

$x = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 1])$

$y_ = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 1])$

2 Features

$y = \text{matmul}(x, W) + b$

$W = \text{tf.Variable}(\text{tf.zeros}[2,1])$

$b = \text{tf.Variable}(\text{tf.zeros}[1])$

$x = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 2])$

$y_ = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 1])$

Tensorflow Graph (Review 2)

1 Feature

```
y = tf.matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

scalar $\left\{ \begin{array}{c} \text{.. 1 feature ..} \end{array} \right\} \left\{ \begin{array}{c} \text{.. 1 coeff ..} \end{array} \right\}$ scalar

2 Features

```
y = matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[2,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 2])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```

scalar $\left\{ \begin{array}{c} \text{.. 2 features ..} \end{array} \right\} \left\{ \begin{array}{c} \text{.. 2 coeffs ..} \end{array} \right\}$ scalar

Tensorflow Graph (Review 2)

1 Feature

$y = \text{tf.matmul}(x, W) + b$

$W = \text{tf.Variable}(\text{tf.zeros}[1,1])$

$b = \text{tf.Variable}(\text{tf.zeros}[1])$

$x = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 1])$

$y_ = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 1])$

scalar $\{ \dots 1 \text{ feature} \dots \} \left\{ \begin{matrix} \dots 1 \text{ coeff} \dots \end{matrix} \right\}$ scalar

2 Features

$y = \text{matmul}(x, W) + b$

$W = \text{tf.Variable}(\text{tf.zeros}[2,1])$

$b = \text{tf.Variable}(\text{tf.zeros}[1])$

$x = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 2])$

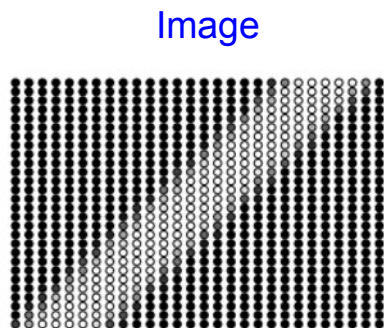
$y_ = \text{tf.placeholder}(\text{tf.float}, [\text{None}, 1])$

Apply multi-feature linear regression

scalar $\{ \dots 2 \text{ features} \dots \} \left\{ \begin{matrix} \dots 2 \text{ coeffs} \dots \end{matrix} \right\}$ scalar

Logistic Regression: Prediction

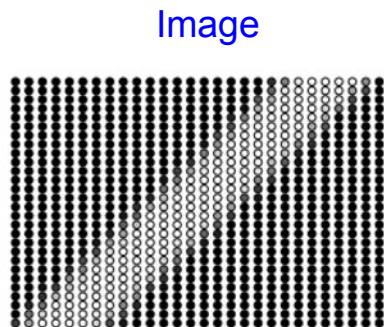
$$y = \text{tf.matmul}(x, W) + b$$



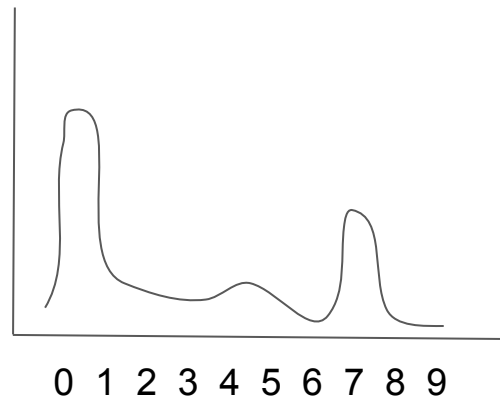
1

scalar

$$\left\{ \begin{array}{c} \text{.. n features ..} \end{array} \right\} \left\{ \begin{array}{c} \text{.. n coeffs ..} \end{array} \right\} \text{scalar}$$

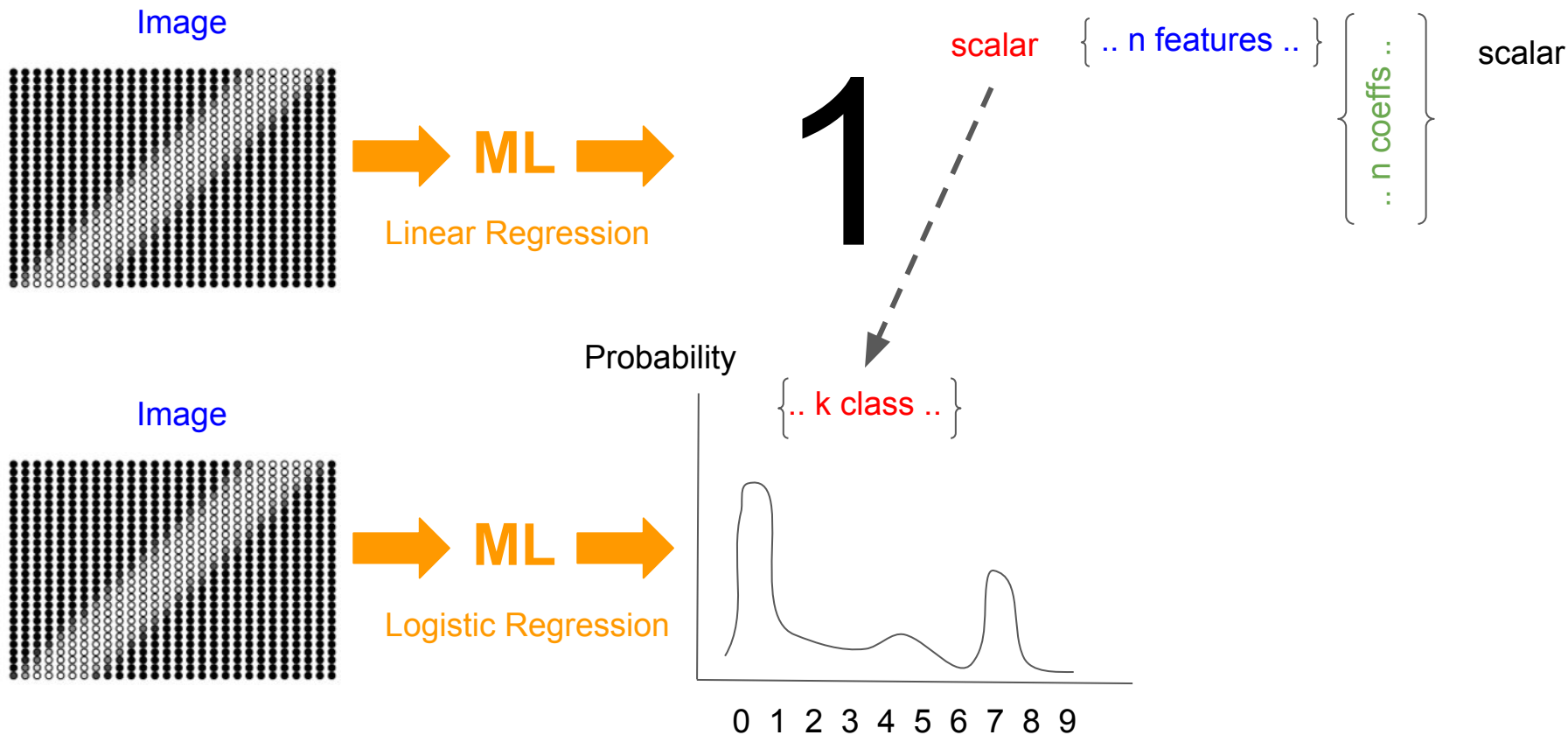


Probability

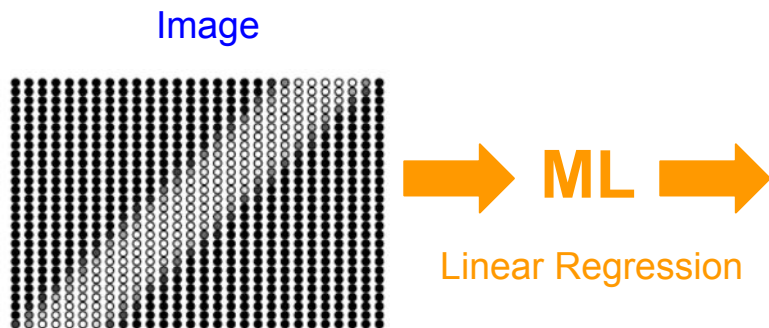


Logistic Regression: Prediction

$$y = \text{tf.matmul}(x, W) + b$$



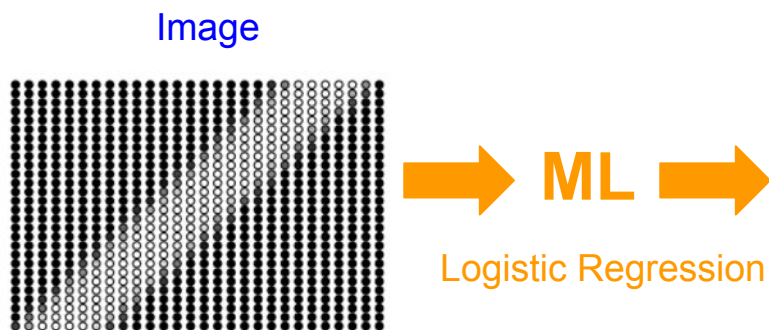
Logistic Regression: Prediction



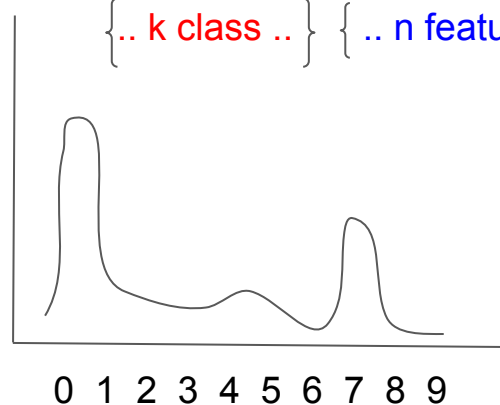
1

$$\text{scalar } y = \text{tf.matmul}(\underbrace{\{ \dots n \text{ features } \dots \}}_{\text{.. n features ..}}, \underbrace{\{ \dots n \text{ coeffs } \dots \}}_{\text{.. n coeffs ..}}) + b$$

scalar



Probability



$$\text{y} = \text{tf.matmul}(\underbrace{\{ \dots k \text{ class } \dots \}}_{\text{.. k class ..}}, \underbrace{\{ \dots n \text{ features } \dots \}}_{\text{.. n features ..}}) + b$$

.. n coeffs ..

.. k class ..

.. k class ..

Tensorflow Graph: Basic, Multi-feature, Multi-class

1 Feature

```
y = tf.matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[1,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 1])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```



2 Features

```
y = matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[2,1])
```

```
b = tf.Variable(tf.zeros[1])
```

```
x = tf.placeholder(tf.float, [None, 2])
```

```
y_ = tf.placeholder(tf.float, [None, 1])
```



2 Features, 10 Classes

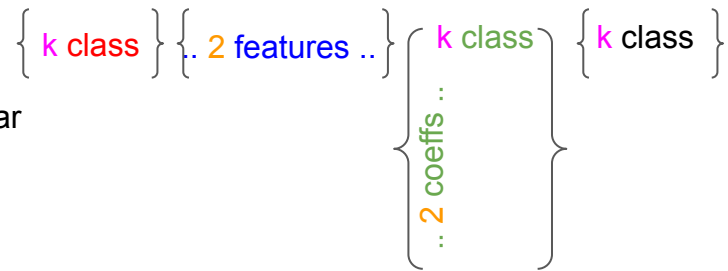
```
y = matmul(x, W) + b
```

```
W = tf.Variable(tf.zeros[2,10])
```

```
b = tf.Variable(tf.zeros[10])
```

```
x = tf.placeholder(tf.float, [None, 2])
```

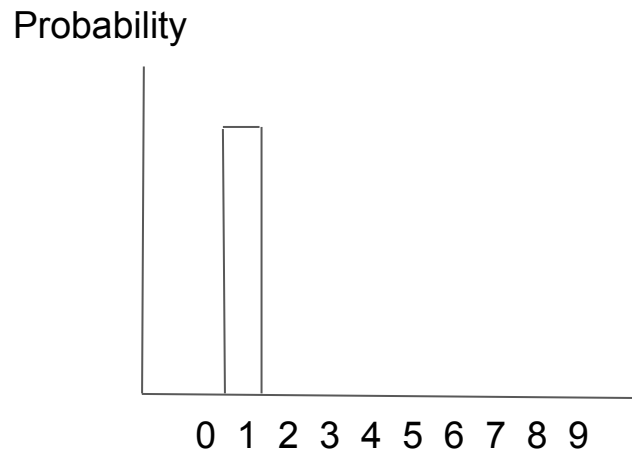
```
y_ = tf.placeholder(tf.float, [None, 10])
```



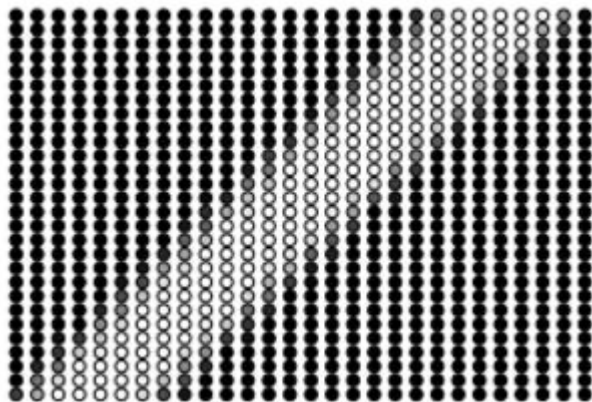
Logistic Regression: Prediction

Great but....sum of all prediction 'probability' NOT 1

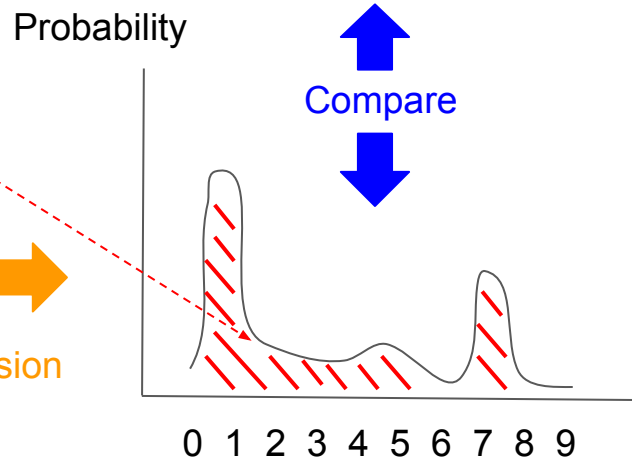
Actual



Image



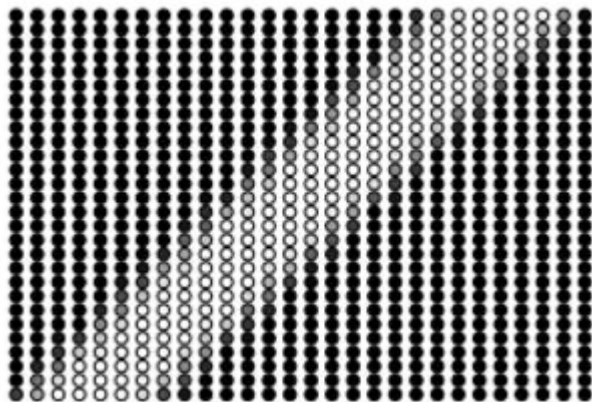
ML
Logistic Regression



Compare

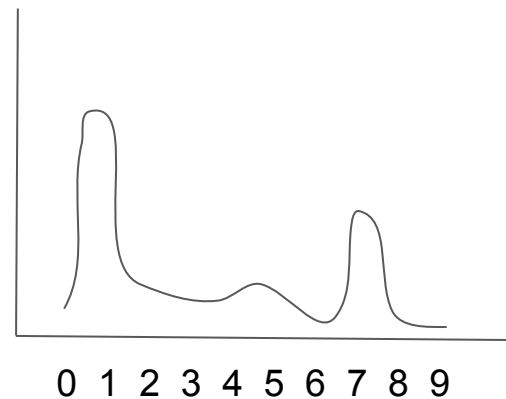
$$\text{softmax}(x)_i = \frac{\exp(x_i)}{\sum_j \exp(x_j)}$$

Image



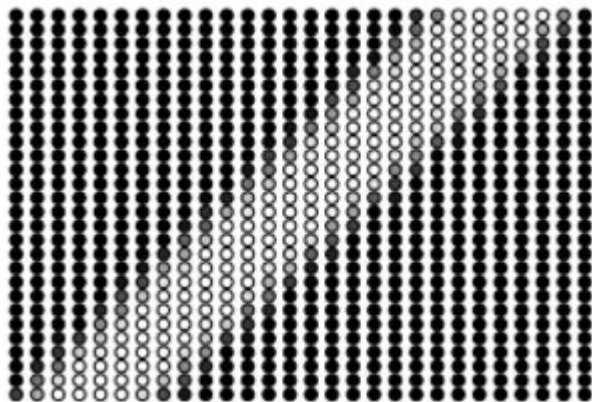
Logistic Regression

Value

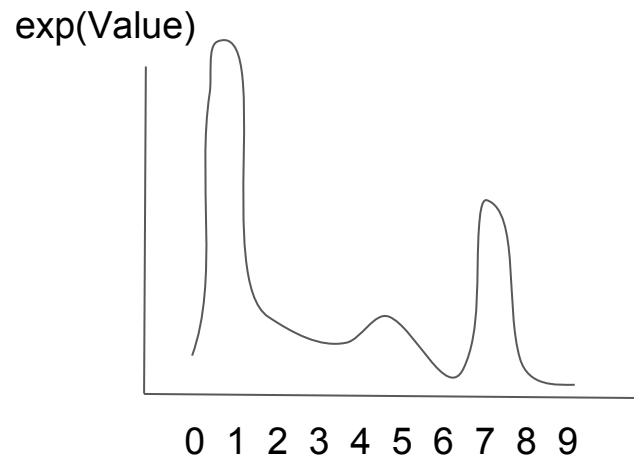


$$\text{softmax}(x)_i = \frac{\exp(x_i)}{\sum_j \exp(x_j)}$$

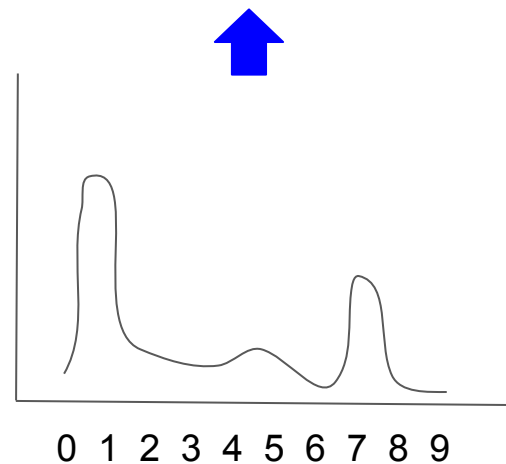
Image



ML
Logistic Regression

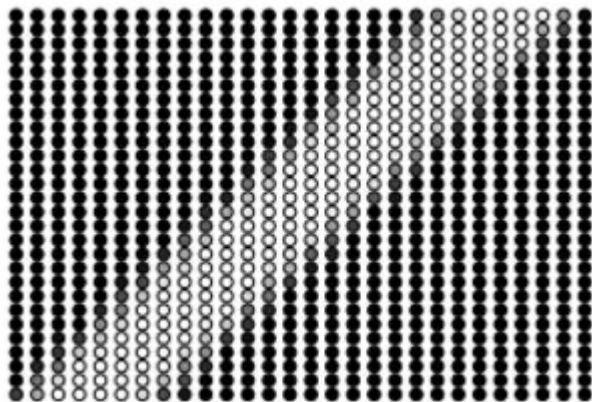


Value

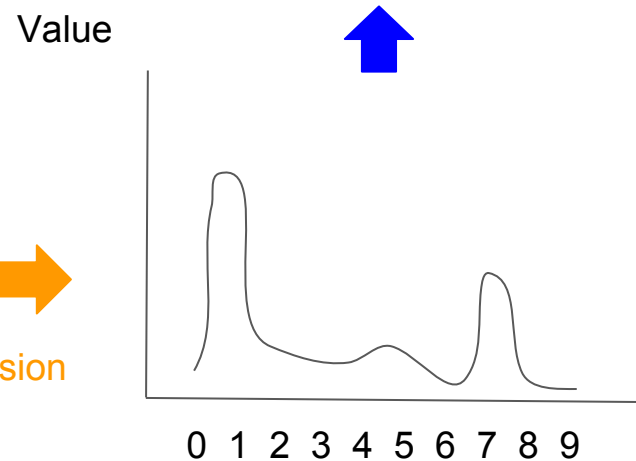
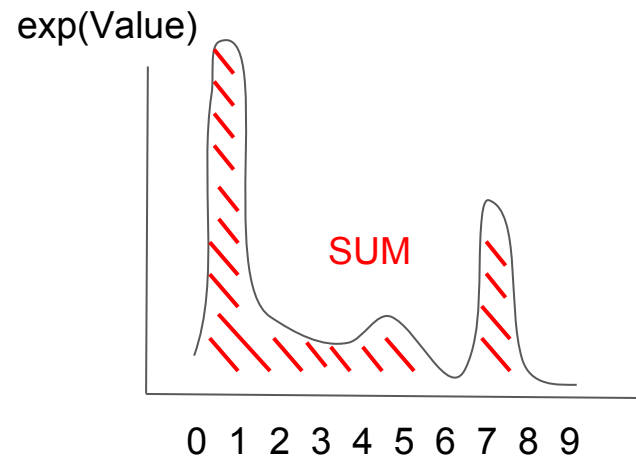


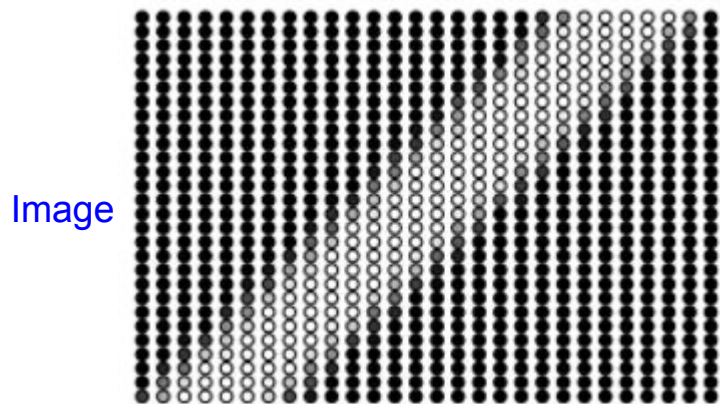
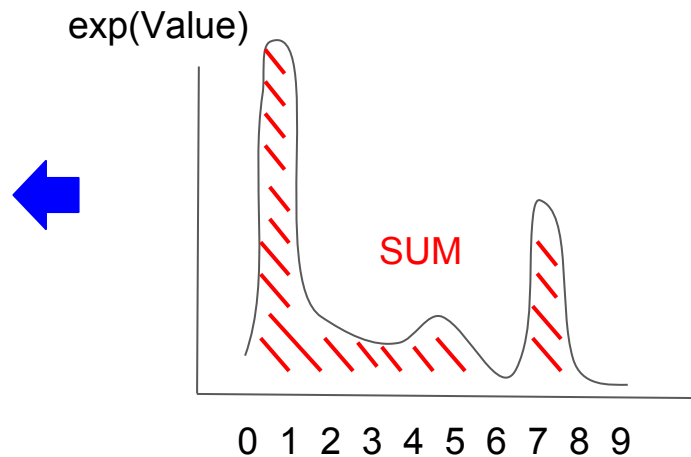
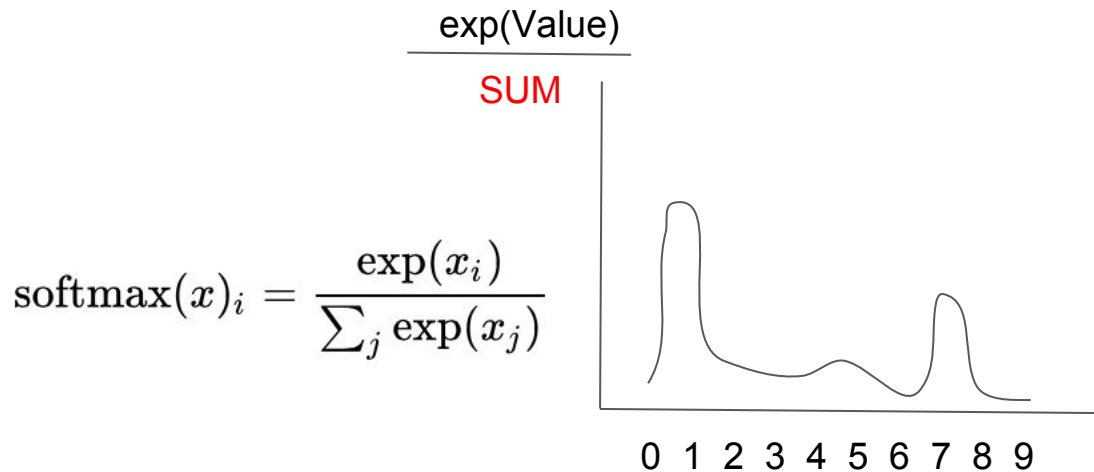
$$\text{softmax}(x)_i = \frac{\exp(x_i)}{\sum_j \exp(x_j)}$$

Image



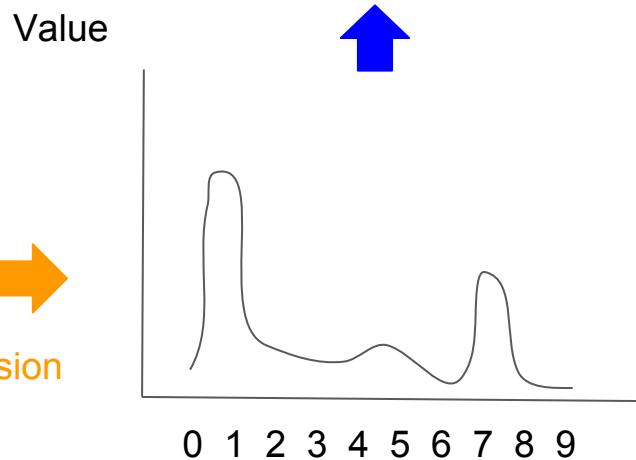
ML
Logistic Regression





ML

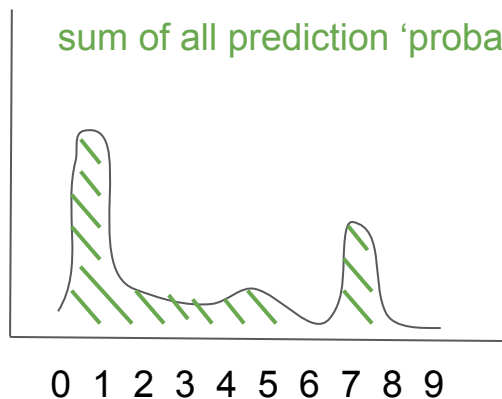
Logistic Regression



$$\text{softmax}(x)_i = \frac{\exp(x_i)}{\sum_j \exp(x_j)}$$

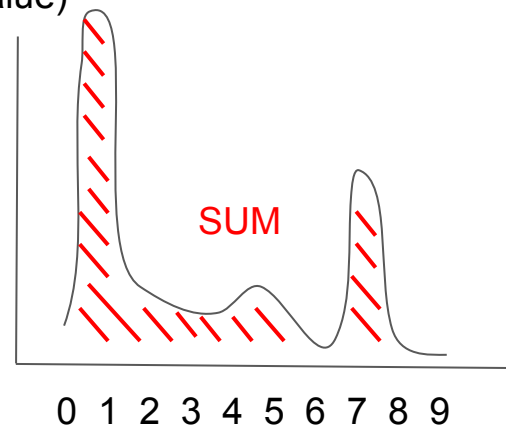
$\frac{\exp(\text{Value})}{\text{SUM}}$

sum of all prediction 'probability' is 1

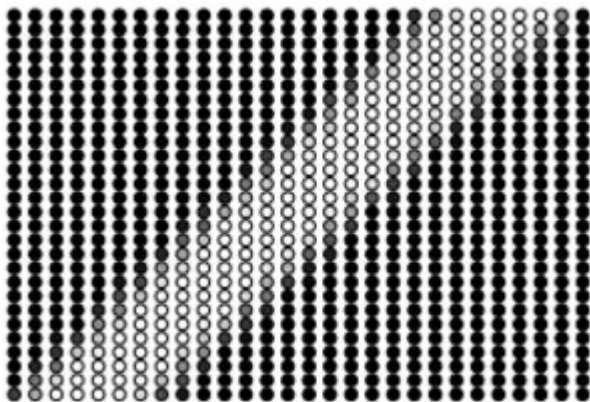


$\exp(\text{Value})$

SUM

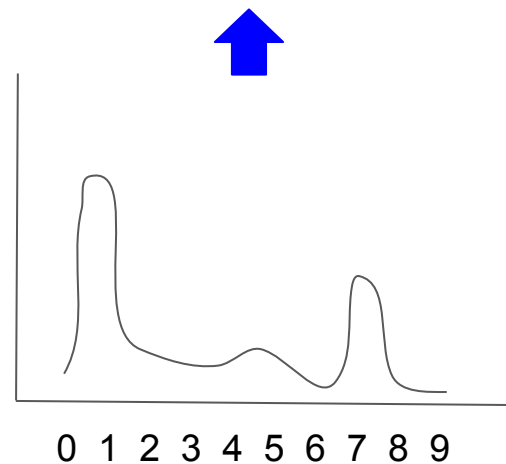


Image



ML
Logistic Regression

Value



Before softmax

$$y = \text{tf.matmul}(x, W) + b$$

With softmax

~~$y = \text{tf.matmul}(x, W) + b$~~

$$\text{softmax}(x)_i = \frac{\exp(x_i)}{\sum_j \exp(x_j)}$$

$y = \text{tf.nn.softmax}(\text{tf.matmul}(x, W) + b)$

Summary

- Cheat sheet: Single feature, Multi-feature, Multi-class
- Logistic regression:
 - Multi-class prediction: Ensure that prediction is one of a discrete set of values
 - Cross-entropy: Measure difference between multi-class prediction and actual
 - Softmax: Ensure the multi-class prediction probability is a valid distribution (sum = 1)

Congrats!

You can now understand Google's Tensorflow Beginner's Tutorial

(<https://www.tensorflow.org/versions/r0.7/tutorials/mnist/beginners/index.html>)

References

- Perform ML with TF using multi-feature linear regression (the wrong way)
 - https://github.com/nethsix/gentle_tensorflow/blob/master/code/linear_regression_multi_feature_using_mini_batch_with_tensorboard.py
- Perform ML with TF using multi-feature linear regression
 - https://github.com/nethsix/gentle_tensorflow/blob/master/code/linear_regression_multi_feature_using_mini_batch_without_matrix_with_tensorboard.py
- Tensorflow official tutorial for character recognition
 - <https://www.tensorflow.org/versions/r0.7/tutorials/mnist/beginners/index.html>
- Colah's excellent explanation of cross-entropy
 - <http://colah.github.io/posts/2015-09-Visual-Information/>