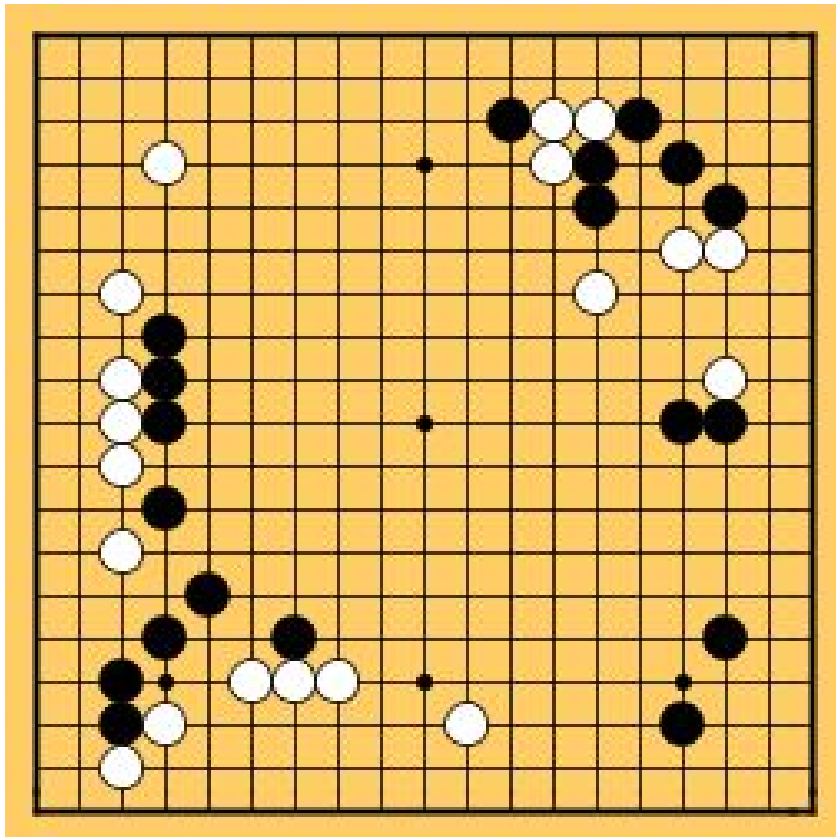


# Human-in-the-loop RL

Emma Brunskill  
CS234 Spring 2017

From here ....  
healthcare...



to education,



## Study

## pre-assessment

B1

B3: Histogram Heights

B3: Histogram Heights 2

B3: Data Underlying

P3: Extracting  
Proportions

B4

B4.2

B5

Skew

Skew2

Shape

Labeling Worked  
Example

Practice Labeling

Practice Labeling Water

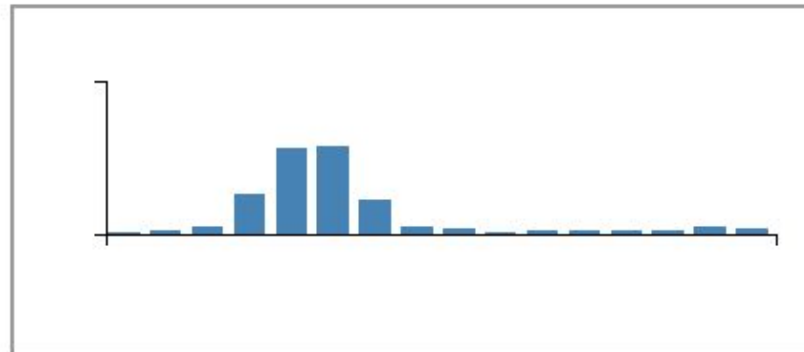
Practice Labeling No  
Histogram: Voters

Practice Why Wrong

VIEW UNIT IN STUDIO

## DESCRIPTIONS AND HISTOGRAMS (1/3 points)

The price of airline tickets varies over time. The following is a histogram that could describe the distribution of airplane ticket prices. Select the best option for each of the questions below.



The x-axis should be labeled as

- ☐ Time
- ☐ Ticket Price
- ☒ Frequency **✗**
- ☐ Distribution

w/Karan Goel, Rika Antonova, Joe  
Runde, Christoph Dann, & Dexter Lee

# Setting

- Set of N skills
  - Understand what x-axis represents
  - Estimate the mean value from a histogram
  - ...
- Assume student can learn each skill independently
- Policy is a mapping from the history of prior skill practices & their outcomes to whether or not to give the student another practice problem
  - E.g. (incorrect, incorrect, incorrect) → give another practice
  - (correct, correct) → no more practice
- Use a parameterized policy to characterize the teaching policy for each skill
- Reward is a function of the student's performance on a post test after the policy for each skill says "no more practice" and how much practice gave

# Initial Work: Bayesian Optimization Policy Search

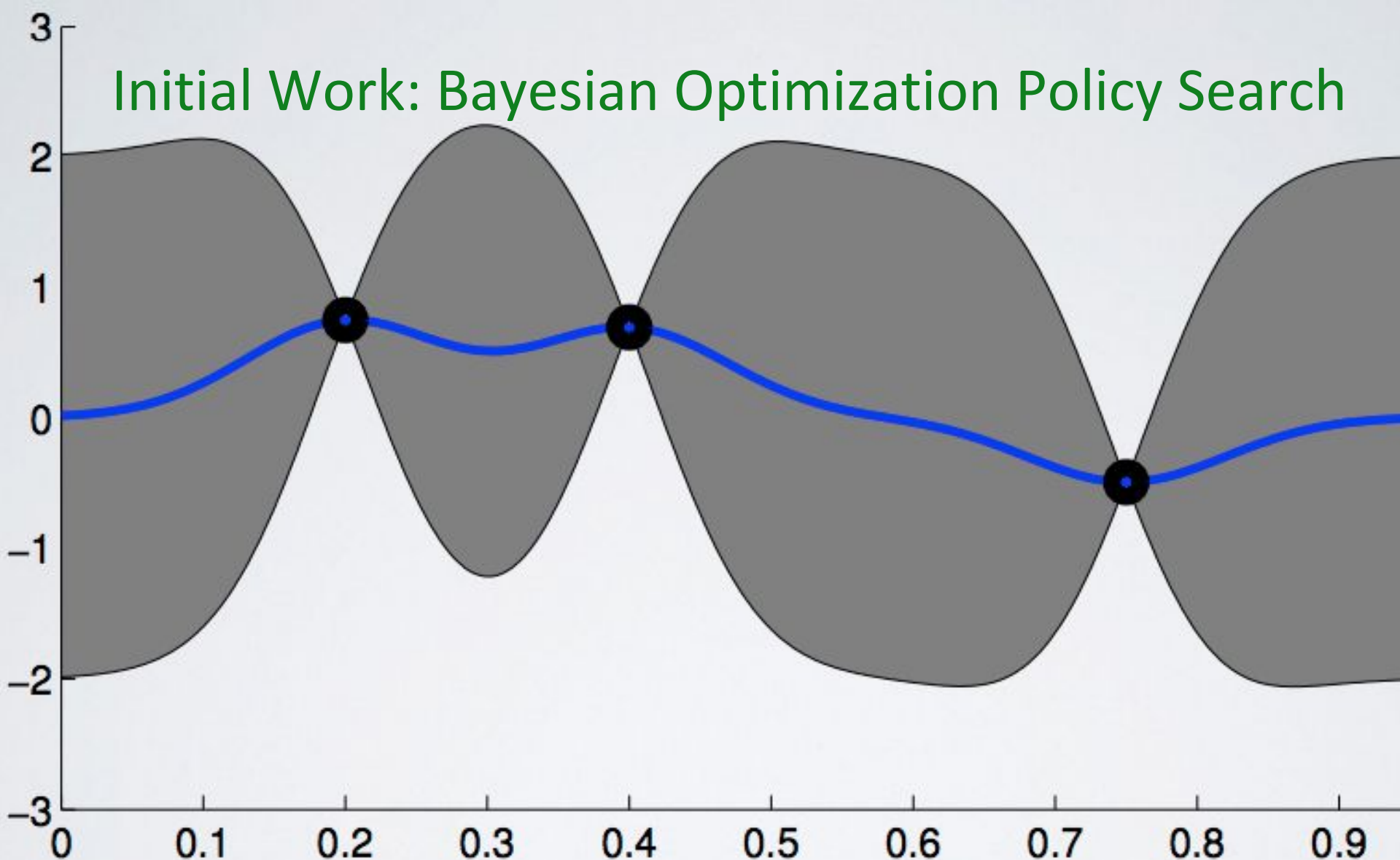
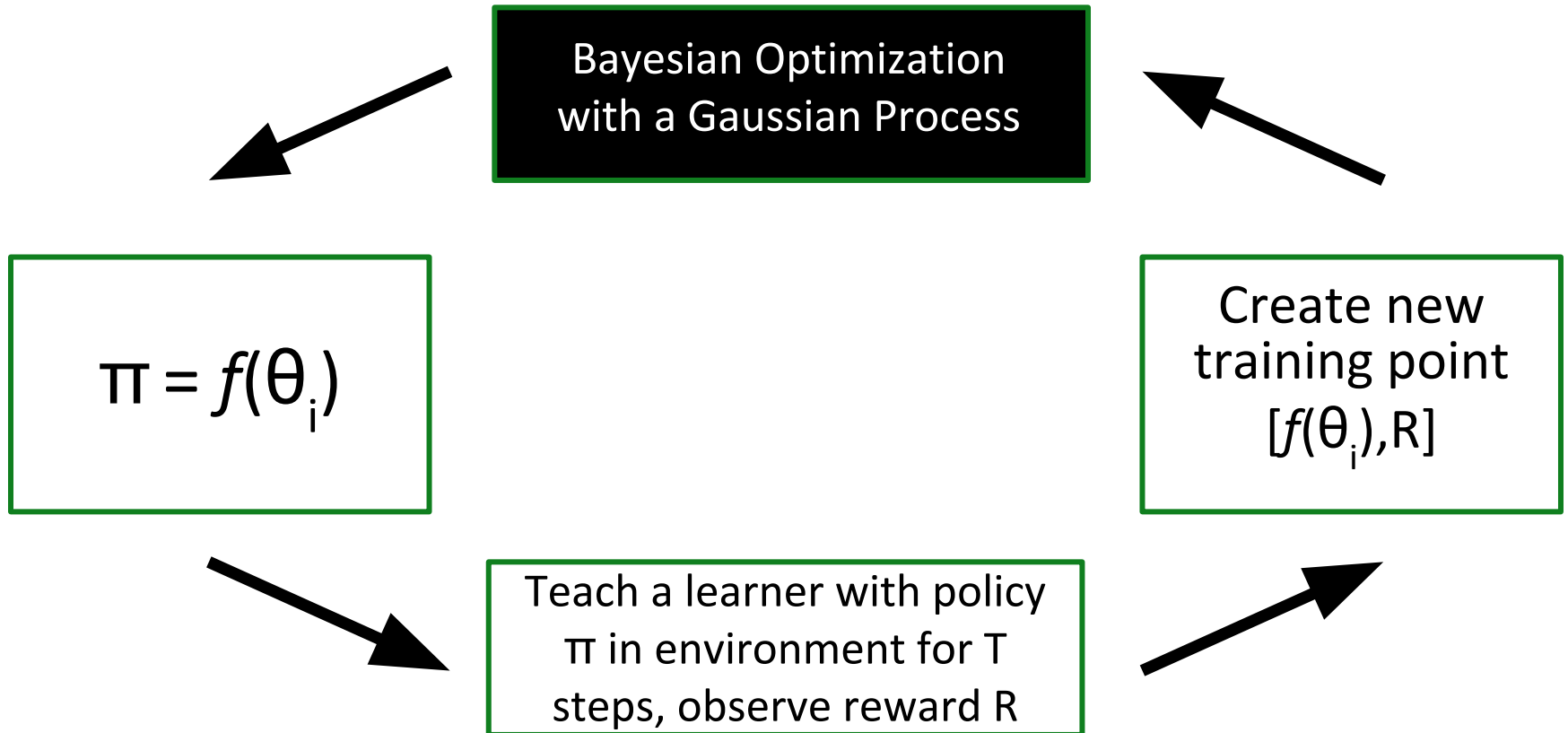


Figure from Ryan Adams

# Learning to Teach

Goal: Should Learn Policy That Maximizes Expected Student Outcomes



# Reward Signal?

- Balance post test performance with amount of practice needed
- $p_s$  = Performance on skill  $s$ ,
- $p$  = Post test performance across all skills,
- $l$  = # practices for skill  $s$

$$f(\pi) = \frac{p_s + \mathbb{I}(p > 9)}{\sqrt{l}}$$

# During Policy Search Tutoring System Stopped Teaching Some Histogram Skills

**Courseware** Course Info Discussion Wiki Progress Instructor **Staff view**

Study

pre-assessment

B1

B3: Histogram Heights

B3: Histogram Heights 2

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P3: Extracting Proportions

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Skew

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Labeling Worked Example

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Practice Labeling Water

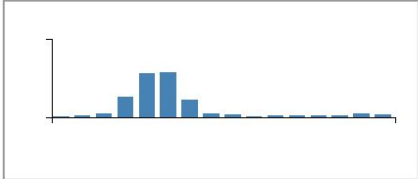
Practice Labeling No Histogram: Voters

Practice Why Wrong

VIEW UNIT IN STUDIO

DESCRIPTIONS AND HISTOGRAMS (1/3 points)

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☐ Ticket Price

☒ Frequency **✗**

☐ Distribution



# Reward Signal: Post Test / # Problems Given

**Courseware** Course Info Discussion Wiki Progress Instructor **Staff view**

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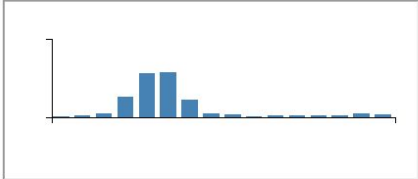
Practice Labeling No Histogram: Voters

Practice Why Wrong

VIEW UNIT IN STUDIO

DESCRIPTIONS AND HISTOGRAMS (1/3 points)

The price of airline tickets varies over time. The following is a histogram that could describe the distribution of airplane ticket prices. Select the best option for each of the questions below.



The x-axis should be labeled as

☐ Time

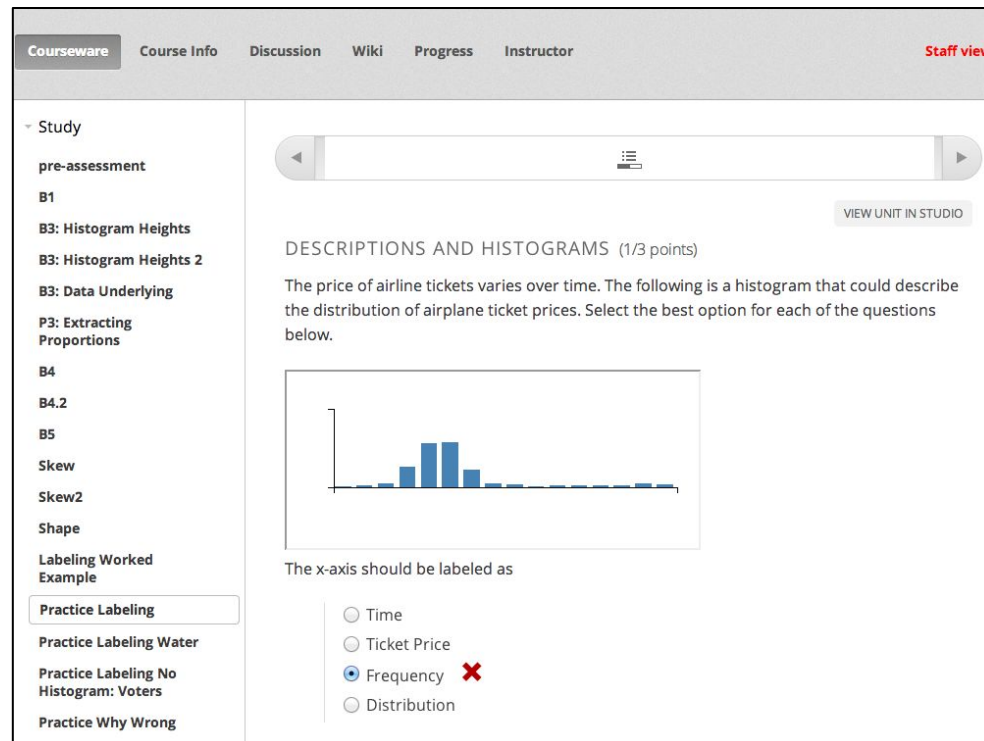
☐ Ticket Price

☒ Frequency **×**

☐ Distribution

$$f(\pi) = \frac{p_s + \mathbb{I}(p > 9)}{\sqrt{l}}$$

# During Policy Search Tutoring System Stopped Teaching Some Histogram Skills



The screenshot shows the Courseware interface with a sidebar on the left and a main content area on the right. The sidebar contains a list of study units: pre-assessment, B1, B3: Histogram Heights, B3: Histogram Heights 2, B3: Data Underlying, P3: Extracting Proportions, B4, B4.2, B5, Skew, Skew2, Shape, Labeling Worked Example, Practice Labeling (highlighted), Practice Labeling Water, Practice Labeling No Histogram: Voters, and Practice Why Wrong. The main content area displays a problem titled "DESCRIPTIONS AND HISTOGRAMS (1/3 points)". The text reads: "The price of airline tickets varies over time. The following is a histogram that could describe the distribution of airplane ticket prices. Select the best option for each of the questions below." Below the text is a histogram with a blue distribution curve. The x-axis is labeled "The x-axis should be labeled as" and the y-axis is labeled "The y-axis should be labeled as". The y-axis has a scale from 0 to 10. The x-axis has a scale from 0 to 10. The histogram shows a distribution that is roughly bell-shaped but slightly skewed to the right. Below the histogram are four radio button options: Time, Ticket Price, Frequency (selected with a red 'X'), and Distribution.

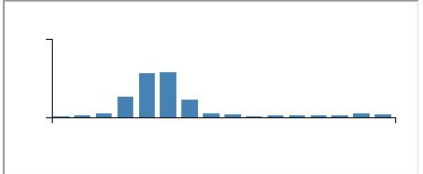
Courseware Course Info Discussion Wiki Progress Instructor Staff view

Study

- pre-assessment
- B1
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- P3: Extracting Proportions
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- Practice Labeling Water
- Practice Labeling No Histogram: Voters
- Practice Why Wrong

DESCRIPTIONS AND HISTOGRAMS (1/3 points)

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- ☒ Frequency
- ☐ Distribution

- No improvement in post test → system had learned that some of our content was inadequate so best thing was to skip it!
- **Content (action space) insufficient to achieve goals**

# Humans are Invention Machines



New actions



New sensors

# Invention Machines: Creating Systems that Can Evolve Beyond Their Original Capacity To Reach Extraordinary Performance



New actions



New sensors

# Problem Formulation

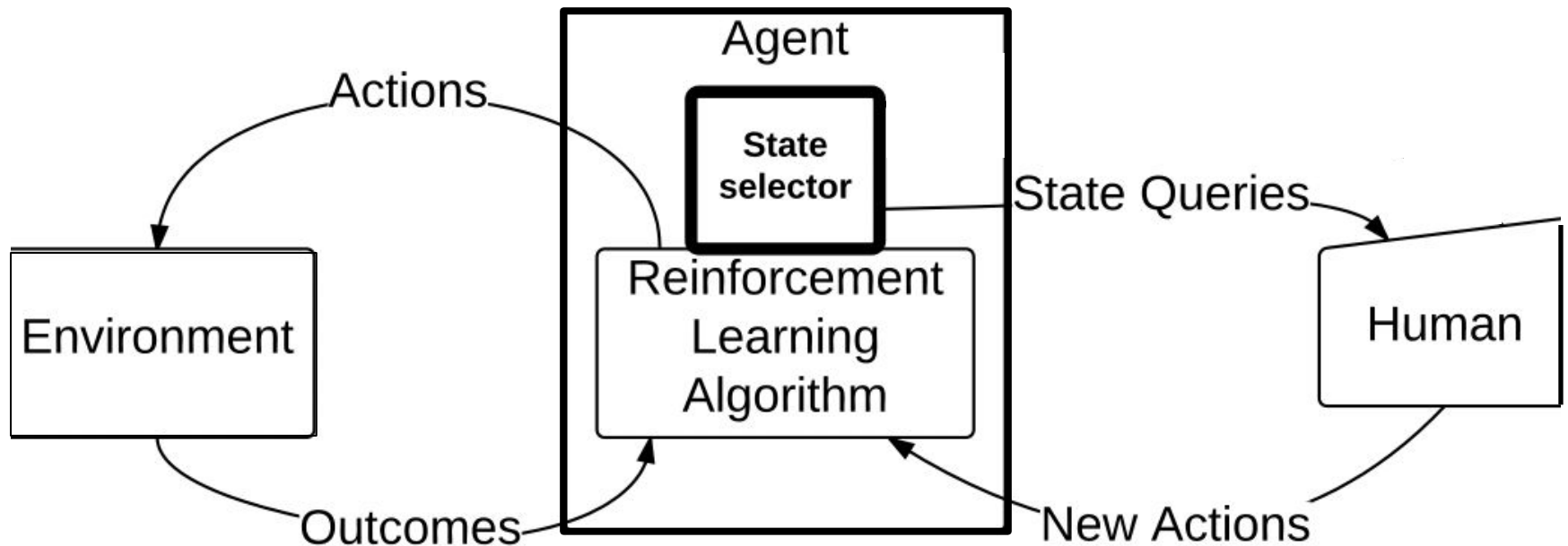
- Maximize expected reward
- Online reinforcement learning
- Directed action invention
  - Where (which states) should we add actions at?

# Related Work

- Policy advice / learning from demonstration
- Changing action spaces
  - Almost all work is reactive, not active solicitation

Online reinforcement  
learning

Active Domain (Action  
Space) Adaptation



# Requesting New Actions

$$\arg \max_s \sum_{s_0 \in S_0} V_{\mathcal{A} \cup a_h}(s_0) p(s_0)$$


Current action set      New action



# Expected Local Improvement

$$\arg \max_s \int_a \underbrace{p_s(a_h)}_{\substack{\text{Prob. human} \\ \text{gives you action} \\ a_h \text{ for state } s}} \underbrace{(V_{\mathcal{A} \cup a_h}(s) - V_{\mathcal{A}}(s))}_{\substack{\text{Improvement in value at state} \\ s \text{ if add in action } a_h}} da_h$$

$$\begin{aligned}
ELI(s) &= \int_a p_s(a_h)(V_{\mathcal{A} \cup a_h}(s) - V_{\mathcal{A}}(s)) da_h \\
&\leq \int_{a: V_{\mathcal{A} \cup a_h}(s) > V_{\mathcal{A}}(s)} p_s(a_h)(V_{\mathcal{A} \cup a_h}(s) - V_{\mathcal{A}}(s)) da_h \\
&\leq \underbrace{(V_{max} - V_{\mathcal{A}}(s))}_{\substack{V(s) \text{ given} \\ \text{current action set}}} \underbrace{\int_{a: V_{\mathcal{A} \cup a_h}(s) > V_{\mathcal{A}}(s)} p_s(a_h) da_h}_{\substack{\text{Probability get a new action} \\ \text{that will increase } V(s)}}
\end{aligned}$$


  
**Unknown!**

# What to Use for $V_{\mathcal{A}}(s)$

$$(V_{max} - V_{\mathcal{A}}(s)) \int_{a: V_{\mathcal{A} \cup a_h}(s) > V_{\mathcal{A}}(s)} p_s(a_h) da_h$$

- Be optimistic (MBIE, Rmax, ...)
- Why?
  - Don't need to add in new actions if current action set might yield optimal behavior
  - Avoids focusing on highly unlikely states

# Probability of Getting a Better Action

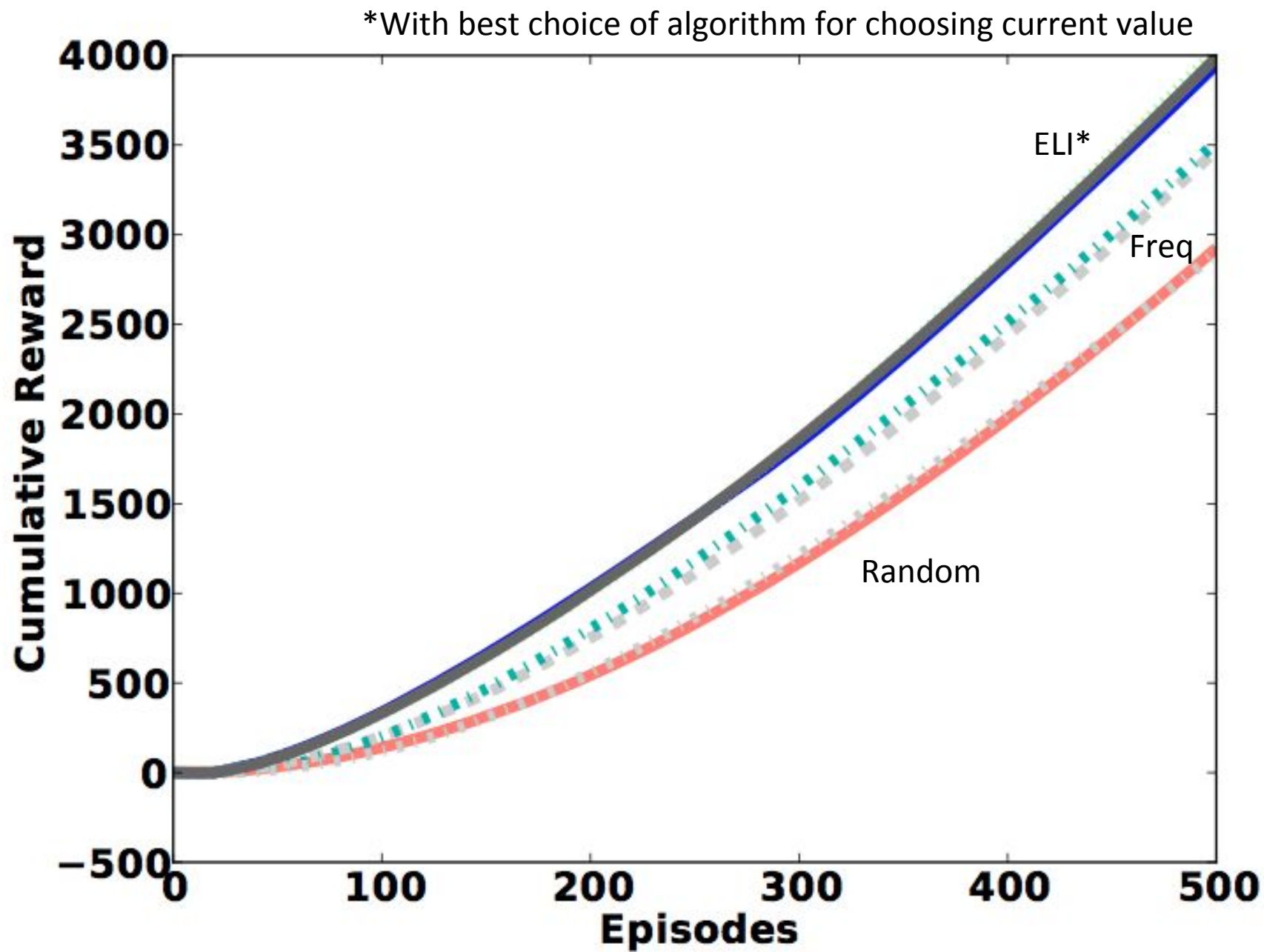
$$(V_{max} - V_{\mathcal{A}}(s)) \int_{a: V_{\mathcal{A} \cup a_h}(s) > V_{\mathcal{A}}(s)} p_s(a_h) da_h$$

- Don't want to ask for actions at same state forever (maybe no improvement possible)
- Model prob of a better action as  $Beta(1, |\mathcal{A}_{s,\ell}| + 1)$
- Chance of better action decays w/ # of actions

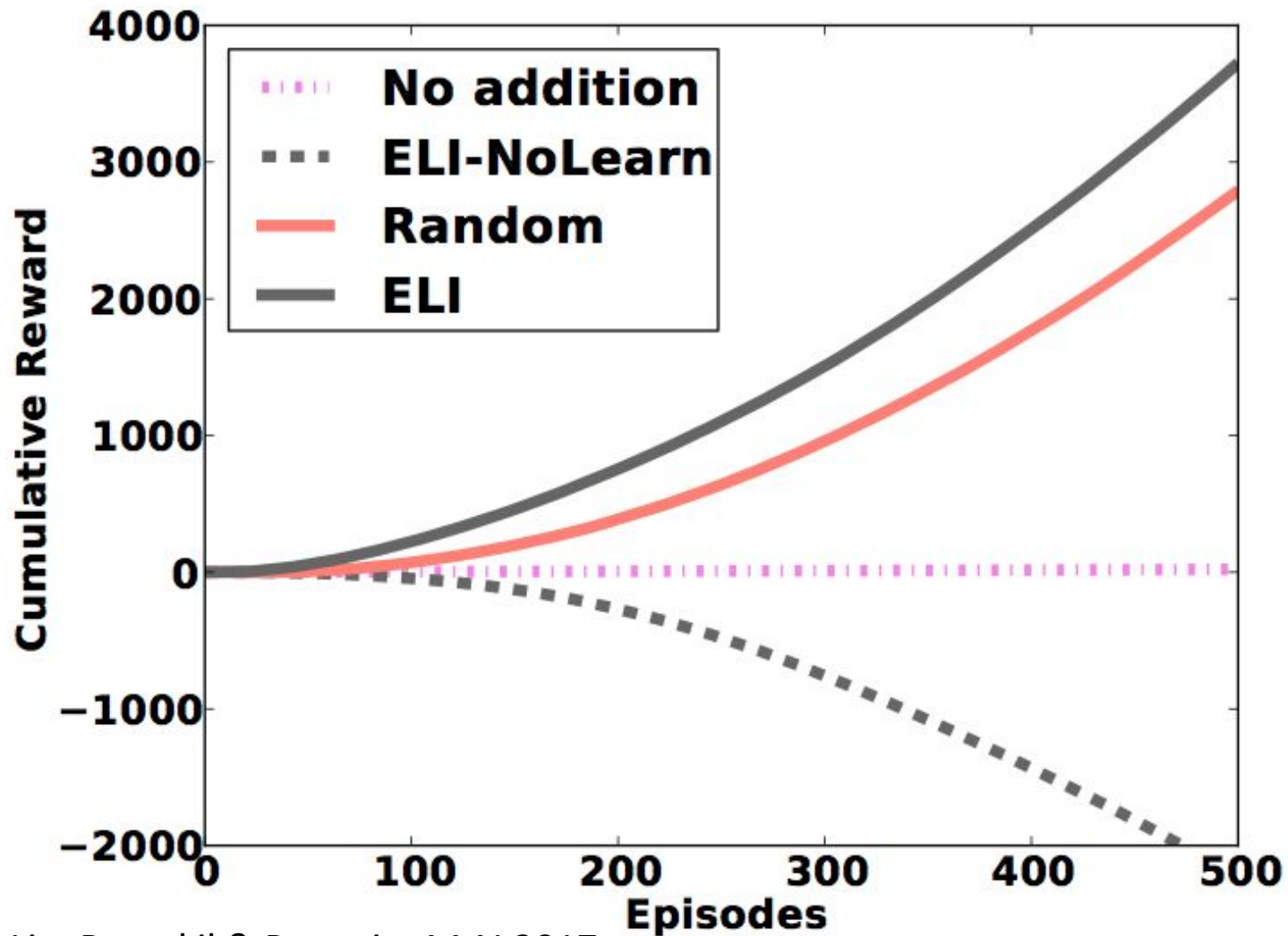
$$ELI(s) = \frac{1}{|\mathcal{A}_{s,\ell}| + 2} (V_{max} - V_{\mathcal{A}}(s))$$

# Simulations

- Large action task\* (Sallans & Hinton 2004)
  - 13 states
  - 273 outcomes (next possible states per state)
  - $2^{20}$  actions per state
- At start each  $s$  has single  $a$  (like default  $\pi$ )
- Every 20 steps can request an action
  - Sample action at random from action set for  $s$
  - Compare ELI vs Random  $s$  vs High freq  $s$



# Mostly Bad Human Input



Chrissy loves exploring outdoors. Yesterday, she saw a herd of 12 elk being chased by a pack of 8 wolves. How many animals in total did Chrissy see while she was exploring?



'animals' needs to be the total of all important parts.

8

12

animals





Chrissy loves exploring outdoors. Yesterday, she saw a herd of 12 elk being chased by a pack of 8 wolves. How many animals in total did Chrissy see while she was exploring?



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12

animals

- New actions = new hints
- Learning where to ask for new hints



# Summary

- Can use RL towards personalized, automated tutoring
  - More applications next week!
- Can create RL systems that evolve beyond their original specification
  - Not limited by original state/action space
  - Help humans-in-the-loop prioritize effort
  - Towards extraordinary performance