

# Package ‘symmetry’

May 12, 2019

**Title** What the Package Does (one line, title case)

**Version** 0.0.0.9000

**Description** What the package does (one paragraph).

**Depends** R (>= 3.1.0)

**License** What license is it under?

**Encoding** UTF-8

**LazyData** true

**Imports** Rcpp, RcppArmadillo

**LinkingTo** Rcpp, RcppArmadillo

**RoxygenNote** 6.1.1

**SystemRequirements** C++11

**Suggests** knitr, rmarkdown, sn, fGarch

**VignetteBuilder** knitr

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B1	<i>Calculate <math>\sqrt{b_1}</math> test statistic (see 'Value' for formula)</i>
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---

### Description

Calculate  $\sqrt{b_1}$  test statistic (see 'Value' for formula)

### Usage

`B1(X, mu = 0)`

### Arguments

X	the sample for which to calculate the statistic
mu	the estimate of the location parameter

### Value

The value of the test statistic given by the formula: < to be added >

### Examples

```
set.seed(1)
X <- rnorm(50)
B1(X, 2)
```

---

BHI	<i>Calculate _ test statistic (see 'Value' for formula)</i>
-----	---

---

### Description

Calculate \_ test statistic (see 'Value' for formula)

### Usage

`BHI(X, mu = 0)`

### Arguments

X	the sample for which to calculate the statistic
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula:

$$\frac{1}{n \binom{n}{2}} \sum_{\mathcal{I}_2} \sum_{i_3=1}^n \left( \frac{1}{2} I\{|X_{i_1} - \mu| < |X_{i_3} - \mu|\} + \frac{1}{2} I\{|X_{i_2} - \mu| < |X_{i_3} - \mu|\} - I\{|X_{(2),X_{i_1},X_{i_2}} - \mu| < |X_{i_3} - \mu|\} \right)$$

**Examples**

```
set.seed(1)
X <- rnorm(50)
BHI(X)
X <- rnorm(50, 1)
BHI(X, 1)
```

---

BHK

---

*Calculate \_ test statistic (see 'Value' for formula)*


---

**Description**

Calculate \_ test statistic (see 'Value' for formula)

**Usage**

```
BHK(X, mu = 0)
```

**Arguments**

X	the sample for which to calculate the statistic
mu	the estimate of the location parameter
k	the value of parameter 'k' used in the formula

**Examples**

```
set.seed(1)
X <- rnorm(50)
BHK(X, 2)
X <- rnorm(50, 1)
BHK(X, 2, 1)
```

---

CH	<i>Calculate _ test statistic (see 'Value' for formula)</i>
----	---

---

**Description**

Calculate \_ test statistic (see 'Value' for formula)

**Usage**

```
CH(X, mu = 0)
```

**Arguments**

X	the sample for which to calculate the statistic
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula: < to be added >

**Examples**

```
set.seed(1)
X <- rnorm(50)
CH(X, 2)
```

---

CM	<i>Calculate Cabilio–Masaro test statistic (see 'Value' for formula)</i>
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---

**Description**

Calculate Cabilio–Masaro test statistic (see 'Value' for formula)

**Usage**

```
CM(X, mu = 0)
```

**Arguments**

X	the sample for which to calculate the statistic
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula: <to be added>

**Examples**

```
set.seed(1)
X <- rnorm(50)
CM(X, 2)
```

K2

*Calculate \_ test statistic (see 'Value' for formula)***Description**

Calculate \_ test statistic (see 'Value' for formula)

**Usage**

K2(X)

**Arguments**

X the sample for which to calculate the statistic

**Value**

The value of the test statistic given by the formula:

$$\sup_{t>0} \frac{1}{n^2} \left| \sum_{i,j=1}^n I\{|X_i - X_j| < t\} - I\{|X_i + X_j| < t\} \right|$$

**Examples**

```
set.seed(1)
X <- rnorm(50)
K2(X)
```

K2U

*Calculate \_ test statistic (see 'Value' for formula)***Description**

Calculate \_ test statistic (see 'Value' for formula)

**Usage**

K2U(X)

**Arguments**

X the sample for which to calculate the statistic

**Value**

The value of the test statistic given by the formula:

$$\sup_{t>0} \frac{1}{\binom{n}{2}} \left| \sum_{1 \leq i < j \leq n} I\{|X_i - X_j| < t\} - I\{|X_i + X_j| < t\} \right|$$

**Examples**

```
set.seed(1)
X <- rnorm(50)
KS(X)
```

KS

*Calculate Kolmogorov Smirnov test statistic (see 'Value' for formula)***Description**

Calculate Kolmogorov Smirnov test statistic (see 'Value' for formula)

**Usage**

```
KS(X, mu = 0)
```

**Arguments**

X	the sample for which to calculate the statistic
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula:

$$\sup_t |F_n(t + \mu) - (1 - F_n(\mu - t))|$$

**Examples**

```
set.seed(1)
X <- rnorm(50)
KS(X)
```

L2

*Calculate \_ test statistic (see 'Value' for formula)***Description**

Calculate \_ test statistic (see 'Value' for formula)

**Usage**

```
L2(X, k)
```

**Arguments**

X	the sample for which to calculate the statistic
k	the tuning parameter for the Laplace transform

**Value**

The value of the test statistic given by the formula:

$$\frac{1}{n^4} \sum_{i,j,k,l=1}^n \left( \frac{1}{k+|X_i-X_j|+|X_k-X_l|} - \frac{1}{k+|X_i-X_j|+|X_k+X_l|} - \frac{1}{k+|X_i+X_j|+|X_k-X_l|} + \frac{1}{k+|X_i+X_j|+|X_k+X_l|} \right)$$

**Examples**

```
set.seed(1)
X <- rnorm(50)
L2(X, 5)
```

---

M

---

*Calculate Mira test statistic (see 'Value' for formula)*


---

**Description**

Calculate Mira test statistic (see 'Value' for formula)

**Usage**

```
M(X, mu = 0)
```

**Arguments**

X	the sample for which to calculate the statistic
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula: < to be added >

**Examples**

```
set.seed(1)
X <- rnorm(50)
M(X, 2)
```

---

MGG	<i>Calculate MGG test statistic (see 'Value' for formula)</i>
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---

**Description**

Calculate MGG test statistic (see 'Value' for formula)

**Usage**

```
MGG(X, mu = 0)
```

**Arguments**

X	the sample for which to calculate the statistic
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula: <to be added>

**Examples**

```
set.seed(1)
X <- rnorm(50)
MGG(X, 2)
```

---

MI	<i>Calculate _ test statistic (see 'Value' for formula)</i>
----	---

---

**Description**

Calculate \_ test statistic (see 'Value' for formula)

**Usage**

```
MI(X, k, mu = 0)
```

**Arguments**

X	the sample for which to calculate the statistic
k	the value of parameter 'k' used in the formula
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula:

$$\frac{1}{n \binom{n}{2k+1}} \sum_{\mathcal{I}_{2k}} \sum_{i_{2k+1}=1}^n I\{- (X_{(k+1), X_{i_1}, \dots, X_{i_{2k}}} - \mu) < X_{i_{2k+1}} - \mu\} - I\{X_{(k+1), X_{i_1}, \dots, X_{i_{2k}}} - \mu < X_{i_{2k+1}} - \mu\}$$



**Examples**

```
set.seed(1)
X <- rnorm(50)
MI(X, 2)
X <- rnorm(50, 1)
MI(X, 2, 1)
```

MK

*Calculate \_ test statistic (see 'Value' for formula)***Description**

Calculate \_ test statistic (see 'Value' for formula)

**Usage**

```
MK(X, k, mu = 0)
```

**Arguments**

X	the sample for which to calculate the statistic
k	the value of parameter 'k' used in the formula
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula:

$$\sup_{t>0} \left| \frac{1}{\binom{n}{2k}} \sum_{\mathcal{I}_{2k}} I\{-(X_{(k+1),X_{i_1},\dots,X_{i_{2k}}} - \mu) < t\} - I\{X_{(k+1),X_{i_1},\dots,X_{i_{2k}}} - \mu < t\} \right|$$

**Examples**

```
set.seed(1)
X <- rnorm(50)
MK(X, 2)
X <- rnorm(50, 1)
MK(X, 2, 1)
```

---

MOI	<i>Calculate _ test statistic (see 'Value' for formula)</i>
-----	---

---

**Description**

Calculate \_ test statistic (see 'Value' for formula)

**Usage**

MOI(X, k, mu = 0)

**Arguments**

X	the sample for which to calculate the statistic
k	the value of parameter 'k' used in the formula
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula:

$$\frac{1}{n \binom{n}{2k}} \sum_{\mathcal{I}_{2k}} \sum_{i_{2k+1}=1}^n I\{|X_{(k), X_{i_1}, \dots, X_{i_{2k}}} - \mu| < |X_{i_{2k+1}} - \mu|\} - I\{|X_{(k+1), X_{i_1}, \dots, X_{i_{2k}}} - \mu| < |X_{i_{2k+1}} - \mu|\}$$

**Examples**

```
set.seed(1)
X <- rnorm(50)
MOI(X, 2)
X <- rnorm(50, 1)
MOI(X, 2, 1)
```

---

MOK	<i>Calculate _ test statistic (see 'Value' for formula)</i>
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---

**Description**

Calculate \_ test statistic (see 'Value' for formula)

**Usage**

MOK(X, k, mu = 0)

**Arguments**

X	the sample for which to calculate the statistic
k	the value of parameter 'k' used in the formula
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula:

$$\sup_{t>0} \left| \frac{1}{\binom{n}{2k}} \sum_{\mathcal{I}_{2k}} I\{|X_{(k),X_{i_1},\dots,X_{i_{2k}}} - \mu| < t\} - I\{|X_{(k+1),X_{i_1},\dots,X_{i_{2k}}} - \mu| < t\} \right|$$

**Examples**

```
set.seed(1)
X <- rnorm(50)
MOK(X, 2)
X <- rnorm(50, 1)
MOK(X, 2, 1)
```

---

NAI	<i>Calculate _ test statistic (see 'Value' for formula)</i>
-----	---

---

**Description**

Calculate \_ test statistic (see 'Value' for formula)

**Usage**

```
NAI(X, k, mu = 0)
```

**Arguments**

X	the sample for which to calculate the statistic
k	the value of parameter 'k' used in the formula
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula:

$$\frac{1}{n \binom{n}{k}} \sum_{\mathcal{I}_k} \sum_{i_{k+1}=1}^n I\{|X_{(1),X_{i_1},\dots,X_{i_k}} - \mu| < |X_{i_{k+1}} - \mu|\} - I\{|X_{(k),X_{i_1},\dots,X_{i_k}} - \mu| < |X_{i_{k+1}} - \mu|\}$$

**Examples**

```
set.seed(1)
X <- rnorm(50)
NAI(X, 2)
X <- rnorm(50, 1)
NAI(X, 2, 1)
```

---

NAK	<i>Calculate _ test statistic (see 'Value' for formula)</i>
-----	---

---

### Description

Calculate \_ test statistic (see 'Value' for formula)

### Usage

```
NAK(X, k, mu = 0)
```

### Arguments

X	the sample for which to calculate the statistic
k	the value of parameter 'k' used in the formula
mu	the estimate of the location parameter

### Value

The value of the test statistic given by the formula:

$$\sup_{t>0} \left| \frac{1}{\binom{n}{k}} \sum_{\mathcal{I}_k} I\{|X_{(1),X_{i_1},\dots,X_{i_k}} - \mu| < t\} - I\{|X_{(k),X_{i_1},\dots,X_{i_k}} - \mu| < t\} \right|$$

### Examples

```
set.seed(1)
X <- rnorm(50)
NAK(X, 2)
X <- rnorm(50, 1)
NAK(X, 2, 1)
```

---

parTvalues	<i>Simulate the distribution of a test statistic in parallel</i>
------------	--

---

### Description

This is just a parallel version of the [Tvalues](#) function, all arguments apply for this function. See [Tvalues](#).

### Usage

```
parTvalues(N, n, dist = list(), TS = list(), freecores = 0,
  clust = NULL)
```

**Arguments**

N	the number of simulations to do
n	the sample size for each simulation
dist	a list which specifies the null distribution (see details)
TS	a list which specifies the test statistic to use (see details)
freecores	how many cores to leave unused (0 for maximum use of cpu)
clust	a cluster to use for parallel

**Value**

A vector of size N, each element being the value of the statistic TS on simulated samples of size n.

**Examples**

```
parTvalues(1000, 50, list(name='norm'), list(name='I1', k=2))
parTvalues(1000, 50, list(name='unif', min=-1, max=1), list(name='I2'))
parTvalues(1000, 50, list(name='logis', loc=0.5), list(name='K1', k=2))
parTvalues(1000, 50, list(name='exp'), list(name='K2'))
```

---

rmixnorm	<i>Mixture of 2 normal distributions</i>
----------	--

---

**Description**

Generates random numbers from a mixture of 2 normal distributions

**Usage**

```
rmixnorm(n, mean1 = 0, sd1 = 1, mean2 = 0, sd2 = 1, p = 0.5)
```

**Arguments**

n	number of observations
mean1	mean of the first normal
sd1	standard deviation of the first normal
mean2	mean of the second normal
sd2	standard deviation of the second normal
p	probability of the first normal

**Value**

Vector of random numbers from the specified mixture of normals.

---

rsl	<i>Azzalini skew logistic distribution</i>
-----	--

---

**Description**

Generates random numbers from the skew logistic distribution

**Usage**

```
rsl(n = 1, xi = 0, omega = 1, alpha = 0, dp = NULL)
```

**Arguments**

n	sample size.
xi	vector of location parameters.
omega	vector of (positive) scale parameters.
alpha	vector of slant parameters.
dp	a vector of length 3 whose elements represent the parameters described above. If dp is specified, the individual parameters cannot be set.

**Value**

Vector of random numbers from Azzalini skew logistic distribution.

---

SGN	<i>Calculate Signed test statistic (see 'Value' for formula)</i>
-----	--

---

**Description**

Calculate Signed test statistic (see 'Value' for formula)

**Usage**

```
SGN(X, mu = 0)
```

**Arguments**

X	the sample for which to calculate the statistic
mu	the estimate of the location parameter

**Value**

The value of the test statistic given by the formula:

$$\frac{1}{n} \sum_{i=1}^n I\{X_i - \mu > 0\} - \frac{1}{2}$$

**Examples**

```
set.seed(1)
X <- rnorm(50)
SGN(X)
```

---

symmetry	<i>symmetry: A package which implements tests for symmetry</i>
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**Description**

symmetry: A package which implements tests for symmetry

---

test_power	<i>Calculate the power of a test</i>
------------	--------------------------------------

---

**Description**

This function calculates the power of a test given the null and alternative T values and the significance level.

**Usage**

```
test_power(t0, t1, alpha = 0.05, two_sided = FALSE)
```

**Arguments**

t0	the vector of null T values
t1	the vector of alternative T values
alpha	the significance level
two_sided	indicator whether to use two sided critical region

---

Tvalues	<i>Simulate the distribution of a test statistic</i>
---------	--

---

**Description**

Simulates the distribution of the specified test statistic under the given null distribution.

**Usage**

```
Tvalues(N, n, dist = list(), TS = list())
```

**Arguments**

N	the number of simulations to do
n	the sample size for each simulation
dist	a list which specifies the null distribution (see details)
TS	a list which specifies the test statistic to use (see details)

### Details

The `dist` argument is a list which must contain a field called "name" which determines which distribution to use (e.g. "norm", "unif", "exp", etc.) and, if needed, the parameters for the distribution. The name must be such that the function "r"+name exists ("rnorm", "runif", "rexp", etc). Further parameters are passed to that function.

The `TS` argument is a list which must contain a field called "name" which specifies which test statistic function to use for each sample. The name can be "I1", "K1", "I2", "K2" for statistics implemented by us, or any other statistic for which an R function exists (e.g. "mean", "var", etc.).

### Value

A vector of size `N`, each element being the value of the statistic `TS` on simulated samples of size `n`.

### Examples

```
Tvalues(1000, 50, list(name='norm'), list(name='I1', k=2))
Tvalues(1000, 50, list(name='unif', min=-1, max=1), list(name='I2'))
Tvalues(1000, 50, list(name='logis', loc=0.5, sca=1), list(name='K1', k=2))
Tvalues(1000, 50, list(name='exp'), list(name='K2'))
```

---

WCX	<i>Calculate Wilcoxon test statistic (see 'Value' for formula)</i>
-----	--

---

### Description

Calculate Wilcoxon test statistic (see 'Value' for formula)

### Usage

```
WCX(X, mu = 0)
```

### Arguments

<code>X</code>	the sample for which to calculate the statistic
<code>mu</code>	the estimate of the location parameter

### Value

The value of the test statistic given by the formula:

$$\frac{1}{\binom{n}{2}} \sum_{1 \leq i < j \leq n} I\{X_i + X_j - 2\mu > 0\} - \frac{1}{2}$$

### Examples

```
set.seed(1)
X <- rnorm(50)
WCX(X)
```



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