# Package 'symmetry'

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Title What the Package Does (one line, title case)						
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BHK						
HG						
<u>I1</u>						
12						
I2A						
12HU						
I2HUA						
I2U						
12UA						

 2 BHI

parTvalues	٠.																						
rsl																							
SGN																							
symmetry																							
test_power	•																						
Tvalues .																							
WCX																							

Index 18

BHI

Calculate \_ test statistic (see 'Value' for formula)

## Description

Calculate \_ test statistic (see 'Value' for formula)

## Usage

```
BHI(X, mu = 0)
```

## **Arguments**

X the sample for which to calculate the statistic
mu the estimate of the location parameter

## Value

The value of the test statistic given by the formula:

$$\frac{1}{n\binom{n}{2}} \sum_{\mathcal{I}_2} \sum_{i_3=1}^n \left( \frac{1}{2} I\{|X_{i_1} - \mu| < |X_{i_3} - \mu|\} + \frac{1}{2} I\{|X_{i_2} - \mu| < |X_{i_3} - \mu|\} - I\{|X_{(2), X_{i_1}, X_{i_2}} - \mu| < |X_{i_3} - \mu|\} \right)$$

```
set.seed(1)
X <- rnorm(50)
BHI(X)
X <- rnorm(50, 1)
BHI(X, 1)</pre>
```

BHK 3

BHK

Calculate \_ test statistic (see 'Value' for formula)

#### **Description**

Calculate \_ test statistic (see 'Value' for formula)

#### Usage

```
BHK(X, mu = 0)
```

## **Arguments**

X the sample for which to calculate the statistic
mu the estimate of the location parameter
k the value of parameter 'k' used in the formula

#### **Examples**

```
set.seed(1)
X <- rnorm(50)
BHK(X, 2)
X <- rnorm(50, 1)
BHK(X, 2, 1)</pre>
```

HG

Calculate \_ test statistic (see 'Value' for formula)

## **Description**

Calculate \_ test statistic (see 'Value' for formula)

# Usage

$$HG(X, k, t, H = TRUE)$$

#### **Arguments**

the sample for which to calculate the statistic
 the value of parameter 'k' used in the formula
 the value with which to compare in indicator
 whether to calculate H or G

## Value

The value of the statistics given by the formula:

$$H = \frac{1}{\binom{n}{2k+1}} \sum_{\mathcal{I}_{2k+1}} I\{-X_{(k+1),X_{i_1},...,X_{i_{2k+1}}} < t\}$$

$$G = \frac{1}{\binom{n}{2k+1}} \sum_{\mathcal{I}_{2k+1}} I\{X_{(k+1),X_{i_1},...,X_{i_{2k+1}}} < t\}$$

4 I2

## **Examples**

```
set.seed(1)
X <- rnorm(50)
HG(X, 2)</pre>
```

Ι1

Calculate \_ test statistic (see 'Value' for formula)

## Description

Calculate \_ test statistic (see 'Value' for formula)

## Usage

$$I1(X, k, mu = 0)$$

## **Arguments**

X the sample for which to calculate the statistic k the value of parameter 'k' used in the formula mu the estimate of the location parameter

#### Value

The value of the test statistic given by the formula:

$$\frac{1}{n\binom{n}{2k}}\sum_{\mathcal{I}_{2k}}\sum_{i_{2k+1}=1}^{n}I\{|X_{(k),X_{i_1},...,X_{i_{2k}}}-\mu|<|X_{i_{2k+1}}-\mu|\}-I\{|X_{(k+1),X_{i_1},...,X_{i_{2k}}}-\mu|<|X_{i_{2k+1}}-\mu|\}$$

## **Examples**

```
set.seed(1)
X <- rnorm(50)
I1(X, 2)
X <- rnorm(50, 1)
I1(X, 2, 1)</pre>
```

12

Calculate \_ test statistic (see 'Value' for formula)

## Description

Calculate \_ test statistic (see 'Value' for formula)

## Usage

I2(X)

*I2A* 5

## **Arguments**

Χ

the sample for which to calculate the statistic

## Value

The value of the test statistic given by the formula:

$$\frac{1}{n^4} \sum_{i,j,a,b=1}^n I\{|X_i - X_j| < X_a + X_b\} - I\{|X_i + X_j| < X_a + X_b\}$$

## **Examples**

```
set.seed(1)
X <- rnorm(50)
I2(X)</pre>
```

I2A

Calculate \_ test statistic (see 'Value' for formula)

## Description

Calculate \_ test statistic (see 'Value' for formula)

## Usage

I2A(X)

## **Arguments**

Χ

the sample for which to calculate the statistic

## Value

The value of the test statistic given by the formula:

$$\frac{1}{n^4} \sum_{i,j,a,b=1}^n I\{|X_i - X_j| < |X_a + X_b|\} - I\{|X_i + X_j| < |X_a + X_b|\}$$

```
set.seed(1)
X <- rnorm(50)
I2A(X)</pre>
```

6 I2HUA

I2HU

Calculate \_ test statistic (see 'Value' for formula)

#### **Description**

Calculate \_ test statistic (see 'Value' for formula)

#### Usage

I2HU(X)

#### **Arguments**

Χ

the sample for which to calculate the statistic

## Value

The value of the test statistic given by the formula:

$$\frac{1}{n^2 \binom{n}{2}} \sum_{1 \le i \le j \le n} \sum_{a,b=1}^n I\{|X_i - X_j| < X_a + X_b\} - I\{|X_i + X_j| < X_a + X_b\}$$

## **Examples**

```
set.seed(1)
X <- rnorm(50)
I2HU(X)</pre>
```

I2HUA

Calculate \_ test statistic (see 'Value' for formula)

#### **Description**

Calculate \_ test statistic (see 'Value' for formula)

## Usage

I2HUA(X)

#### **Arguments**

Χ

the sample for which to calculate the statistic

#### Value

The value of the test statistic given by the formula:

$$\frac{1}{n^2 \binom{n}{2}} \sum_{1 \le i \le j \le n} \sum_{a,b=1}^n I\{|X_i - X_j| < |X_a + X_b|\} - I\{|X_i + X_j| < |X_a + X_b|\}$$

*12U* 7

## **Examples**

```
set.seed(1)
X <- rnorm(50)
I2HUA(X)</pre>
```

I2U

Calculate \_ test statistic (see 'Value' for formula)

#### **Description**

Calculate \_ test statistic (see 'Value' for formula)

## Usage

I2U(X)

## **Arguments**

Χ

the sample for which to calculate the statistic

## Value

The value of the test statistic given by the formula:

$$\frac{1}{\binom{n}{4}} \sum_{1 \leq i < j < a < b \leq n} I\{|X_i - X_j| < X_a + X_b\} - I\{|X_i + X_j| < X_a + X_b\}$$

## **Examples**

```
set.seed(1)
X <- rnorm(50)
I2U(X)</pre>
```

I2UA

Calculate \_ test statistic (see 'Value' for formula)

# Description

Calculate \_ test statistic (see 'Value' for formula)

## Usage

I2UA(X)

## **Arguments**

Χ

the sample for which to calculate the statistic

8 I2UAS

#### Value

The value of the test statistic given by the formula:

$$\frac{1}{\binom{n}{4}} \sum_{1 \leq i < j < a < b \leq n} I\{|X_i - X_j| < |X_a + X_b|\} - I\{|X_i + X_j| < |X_a + X_b|\}$$

## **Examples**

```
set.seed(1)
X <- rnorm(50)
I2UA(X)</pre>
```

I2UAS

Calculate \_ test statistic (see 'Value' for formula)

# Description

Calculate \_ test statistic (see 'Value' for formula)

## Usage

I2UAS(X)

# Arguments

Χ

the sample for which to calculate the statistic

## Value

The value of the test statistic given by the formula:

$$\frac{1}{\binom{n}{4}} \sum_{1 \leq i < j < a < b \leq n} I\{|X_i - X_j| < |X_a + X_b|\} - I\{|X_i + X_j| < |X_a + X_b|\}$$

```
set.seed(1)
X <- rnorm(50)
I2UAS(X)</pre>
```

12US 9

I2US

Calculate \_ test statistic (see 'Value' for formula)

## Description

Calculate \_ test statistic (see 'Value' for formula)

## Usage

I2US(X)

## **Arguments**

Χ

the sample for which to calculate the statistic

## Value

The value of the test statistic given by the formula:

$$\frac{1}{\binom{n}{4}} \sum_{1 \le i < j < a < b \le n} I\{|X_i - X_j| < X_a + X_b\} - I\{|X_i + X_j| < X_a + X_b\}$$

#### **Examples**

```
set.seed(1)
X <- rnorm(50)
I2US(X)</pre>
```

Κ1

Calculate \_ test statistic (see 'Value' for formula)

## **Description**

Calculate \_ test statistic (see 'Value' for formula)

#### Usage

$$K1(X, k, mu = 0)$$

## **Arguments**

X the sample for which to calculate the statistic k the value of parameter 'k' used in the formula

mu the estimate of the location parameter

## Value

The value of the test statistic given by the formula:

$$\sup_{t>0} \left| \frac{1}{\binom{n}{2k}} \sum_{\mathcal{I}_{2k}} I\{|X_{(k),X_{i_1},\dots,X_{i_{2k}}} - \mu| < t\} - I\{|X_{(k+1),X_{i_1},\dots,X_{i_{2k}}} - \mu| < t\}\right|$$

10 K2U

## **Examples**

```
set.seed(1)
X <- rnorm(50)
K1(X, 2)
X <- rnorm(50, 1)
K1(X, 2, 1)</pre>
```

K2

Calculate \_ test statistic (see 'Value' for formula)

## **Description**

Calculate \_ test statistic (see 'Value' for formula)

## Usage

K2(X)

## **Arguments**

Χ

the sample for which to calculate the statistic

#### Value

The value of the test statistic given by the formula:

$$\sup_{t>0} \frac{1}{n^2} \left| \sum_{i,j=1}^n I\{|X_i - X_j| < t\} - I\{|X_i + X_j| < t\} \right|$$

# **Examples**

```
set.seed(1)
X <- rnorm(50)
K2(X)</pre>
```

K2U

Calculate \_ test statistic (see 'Value' for formula)

## **Description**

Calculate \_ test statistic (see 'Value' for formula)

## Usage

K2U(X)

## **Arguments**

Χ

the sample for which to calculate the statistic

KS 11

#### Value

The value of the test statistic given by the formula:

$$\sup_{t>0} \frac{1}{\binom{n}{2}} \left| \sum_{1 \le i < j \le n} I\{|X_i - X_j| < t\} - I\{|X_i + X_j| < t\} \right|$$

## **Examples**

```
set.seed(1)
X <- rnorm(50)
K2U(X)</pre>
```

KS

Calculate Kolmogorov Smirnov test statistic (see 'Value' for formula)

# Description

Calculate Kolmogorov Smirnov test statistic (see 'Value' for formula)

# Usage

$$KS(X, mu = 0)$$

# Arguments

X the sample for which to calculate the statistic

mu the estimate of the location parameter

## Value

The value of the test statistic given by the formula:

$$\sup_{t} |F_n(t+\mu) - (1 - F_n(\mu - t))|$$

```
set.seed(1)
X <- rnorm(50)
KS(X)</pre>
```

12 NAI

L1

Calculate \_ test statistic (see 'Value' for formula)

## Description

Calculate \_ test statistic (see 'Value' for formula)

## Usage

## Arguments

X the sample for which to calculate the statistic

a the tuning parameter for the Laplace transform

#### Value

The value of the test statistic given by the formula:

$$\begin{array}{ll} \frac{1}{n^4} \sum_{i,j,k,l=1}^n & \left( \frac{1}{a+|X_i-X_j|+|X_k-X_l|} - \frac{1}{a+|X_i-X_j|+|X_k+X_l|} \right. \\ & \left. - \frac{1}{a+|X_i+X_j|+|X_k-X_l|} + \frac{1}{a+|X_i+X_j|+|X_k+X_l|} \right) \end{array}$$

## **Examples**

```
set.seed(1)
X <- rnorm(50)
L1(X)</pre>
```

NAI

Calculate \_ test statistic (see 'Value' for formula)

## **Description**

Calculate \_ test statistic (see 'Value' for formula)

## Usage

$$NAI(X, k, mu = 0)$$

# Arguments

X the sample for which to calculate the statistic

k the value of parameter 'k' used in the formula

mu the estimate of the location parameter

*NAK* 13

#### Value

The value of the test statistic given by the formula:

$$\frac{1}{n\binom{n}{k}} \sum_{\mathcal{I}_k} \sum_{i_{k+1}=1}^n I\{|X_{(1),X_{i_1},\dots,X_{i_k}} - \mu| < |X_{i_{k+1}} - \mu|\} - I\{|X_{(k),X_{i_1},\dots,X_{i_k}} - \mu| < |X_{i_{k+1}} - \mu|\}$$

## **Examples**

```
set.seed(1)
X <- rnorm(50)
NAI(X, 2)
X <- rnorm(50, 1)
NAI(X, 2, 1)</pre>
```

NAK

Calculate \_ test statistic (see 'Value' for formula)

## **Description**

Calculate \_ test statistic (see 'Value' for formula)

## Usage

```
NAK(X, k, mu = 0)
```

## Arguments

X the sample for which to calculate the statistic
k the value of parameter 'k' used in the formula
mu the estimate of the location parameter

## Value

The value of the test statistic given by the formula:

$$\sup_{t>0} \left| \frac{1}{\binom{n}{k}} \sum_{\mathcal{I}_k} I\{|X_{(1),X_{i_1},\dots,X_{i_k}} - \mu| < t\} - I\{|X_{(k),X_{i_1},\dots,X_{i_k}} - \mu| < t\} \right|$$

```
set.seed(1)
X <- rnorm(50)
NAK(X, 2)
X <- rnorm(50, 1)
NAK(X, 2, 1)</pre>
```

14 rsl

parTvalues	Simulate the distribution of a test statistic in parallel

## **Description**

This is just a parallel version of the Tvalues function, all arguments apply for this function. See Tvalues.

#### Usage

```
parTvalues(N, n, dist = list(), TS = list(), freecores = 0,
  clust = NULL)
```

## **Arguments**

N	the number of simulations to do
n	the sample size for each simulation
dist	a list which specifies the null distribution (see details)
TS	a list which specifies the test statistic to use (see details)
freecores	how many cores to leave unused (0 for maximum use of cpu)
clust	a cluster to use for parallel

## Value

A vector of size N, each element being the value of the statistic TS on simulated samples of size n.

# **Examples**

```
parTvalues(1000, 50, list(name='norm'), list(name='I1', k=2))
parTvalues(1000, 50, list(name='unif', min=-1, max=1), list(name='I2'))
parTvalues(1000, 50, list(name='logis', loc=0.5), list(name='K1', k=2))
parTvalues(1000, 50, list(name='exp'), list(name='K2'))
```

rsl

Azzalini skew logistic distribution

# Description

Generates random numbers from the skew logistic distribution

# Usage

```
rsl(n = 1, xi = 0, omega = 1, alpha = 0, dp = NULL)
```

SGN 15

#### **Arguments**

n sample size.

xi vector of location parameters.

omega vector of (positive) scale parameters.

alpha vector of slant parameters.

dp a vector of length 3 whose elements represent the parameters described above.

If dp is specified, the individual parameters cannot be set.

## Value

Vector of random numbers from Azzalini skew logistic distribution.

SGN

Calculate Signed test statistic (see 'Value' for formula)

## **Description**

Calculate Signed test statistic (see 'Value' for formula)

## Usage

```
SGN(X, mu = 0)
```

# Arguments

X the sample for which to calculate the statistic

mu the estimate of the location parameter

## Value

The value of the test statistic given by the formula:

$$\frac{1}{n}\sum_{i=1}^{n}I\{X_i-\mu>0\}-\frac{1}{2}$$

## **Examples**

```
set.seed(1)
X <- rnorm(50)
SGN(X)</pre>
```

symmetry

symmetry: A package which implements tests for symmetry

## **Description**

symmetry: A package which implements tests for symmetry

Tvalues Tvalues

test_power	Calculate the power of a test

## **Description**

This function calculates the power of a test given the null and alternative T values and the significance level.

## Usage

```
test_power(t0, t1, alpha = 0.05, two_sided = FALSE)
```

## **Arguments**

to the vector of null T values

the vector of alternative T values

alpha the significance level

two\_sided indicator whether to use two sided critical region

Tvalues	Simulate the distribution of a test statistic	

## **Description**

Simulates the distribution of the specified test statistic under the given null distribution.

## Usage

```
Tvalues(N, n, dist = list(), TS = list())
```

## **Arguments**

N	the number of simulations to do
n	the sample size for each simulation
dist	a list which specifies the null distribution (see details)
TS	a list which specifies the test statistic to use (see details)

## **Details**

The dist argument is a list which must contain a field called "name" which determines which distribution to use (e.g. "norm", "unif", "exp", etc.) and, if needed, the parameters for the distribution. The name must be such that the function "r"+name exists ("rnorm", "runif", "rexp", etc). Further parameters are passed to that function.

The TS argument is a list which must contain a field called "name" which specifies which test statistic function to use for each sample. The name can be "I1", "K1", "I2", "K2" for statistics implemented by us, or any other statistic for which an R function exists (e.g. "mean", "var", etc.).

WCX 17

#### Value

A vector of size N, each element being the value of the statistic TS on simulated samples of size n.

## **Examples**

```
Tvalues(1000, 50, list(name='norm'), list(name='I1', k=2))
Tvalues(1000, 50, list(name='unif', min=-1, max=1), list(name='I2'))
Tvalues(1000, 50, list(name='logis', loc=0.5, sca=1), list(name='K1', k=2))
Tvalues(1000, 50, list(name='exp'), list(name='K2'))
```

WCX

Calculate Wilcoxon test statistic (see 'Value' for formula)

## **Description**

Calculate Wilcoxon test statistic (see 'Value' for formula)

## Usage

```
WCX(X, mu = 0)
```

## **Arguments**

X the sample for which to calculate the statistic mu the estimate of the location parameter

## Value

The value of the test statistic given by the formula:

$$\frac{1}{\binom{n}{2}} \sum_{1 \le i < j \le n} I\{X_i + X_j - 2\mu > 0\} - \frac{1}{2}$$

```
set.seed(1)
X <- rnorm(50)
WCX(X)</pre>
```

# **Index**

```
BHI, 2
BHK, 3
HG, 3
I1, 4
I2, 4
I2A, 5
I2HU, 6
I2HUA, 6
I2U, 7
I2UA, 7
I2UAS, 8
I2US, 9
K1, 9
K2, 10
K2U, 10
KS, 11
L1, 12
NAI, 12
NAK, 13
parTvalues, 14
rs1, 14
SGN, 15
symmetry, 15
symmetry-package(symmetry), 15
\texttt{test\_power},\, \textcolor{red}{16}
Tvalues, 14, 16
WCX, 17
```