

This problem set is individual and worth a total of 100 points. Solutions **must** be handed in as a hard copy at the beginning of class on 2/25. Please write your answers **clearly within the space provided** for each question.

Your Name: _____

1. Give the exact number of pointers present in Linked Lists of length n with the following characteristics (the total count may include **head**, **tail**, and links between nodes):

(a) [5 points] A singly linked list with **no tail** pointer

(b) [5 points] A singly linked list with a **tail** pointer

(c) [5 points] A doubly linked list with **no tail** pointer

2. [5 points] Out of insertion sort and selection sort, which sorting algorithm has a better best-case runtime? What type of input would yield this best case behavior?

3. For a dynamic array with an initial capacity of 1, where elements are inserted one at a time:

(a) [5 points] How many times would the array need to be resized to accommodate the insertion of 40 elements if its scaling factor was 3.0?

- (b) [5 points] How many times would the array need to be resized to accommodate the insertion of 100 elements if its scaling factor was 2.0?
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- (c) [10 points] What is the general formula for how many times the array must be resized if it has a scaling factor of k and needs to accept n elements?
-

4. [30 points] Provide the time complexity, using Θ notation, of efficient algorithms for the functions below. Each column represents a linked list. All linked lists store a single integer at each node, no list stores its element count internally, and all lists have a tail pointer except when indicated.

Function	SLL	SLL (no tail)	DLL	CDLL
<code>int size()</code>				
<code>int at(int)</code>				
<code>int front()</code>				
<code>int back()</code>				
<code>bool empty()</code>				
<code>void clear()</code>				
<code>void set(int, int)</code>				
<code>void push_back(int)</code>				
<code>int pop_back()</code>				
<code>void insert_at(int, int)</code>				
<code>void delete_at(int)</code>				
<code>void reverse()</code>				

5. [10 points] Suppose that you have a SLL without a tail pointer. Write a $O(n)$ function to reverse the list. The class **SLL** contains *only* a single pointer **head**. Each **Node** in the list contains a pointer **next** to the next element.

```
void SLL::reverse() {
```

```
}
```

6. [5 points] What major advantages does a dynamic array have over a linked list?

7. [5 points] What major advantages does a linked list have over a dynamic array?

8. [10 points] Examine the following function which implements a destructor for a singly linked list class `SLL`. Is there a bug? If yes, how would you fix it?

```
SLL::~~SLL() {  
    Node *p = head;  
    // go through list and remove all the nodes  
    while(p != NULL) {  
        delete p;  
        p = next;  
    }  
}
```
