PHYS226: Electricity and Magnetism

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Electric Forces ::

$$F_{ab} = k_e \frac{q_a q_b}{d^2}$$

$$E = k_e \frac{q}{r^2}$$

$$E = \frac{F_e}{q_b}$$

$$\tau = p * E = (qE)(dsin(\phi))$$

Ring of Charge::

$$\lambda = \frac{Q}{2\pi a}: dQ = \lambda ds: a \text{ is the height from the origin to the top of the ring.}$$

$$dE = k \frac{dQ}{x^2 + a^2}: x \text{ is the distance from the origin to the point charge.}$$

$$dE = k \frac{\lambda x}{(x^2 + a^2)^{\frac{3}{2}}} ds: \text{Simplified } dE_x$$

$$E = k \frac{Qx}{(x^2 + a^2)^{\frac{3}{2}}}$$

Uniformly Charged Disk ::

$$\begin{split} dQ &= \sigma dA = 2\pi \sigma r dr : \sigma \text{ is the charge per unit area.} \\ dE_x &= k \frac{2\pi \sigma r x}{(x^2 + a^2)^{\frac{3}{2}}} dr \\ E_x &= \frac{\sigma}{2\epsilon_0} [1 - \frac{1}{\sqrt{R^2/x^2 + 1}}] \\ E &= \frac{\sigma}{2\epsilon_0} : \text{ for R } >> x \end{split}$$

Potential Energy and Work ::

$$W = U_a - U_b = -(U_b - U_a) = -\Delta U$$
$$\Delta U = q_0 E d$$

$$W_{a \to b} = Fd = -q_0 Ed$$

$$W_{a\to b} = \int_a^b F \cos\phi \ dl$$

$$U = \frac{kq_aq_b}{r}$$

$$V = \frac{U}{q_0}$$

$$V_a - V_b = -(V_b - V_a) = -\frac{\Delta U}{q_0} = \frac{W_{a \to b}}{q_0}$$

$$V = \frac{\lambda}{2\pi\epsilon_0} ln \frac{R}{r}$$
: For infinite line charge.

$$V = k \frac{Q}{\sqrt{x^2 + a^2}}$$
: For ring of charge.

$$E = \frac{V}{d}$$

$$E = -\Delta V$$

$$q\frac{V}{d} = mg$$

Capacitors and Capacitance ::

$$U = \frac{1}{2}\frac{Q^2}{C} = \frac{1}{2}QV = \frac{1}{2}CV^2$$

Capacitors in series :
$$C_{eq}^{-1} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$$

Capacitors in parallel :
$$C_{eq} = C_1 + C_2 + \dots$$

$$C = \frac{Q}{V}$$