

# Lab Exercise-08:LSTM/GRU-Based Recurrent Neural Network Construction

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## Import Libraries

- **numpy** : Provides efficient support for numerical computations and array operations.
- **pandas** : Facilitates data manipulation and analysis with powerful data structures like DataFrames.
- **matplotlib.pyplot** : Enables creation of static, animated, and interactive visualizations.
- **seaborn** : Enhances data visualization with advanced statistical plots and improved aesthetics.

```
In [1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
```

## Load Dataset

### 1. Country Name

- **Description:** The name of the country.
- **Type:** Categorical/String.

### 2. Country Code

- **Description:** A unique code or abbreviation representing the country.
- **Type:** Categorical/String.

### 3. Year

- **Description:** The year for which the data is recorded.
- **Type:** Numeric/Integer.

### 4. Agriculture (% GDP)

- **Description:** The percentage of a country's Gross Domestic Product (GDP) derived from agriculture.
- **Type:** Numeric/Float.

### 5. Ease of Doing Business

- **Description:** An index or score representing how easy it is to do business in the country, typically based on various factors like regulatory environment, business regulations, etc.
- **Type:** Numeric/Float or Categorical.

### 6. Education Expenditure (% GDP)

- **Description:** The percentage of a country's GDP spent on education.
- **Type:** Numeric/Float.

### 7. Export (% GDP)

- **Description:** The percentage of a country's GDP that comes from exports.
- **Type:** Numeric/Float.

### 8. GDP

- **Description:** The Gross Domestic Product of the country, which measures the total economic output.
- **Type:** Numeric/Float.

## 9. Health Expenditure (% GDP)

- **Description:** The percentage of a country's GDP spent on health care.
- **Type:** Numeric/Float.

## 10. Import (% GDP)

- **Description:** The percentage of a country's GDP that is spent on imports.
- **Type:** Numeric/Float.

## 11. Industry (% GDP)

- **Description:** The percentage of a country's GDP derived from the industrial sector.
- **Type:** Numeric/Float.

## 12. Inflation Rate

- **Description:** The rate at which the general level of prices for goods and services is rising, causing purchasing power to fall.
- **Type:** Numeric/Float.

## 13. R&D

- **Description:** Expenditure on Research and Development as a percentage of GDP, or another measure of R&D investment.
- **Type:** Numeric/Float.

## 14. Service (% GDP)

- **Description:** The percentage of a country's GDP derived from the service sector.
- **Type:** Numeric/Float.

## 15. Unemployment

- **Description:** The percentage of the labor force that is unemployed and actively seeking employment.
- **Type:** Numeric/Float.

## 16. Population

- **Description:** The total number of people living in the country.
- **Type:** Numeric/Integer.

## 17. Land

- **Description:** The total land area of the country.
- **Type:** Numeric/Float.

## 18. Continent Name

- **Description:** The continent on which the country is located.
- **Type:** Categorical/String.

## 19. Export

- **Description:** This feature appears twice in the list; it might be duplicated or refer to different aspects of export data. Ensure consistency or clarification of this feature.
- **Type:** Numeric/Float.

## 20. Import

- **Description:** Similar to exports, this feature appears twice and might need clarification or correction for duplication.
- **Type:** Numeric/Float.

## 21. Education Expenditure

- **Description:** This feature also appears twice; confirm whether it's the same as earlier or a different aspect of education expenditure.
- **Type:** Numeric/Float.

## 22. Health Expenditure

- **Description:** Same as above, confirm the feature's duplication or intended different aspect.

- **Type:** Numeric/Float.

## 23. Net Trade

- **Description:** The difference between exports and imports as a percentage of GDP.
- **Type:** Numeric/Float.

## 24. GDP Per Capita

- **Description:** The GDP divided by the population, representing the average economic output per person.
- **Type:** Numeric/Float.

## 25. Population Density

- **Description:** The number of people per unit area of land (e.g., people per square kilometer).
- **Type:** Numeric/Float.

```
In [2]: df3 = pd.read_csv('/content/Countries.csv')
df3.shape
```

```
Out[2]: (5106, 25)
```

The dataset consists of 5106 rows and 25 columns

```
In [3]: df3.head()
```

Out[3]:

	Country Name	Country Code	Year	Agriculture (% GDP)	Ease of Doing Business	Education Expenditure (% GDP)	Export (% GDP)	GDP	Health Expenditure (% GDP)	Import (% GDP)	...	Population	Land	Continent Name	Exp
0	Afghanistan	AFG	2000	27.501127	40.717968	13.670101	NaN	1.415197e+10	10.902580	NaN	...	19542982.0	652860.0	Asia	f
1	Afghanistan	AFG	2001	27.501127	40.717968	13.670101	NaN	1.415197e+10	10.902580	NaN	...	19688632.0	652860.0	Asia	f
2	Afghanistan	AFG	2002	38.627892	40.717968	13.670101	NaN	3.854235e+09	9.443391	NaN	...	21000256.0	652860.0	Asia	f
3	Afghanistan	AFG	2003	37.418855	40.717968	13.670101	NaN	4.539497e+09	8.941258	NaN	...	22645130.0	652860.0	Asia	f
4	Afghanistan	AFG	2004	29.721067	40.717968	13.670101	NaN	5.220825e+09	9.808474	NaN	...	23553551.0	652860.0	Asia	f

5 rows × 25 columns



In [4]:

```
df3.info()
```

```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 5106 entries, 0 to 5105
Data columns (total 25 columns):
#   Column                                Non-Null Count  Dtype
---  -
0   Country Name                          5106 non-null   object
1   Country Code                          5106 non-null   object
2   Year                                  5106 non-null   int64
3   Agriculture (% GDP)                   4830 non-null   float64
4   Ease of Doing Business                 4508 non-null   float64
5   Education Expenditure (% GDP)         4738 non-null   float64
6   Export (% GDP)                        4646 non-null   float64
7   GDP                                    5037 non-null   float64
8   Health Expenditure (% GDP)            4531 non-null   float64
9   Import (% GDP)                        4646 non-null   float64
10  Industry (% GDP)                      4853 non-null   float64
11  Inflation Rate                        4554 non-null   float64
12  R&D                                    3588 non-null   float64
13  Service (% GDP)                       4807 non-null   float64
14  Unemployment                          4439 non-null   float64
15  Population                            5106 non-null   float64
16  Land                                  5106 non-null   float64
17  Continent Name                        5106 non-null   object
18  Export                                4646 non-null   float64
19  Import                                4646 non-null   float64
20  Education Expenditure                 4692 non-null   float64
21  Health Expenditure                    4531 non-null   float64
22  Net Trade                             4646 non-null   float64
23  GDP Per Capita                        5037 non-null   float64
24  Population Density                    5106 non-null   float64
dtypes: float64(21), int64(1), object(3)
memory usage: 997.4+ KB

```

```
In [5]: df3.describe()
```

Out[5]:

	Year	Agriculture (% GDP)	Ease of Doing Business	Education Expenditure (% GDP)	Export (% GDP)	GDP	Health Expenditure (% GDP)	Import (% GDP)	Industry (% GDP)	Inflation Rate	...	Unemplo
count	5106.000000	4830.000000	4508.000000	4738.000000	4646.000000	5.037000e+03	4531.000000	4646.000000	4853.000000	4554.000000	...	4439.0
mean	2011.000000	10.893914	61.738665	14.458547	44.018003	3.120245e+11	6.167133	49.445204	26.315490	6.991400	...	8.7
std	6.633899	10.971965	13.775267	4.984259	33.173984	1.405946e+12	2.744570	30.474001	12.924200	19.858123	...	5.8
min	2000.000000	0.012519	19.977700	0.833360	1.571162	1.396473e+07	1.263576	1.127672	2.758632	-16.859691	...	0.0
25%	2005.000000	2.275972	52.919894	10.870940	23.544736	4.186073e+09	4.158750	29.401814	17.919508	1.599237	...	3.8
50%	2011.000000	6.979923	61.982110	13.952830	36.438987	1.777477e+10	5.639608	42.543697	24.119251	3.466447	...	6.9
75%	2017.000000	16.748657	72.535918	17.609406	54.543771	1.216041e+11	7.865923	60.600202	31.812769	7.288914	...	10.8
max	2022.000000	79.042362	87.166330	44.801800	433.836004	2.546270e+13	24.230680	429.359095	86.669555	557.201817	...	37.9

8 rows × 22 columns



```
In [6]: df3.isnull().sum()
```



Out[6]:

	0
Country Name	0
Country Code	0
Year	0
Agriculture (% GDP)	276
Ease of Doing Business	598
Education Expenditure (% GDP)	368
Export (% GDP)	460
GDP	69
Health Expenditure (% GDP)	575
Import (% GDP)	460
Industry (% GDP)	253
Inflation Rate	552
R&D	1518
Service (% GDP)	299
Unemployment	667
Population	0
Land	0
Continent Name	0
Export	460
Import	460
Education Expenditure	414
Health Expenditure	575
Net Trade	460
GDP Per Capita	69

	0
<b>Population Density</b>	0

**dtype:** int64

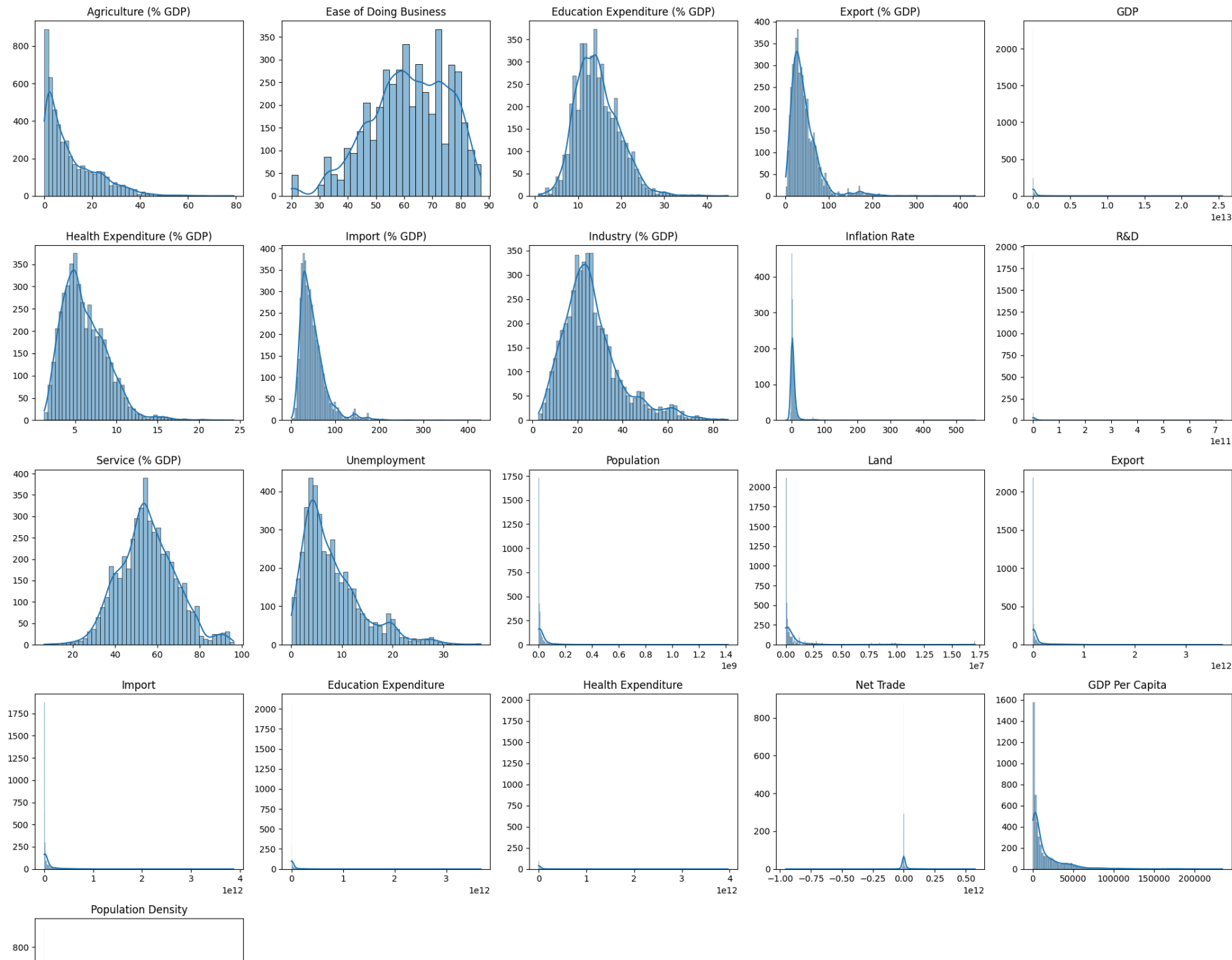
```
In [7]: # List of numerical columns
numerical_columns = [
    'Agriculture (% GDP)', 'Ease of Doing Business', 'Education Expenditure (% GDP)',
    'Export (% GDP)', 'GDP', 'Health Expenditure (% GDP)', 'Import (% GDP)',
    'Industry (% GDP)', 'Inflation Rate', 'R&D', 'Service (% GDP)', 'Unemployment',
    'Population', 'Land', 'Export', 'Import', 'Education Expenditure',
    'Health Expenditure', 'Net Trade', 'GDP Per Capita', 'Population Density'
]

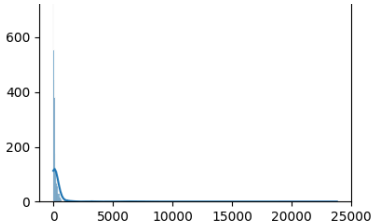
# Plot histograms for each numerical column
plt.figure(figsize=(20, 18))
for i, col in enumerate(numerical_columns, 1):
    plt.subplot(5, 5, i)
    sns.histplot(df3[col].dropna(), kde=True)
    plt.title(col)
    plt.xlabel('')
    plt.ylabel('')

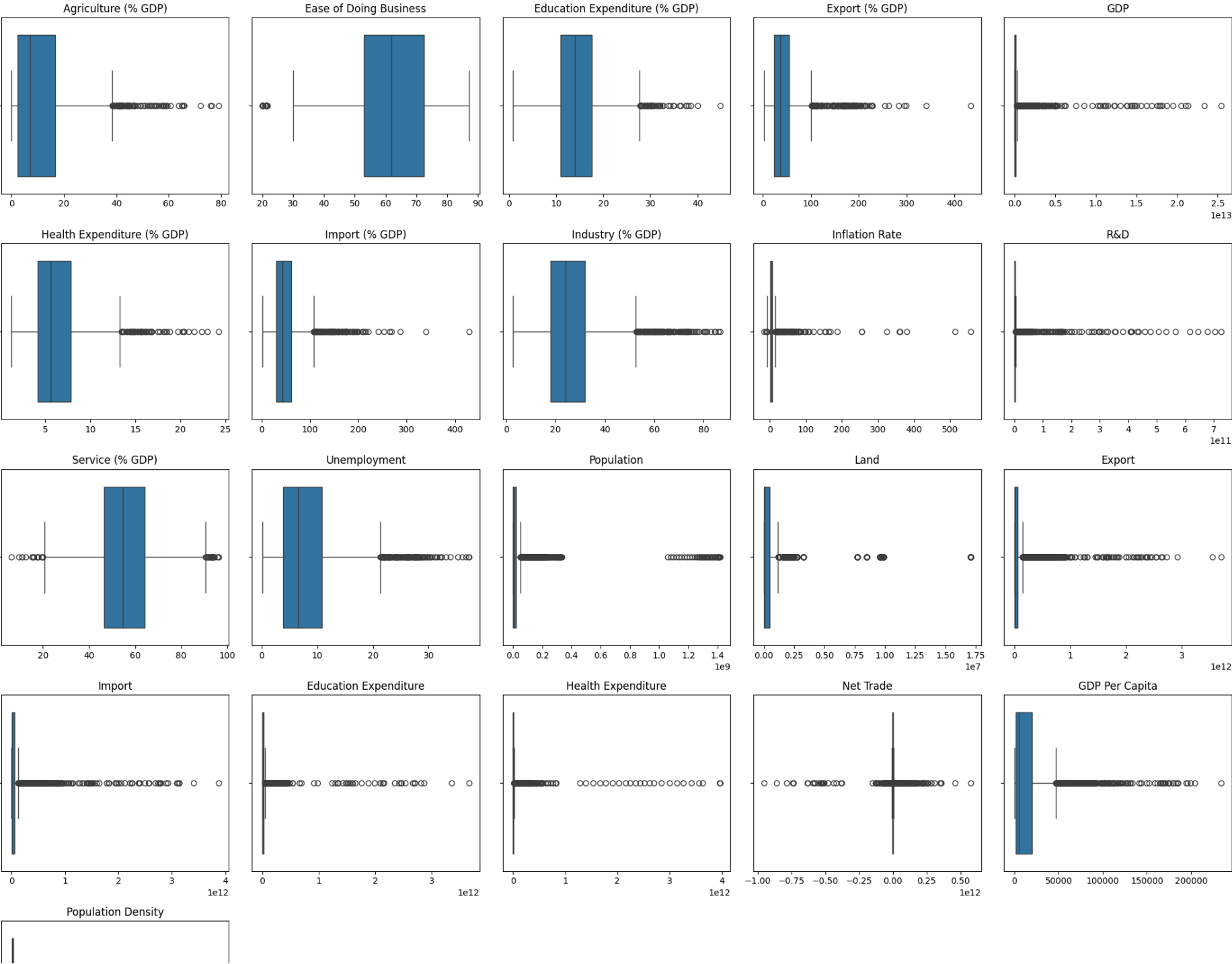
plt.tight_layout()
plt.show()

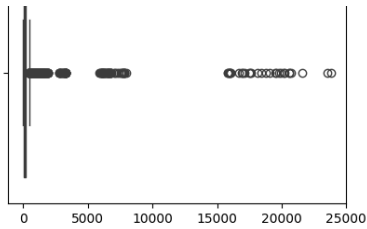
# Plot boxplots for each numerical column to check for outliers
plt.figure(figsize=(20, 18))
for i, col in enumerate(numerical_columns, 1):
    plt.subplot(5, 5, i)
    sns.boxplot(x=df3[col].dropna())
    plt.title(col)
    plt.xlabel('')

plt.tight_layout()
plt.show()
```







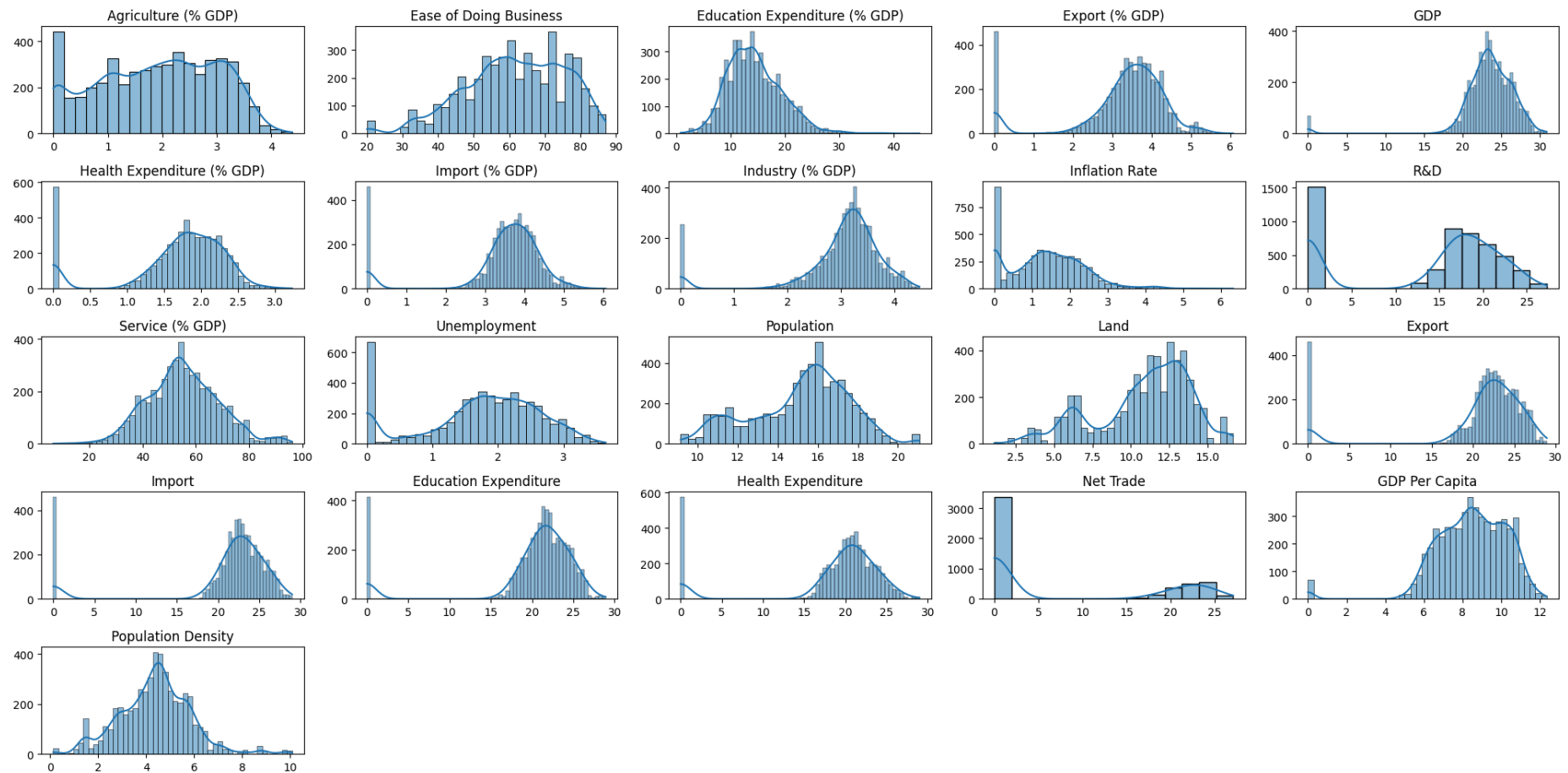


```
In [8]: # Calculate skewness
skewness = df3[numerical_columns].skew()

# Transformations to reduce skewness
# Apply log transformation for highly skewed data
for col in skewness[abs(skewness) > 1].index:
    df3[col] = df3[col].apply(lambda x: np.log(x + 1) if x > 0 else 0)

# Check the distribution after transformation
plt.figure(figsize=(20, 10))
for i, col in enumerate(numerical_columns, 1):
    plt.subplot(5, 5, i)
    sns.histplot(df3[col], kde=True)
    plt.title(col)
    plt.xlabel('')
    plt.ylabel('')

plt.tight_layout()
plt.show()
```



```
In [9]: # Using median for imputation
median_values = {
    'Agriculture (% GDP)': df3['Agriculture (% GDP)'].median(),
    'Ease of Doing Business': df3['Ease of Doing Business'].median(),
    'Education Expenditure (% GDP)': df3['Education Expenditure (% GDP)'].median(),
    'Export (% GDP)': df3['Export (% GDP)'].median(),
    'Health Expenditure (% GDP)': df3['Health Expenditure (% GDP)'].median(),
    'Import (% GDP)': df3['Import (% GDP)'].median(),
    'Industry (% GDP)': df3['Industry (% GDP)'].median(),
    'Inflation Rate': df3['Inflation Rate'].median(),
    'R&D': df3['R&D'].median(),
    'Service (% GDP)': df3['Service (% GDP)'].median(),
    'Unemployment': df3['Unemployment'].median(),
    'Net Trade': df3['Net Trade'].median(),
}
```

```

}
df3.fillna(median_values, inplace=True)

# Columns with smaller amounts of missing data can be imputed with forward fill or backward fill
df3.fillna(method='ffill', inplace=True) # Forward fill
df3.fillna(method='bfill', inplace=True) # Backward fill

# Check if all missing values are handled
missing_values_post = df3.isnull().sum()
print(missing_values_post)

```

```

Country Name      0
Country Code      0
Year              0
Agriculture (% GDP)  0
Ease of Doing Business  0
Education Expenditure (% GDP)  0
Export (% GDP)     0
GDP                0
Health Expenditure (% GDP)  0
Import (% GDP)     0
Industry (% GDP)   0
Inflation Rate     0
R&D                0
Service (% GDP)    0
Unemployment       0
Population         0
Land               0
Continent Name     0
Export             0
Import             0
Education Expenditure  0
Health Expenditure  0
Net Trade          0
GDP Per Capita     0
Population Density  0
dtype: int64

```

```

<ipython-input-9-75d43282897e>:19: FutureWarning: DataFrame.fillna with 'method' is deprecated and will raise in a future version. Use obj.ffill() or obj.bfill() instead.

```

```

    df3.fillna(method='ffill', inplace=True) # Forward fill

```

```

<ipython-input-9-75d43282897e>:20: FutureWarning: DataFrame.fillna with 'method' is deprecated and will raise in a future version. Use obj.ffill() or obj.bfill() instead.

```

```

    df3.fillna(method='bfill', inplace=True) # Backward fill

```



```

In [10]: # List of numerical columns
numerical_columns = [
    'Agriculture (% GDP)', 'Ease of Doing Business', 'Education Expenditure (% GDP)',
    'Export (% GDP)', 'GDP', 'Health Expenditure (% GDP)', 'Import (% GDP)',
    'Industry (% GDP)', 'Inflation Rate', 'R&D', 'Service (% GDP)', 'Unemployment',
    'Population', 'Land', 'Export', 'Import', 'Education Expenditure',
    'Health Expenditure', 'Net Trade', 'GDP Per Capita', 'Population Density'
]

# Function to identify outliers using IQR
def identify_outliers(df, col):
    Q1 = df[col].quantile(0.25)
    Q3 = df[col].quantile(0.75)
    IQR = Q3 - Q1
    lower_bound = Q1 - 1.5 * IQR
    upper_bound = Q3 + 1.5 * IQR
    return df[(df[col] < lower_bound) | (df[col] > upper_bound)]

from scipy import stats

# Function to identify outliers using Z-Score
def identify_outliers_zscore(df, col):
    z_scores = np.abs(stats.zscore(df[col].dropna()))
    return df[z_scores > 3]

# Function to handle outliers using Z-Score
def handle_outliers_zscore(df, col):
    z_scores = np.abs(stats.zscore(df[col].dropna()))
    df[col] = np.where(z_scores > 3, df[col].median(), df[col])

# Identify and count outliers for each column before handling
outliers_info_before_z = {}
for col in numerical_columns:
    outliers = identify_outliers_zscore(df3, col)
    outliers_info_before_z[col] = len(outliers)

# Print number of outliers for each column before handling
print("Number of outliers in each column before Z-Score handling:")
for col, count in outliers_info_before_z.items():
    print(f"{col}: {count} outliers")

# Handle outliers using Z-Score
for col in numerical_columns:

```

```
    handle_outliers_zscore(df3, col)

# Identify and count outliers for each column after handling
outliers_info_after_z = {}
for col in numerical_columns:
    outliers = identify_outliers_zscore(df3, col)
    outliers_info_after_z[col] = len(outliers)

# Print number of outliers for each column after handling
print("\nNumber of outliers in each column after Z-Score handling:")
for col, count in outliers_info_after_z.items():
    print(f"{col}: {count} outliers")
```

Number of outliers in each column before Z-Score handling:

Agriculture (% GDP): 0 outliers  
Ease of Doing Business: 46 outliers  
Education Expenditure (% GDP): 43 outliers  
Export (% GDP): 0 outliers  
GDP: 69 outliers  
Health Expenditure (% GDP): 0 outliers  
Import (% GDP): 0 outliers  
Industry (% GDP): 253 outliers  
Inflation Rate: 34 outliers  
R&D: 0 outliers  
Service (% GDP): 14 outliers  
Unemployment: 0 outliers  
Population: 0 outliers  
Land: 7 outliers  
Export: 460 outliers  
Import: 460 outliers  
Education Expenditure: 414 outliers  
Health Expenditure: 0 outliers  
Net Trade: 0 outliers  
GDP Per Capita: 69 outliers  
Population Density: 53 outliers

Number of outliers in each column after Z-Score handling:

Agriculture (% GDP): 0 outliers  
Ease of Doing Business: 0 outliers  
Education Expenditure (% GDP): 14 outliers  
Export (% GDP): 0 outliers  
GDP: 2 outliers  
Health Expenditure (% GDP): 0 outliers  
Import (% GDP): 0 outliers  
Industry (% GDP): 29 outliers  
Inflation Rate: 27 outliers  
R&D: 0 outliers  
Service (% GDP): 4 outliers  
Unemployment: 0 outliers  
Population: 0 outliers  
Land: 0 outliers  
Export: 1 outliers  
Import: 1 outliers  
Education Expenditure: 2 outliers  
Health Expenditure: 0 outliers  
Net Trade: 0 outliers

GDP Per Capita: 0 outliers  
Population Density: 46 outliers

```
In [11]: import pandas as pd
from sklearn.preprocessing import MinMaxScaler
# Drop irrelevant columns
df3 = df3.drop(columns=['Continent Name', 'Country Code'])

# One-hot encode the 'Country Name' column
df_encoded = pd.get_dummies(df3, columns=['Country Name'])

# Identify numeric columns for normalization
numeric_cols = df_encoded.select_dtypes(include=['float64', 'int64']).columns

# Exclude columns that should not be normalized
cols_to_normalize = numeric_cols.difference(['Year', 'GDP', 'GDP Per Capita'])

# Initialize MinMaxScaler
scaler = MinMaxScaler()

# Normalize selected columns
df_encoded[cols_to_normalize] = scaler.fit_transform(df_encoded[cols_to_normalize])

# Split the dataset into features and labels
X = df_encoded.drop(columns=['GDP', 'GDP Per Capita'])
y_gdp = df_encoded['GDP']
y_gdp_per_capita = df_encoded['GDP Per Capita']

# Optional: Display the first few rows of the processed dataset
print(X.head())
print(y_gdp.head())
print(y_gdp_per_capita.head())
```

Year	Agriculture (% GDP)	Ease of Doing Business	\		
0 2000	0.764381		0.186992		
1 2001	0.764381		0.186992		
2 2002	0.839586		0.186992		
3 2003	0.832516		0.186992		
4 2004	0.781496		0.186992		
	Education Expenditure (% GDP)	Export (% GDP)	Health Expenditure (% GDP)	\	
0	0.460627	0.0	0.767258		
1	0.460627	0.0	0.767258		
2	0.460627	0.0	0.726743		
3	0.460627	0.0	0.711478		
4	0.460627	0.0	0.737387		
	Import (% GDP)	Industry (% GDP)	Inflation Rate	R&D	... \
0	0.0	0.553659	0.456583	0.0	...
1	0.0	0.553659	0.456583	0.0	...
2	0.0	0.599201	0.456583	0.0	...
3	0.0	0.584812	0.456583	0.0	...
4	0.0	0.628714	0.456583	0.0	...
	Country Name_Uruguay	Country Name_Uzbekistan	Country Name_Vanuatu	\	
0	False	False	False		
1	False	False	False		
2	False	False	False		
3	False	False	False		
4	False	False	False		
	Country Name_Venezuela, RB	Country Name_Vietnam	\		
0	False	False			
1	False	False			
2	False	False			
3	False	False			
4	False	False			
	Country Name_Virgin Islands (U.S.)	Country Name_West Bank and Gaza	\		
0	False	False			
1	False	False			
2	False	False			
3	False	False			
4	False	False			
	Country Name_Yemen, Rep.	Country Name_Zambia	Country Name_Zimbabwe		
0	False	False	False		

1	False	False	False
2	False	False	False
3	False	False	False
4	False	False	False

[5 rows x 235 columns]

```
0    23.373120
1    23.373120
2    22.072438
3    22.236082
4    22.375921
```

Name: GDP, dtype: float64

```
0    6.586373
1    6.578958
2    5.217827
3    5.305603
4    5.405635
```

Name: GDP Per Capita, dtype: float64

```
In [12]: # Ensure features are a numpy array
X_np = np.array(X)
```

```
In [13]: import seaborn as sns
from sklearn.preprocessing import MinMaxScaler
from sklearn.model_selection import train_test_split
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, LSTM, Dropout
from tensorflow.keras.optimizers import Adam

# To ignore warnings
import warnings
warnings.filterwarnings("ignore")
```

```
In [14]: # Reshape the features for LSTM
X_lstm = np.reshape(X_np, (X.shape[0], X.shape[1], 1)).astype('float32') # Convert to float32

# Split data into training and testing
X_train, X_test, y_train, y_test = train_test_split(X_lstm, y_gdp.astype('float32'), test_size=0.2, random_state=42) # Convert y_


# Building the LSTM Model
model_gdp = Sequential()
model_gdp.add(LSTM(50, return_sequences=True, input_shape=(X_train.shape[1], 1)))
model_gdp.add(Dropout(0.2))
```


```
model_gdp.add(LSTM(50, return_sequences=False))
model_gdp.add(Dropout(0.2))
model_gdp.add(Dense(25))
model_gdp.add(Dense(1))


# Compile the model
model_gdp.compile(optimizer=Adam(learning_rate=0.001), loss='mean_squared_error')


# Train the model
model_gdp.fit(X_train, y_train, batch_size=32, epochs=500)


# Predicting GDP
pred_gdp = model_gdp.predict(X_test)
```


Epoch 1/500  
**128/128**  6s 16ms/step - loss: 247.3952


Epoch 2/500  
**128/128**  2s 18ms/step - loss: 9.2256


Epoch 3/500  
**128/128**  3s 18ms/step - loss: 8.7127


Epoch 4/500  
**128/128**  2s 15ms/step - loss: 9.2279


Epoch 5/500  
**128/128**  3s 15ms/step - loss: 8.9232


Epoch 6/500  
**128/128**  3s 15ms/step - loss: 8.8850


Epoch 7/500  
**128/128**  3s 17ms/step - loss: 8.8823


Epoch 8/500  
**128/128**  4s 25ms/step - loss: 8.0734


Epoch 9/500  
**128/128**  2s 15ms/step - loss: 8.9588


Epoch 10/500  
**128/128**  3s 15ms/step - loss: 8.8221


Epoch 11/500  
**128/128**  3s 15ms/step - loss: 8.3923


Epoch 12/500  
**128/128**  3s 17ms/step - loss: 8.4267


Epoch 13/500  
**128/128**  3s 19ms/step - loss: 8.5771


Epoch 14/500  
**128/128**  2s 18ms/step - loss: 8.7594


Epoch 15/500  
**128/128**  3s 18ms/step - loss: 8.1593


Epoch 16/500  
**128/128**  2s 17ms/step - loss: 8.6375


Epoch 17/500  
**128/128**  5s 34ms/step - loss: 8.4753

Epoch 18/500  
**128/128**  3s 23ms/step - loss: 8.5389


Epoch 19/500  
**128/128**  2s 18ms/step - loss: 8.5458


Epoch 20/500  
**128/128**  2s 17ms/step - loss: 8.2659


Epoch 21/500  
**128/128**  3s 24ms/step - loss: 8.1026


Epoch 22/500  
**128/128**  5s 20ms/step - loss: 8.4744





Epoch 23/500  
**128/128**  2s 15ms/step - loss: 8.2691


Epoch 24/500  
**128/128**  3s 15ms/step - loss: 8.5246


Epoch 25/500  
**128/128**  2s 15ms/step - loss: 8.3761


Epoch 26/500  
**128/128**  3s 21ms/step - loss: 8.0406


Epoch 27/500  
**128/128**  2s 16ms/step - loss: 7.9377


Epoch 28/500  
**128/128**  2s 15ms/step - loss: 7.8197


Epoch 29/500  
**128/128**  2s 15ms/step - loss: 7.8194


Epoch 30/500  
**128/128**  2s 15ms/step - loss: 8.4309


Epoch 31/500  
**128/128**  3s 16ms/step - loss: 7.7442


Epoch 32/500  
**128/128**  3s 20ms/step - loss: 8.1259


Epoch 33/500  
**128/128**  5s 16ms/step - loss: 7.8281

Epoch 34/500  
**128/128**  2s 15ms/step - loss: 8.0249

Epoch 35/500  
**128/128**  3s 15ms/step - loss: 7.7735


Epoch 36/500  
**128/128**  3s 22ms/step - loss: 8.2193


Epoch 37/500  
**128/128**  2s 15ms/step - loss: 7.9213

Epoch 38/500  
**128/128**  2s 15ms/step - loss: 7.8296


Epoch 39/500  
**128/128**  2s 15ms/step - loss: 7.8206























Epoch 40/500  
**128/128**  2s 15ms/step - loss: 7.5482























Epoch 41/500  
**128/128**  2s 16ms/step - loss: 7.8795

Epoch 42/500  
**128/128**  3s 21ms/step - loss: 7.6330

Epoch 43/500  
**128/128**  4s 16ms/step - loss: 7.5068

Epoch 44/500  
**128/128**  2s 15ms/step - loss: 7.6622

Epoch 45/500  
**128/128**  2s 15ms/step - loss: 7.4096  
Epoch 46/500  
**128/128**  2s 18ms/step - loss: 7.3548  
Epoch 47/500  
**128/128**  3s 20ms/step - loss: 7.4440  
Epoch 48/500  
**128/128**  2s 15ms/step - loss: 7.4263  
Epoch 49/500  
**128/128**  3s 15ms/step - loss: 7.3942  
Epoch 50/500  
**128/128**  3s 15ms/step - loss: 7.0874  
Epoch 51/500  
**128/128**  2s 15ms/step - loss: 7.3641  
Epoch 52/500  
**128/128**  3s 20ms/step - loss: 6.9077  
Epoch 53/500  
**128/128**  2s 17ms/step - loss: 6.9507  
Epoch 54/500  
**128/128**  2s 15ms/step - loss: 6.9826  
Epoch 55/500  
**128/128**  3s 15ms/step - loss: 7.1061  
Epoch 56/500  
**128/128**  3s 19ms/step - loss: 7.3396  
Epoch 57/500  
**128/128**  3s 20ms/step - loss: 6.8923  
Epoch 58/500  
**128/128**  5s 16ms/step - loss: 6.9270  
Epoch 59/500  
**128/128**  2s 15ms/step - loss: 6.8454  
Epoch 60/500  
**128/128**  3s 15ms/step - loss: 6.7574  
Epoch 61/500  
**128/128**  2s 18ms/step - loss: 7.1090  
Epoch 62/500  
**128/128**  3s 19ms/step - loss: 6.9041  
Epoch 63/500  
**128/128**  2s 15ms/step - loss: 6.4952  
Epoch 64/500  
**128/128**  3s 15ms/step - loss: 6.6987  
Epoch 65/500  
**128/128**  2s 15ms/step - loss: 6.8577  
Epoch 66/500  
**128/128**  3s 15ms/step - loss: 6.5151

Epoch 67/500  
**128/128**  3s 21ms/step - loss: 6.5754  
Epoch 68/500  
**128/128**  2s 15ms/step - loss: 6.4001  
Epoch 69/500  
**128/128**  3s 19ms/step - loss: 6.4457  
Epoch 70/500  
**128/128**  2s 15ms/step - loss: 6.5381  
Epoch 71/500  
**128/128**  3s 15ms/step - loss: 6.5283  
Epoch 72/500  
**128/128**  3s 22ms/step - loss: 6.4241  
Epoch 73/500  
**128/128**  4s 16ms/step - loss: 6.0843  
Epoch 74/500  
**128/128**  2s 15ms/step - loss: 6.3223  
Epoch 75/500  
**128/128**  2s 15ms/step - loss: 6.4547  
Epoch 76/500  
**128/128**  3s 18ms/step - loss: 6.2727  
Epoch 77/500  
**128/128**  2s 19ms/step - loss: 6.4767  
Epoch 78/500  
**128/128**  2s 15ms/step - loss: 6.4941  
Epoch 79/500  
**128/128**  2s 15ms/step - loss: 6.2451  
Epoch 80/500  
**128/128**  2s 15ms/step - loss: 6.0320  
Epoch 81/500  
**128/128**  3s 16ms/step - loss: 6.3162  
Epoch 82/500  
**128/128**  3s 20ms/step - loss: 6.2849  
Epoch 83/500  
**128/128**  2s 17ms/step - loss: 6.3094  
Epoch 84/500  
**128/128**  2s 15ms/step - loss: 6.3142  
Epoch 85/500  
**128/128**  3s 15ms/step - loss: 5.9949  
Epoch 86/500  
**128/128**  2s 15ms/step - loss: 6.0751  
Epoch 87/500  
**128/128**  2s 15ms/step - loss: 6.1884  
Epoch 88/500  
**128/128**  3s 22ms/step - loss: 6.0339

Epoch 89/500  
**128/128**  4s 17ms/step - loss: 5.8235

Epoch 90/500  
**128/128**  2s 15ms/step - loss: 6.0537

Epoch 91/500  
**128/128**  2s 15ms/step - loss: 5.9937

Epoch 92/500  
**128/128**  3s 19ms/step - loss: 6.3718

Epoch 93/500  
**128/128**  2s 19ms/step - loss: 5.9809

Epoch 94/500  
**128/128**  2s 15ms/step - loss: 5.7018

Epoch 95/500  
**128/128**  2s 15ms/step - loss: 5.9216

Epoch 96/500  
**128/128**  2s 15ms/step - loss: 6.1651

Epoch 97/500  
**128/128**  2s 15ms/step - loss: 5.9241


Epoch 98/500  
**128/128**  2s 19ms/step - loss: 5.9818

Epoch 99/500  
**128/128**  2s 19ms/step - loss: 5.8953

Epoch 100/500  
**128/128**  2s 16ms/step - loss: 5.9666

Epoch 101/500  
**128/128**  3s 15ms/step - loss: 5.8021

Epoch 102/500  
**128/128**  3s 15ms/step - loss: 5.7929

Epoch 103/500  
**128/128**  2s 16ms/step - loss: 5.7702

Epoch 104/500  
**128/128**  3s 21ms/step - loss: 5.8305

Epoch 105/500  
**128/128**  2s 15ms/step - loss: 5.9620























Epoch 106/500  
**128/128**  2s 15ms/step - loss: 5.8931























Epoch 107/500  
**128/128**  3s 15ms/step - loss: 5.9306


Epoch 108/500  
**128/128**  2s 15ms/step - loss: 5.7494


Epoch 109/500  
**128/128**  3s 20ms/step - loss: 5.7913


Epoch 110/500  
**128/128**  2s 18ms/step - loss: 5.6870

Epoch 111/500  
**128/128**  2s 15ms/step - loss: 5.1610  
Epoch 112/500  
**128/128**  3s 15ms/step - loss: 2.0513  
Epoch 113/500  
**128/128**  3s 16ms/step - loss: 1.3885  
Epoch 114/500  
**128/128**  2s 16ms/step - loss: 1.4495  
Epoch 115/500  
**128/128**  3s 22ms/step - loss: 1.4570  
Epoch 116/500  
**128/128**  2s 15ms/step - loss: 0.9684  
Epoch 117/500  
**128/128**  2s 15ms/step - loss: 1.0942  
Epoch 118/500  
**128/128**  3s 15ms/step - loss: 0.9170  
Epoch 119/500  
**128/128**  2s 15ms/step - loss: 0.9143  
Epoch 120/500  
**128/128**  2s 18ms/step - loss: 1.2692  
Epoch 121/500  
**128/128**  3s 20ms/step - loss: 1.0012  
Epoch 122/500  
**128/128**  5s 16ms/step - loss: 1.1030  
Epoch 123/500  
**128/128**  2s 15ms/step - loss: 1.3179  
Epoch 124/500  
**128/128**  2s 15ms/step - loss: 1.0048  
Epoch 125/500  
**128/128**  3s 20ms/step - loss: 0.7350  
Epoch 126/500  
**128/128**  2s 17ms/step - loss: 0.6992  
Epoch 127/500  
**128/128**  2s 15ms/step - loss: 0.6867  
Epoch 128/500  
**128/128**  3s 15ms/step - loss: 0.6654  
Epoch 129/500  
**128/128**  3s 15ms/step - loss: 0.8890  
Epoch 130/500  
**128/128**  2s 17ms/step - loss: 0.8227  
Epoch 131/500  
**128/128**  3s 20ms/step - loss: 0.7960  
Epoch 132/500  
**128/128**  5s 16ms/step - loss: 0.8292


Epoch 133/500  
**128/128**  2s 15ms/step - loss: 0.6337  
Epoch 134/500  
**128/128**  2s 15ms/step - loss: 0.6284  
Epoch 135/500  
**128/128**  2s 17ms/step - loss: 0.7096  
Epoch 136/500  
**128/128**  3s 20ms/step - loss: 0.5391  
Epoch 137/500  
**128/128**  2s 15ms/step - loss: 0.6609  
Epoch 138/500  
**128/128**  2s 15ms/step - loss: 0.5487  
Epoch 139/500  
**128/128**  2s 15ms/step - loss: 0.6801  
Epoch 140/500  
**128/128**  2s 15ms/step - loss: 0.8296  
Epoch 141/500  
**128/128**  2s 17ms/step - loss: 0.8403  
Epoch 142/500  
**128/128**  3s 20ms/step - loss: 0.5187  
Epoch 143/500  
**128/128**  2s 15ms/step - loss: 1.4689  
Epoch 144/500  
**128/128**  2s 15ms/step - loss: 0.5767  
Epoch 145/500  
**128/128**  3s 15ms/step - loss: 0.5224  
Epoch 146/500  
**128/128**  3s 16ms/step - loss: 0.4421  
Epoch 147/500  
**128/128**  3s 21ms/step - loss: 0.4864  
Epoch 148/500  
**128/128**  5s 16ms/step - loss: 0.4780  
Epoch 149/500  
**128/128**  2s 15ms/step - loss: 0.8829  
Epoch 150/500  
**128/128**  3s 15ms/step - loss: 2.2255  
Epoch 151/500  
**128/128**  3s 20ms/step - loss: 0.4465  
Epoch 152/500  
**128/128**  2s 18ms/step - loss: 0.4805  
Epoch 153/500  
**128/128**  2s 15ms/step - loss: 0.9332  
Epoch 154/500  
**128/128**  3s 15ms/step - loss: 0.5483


Epoch 155/500  
**128/128**  2s 15ms/step - loss: 0.5712


Epoch 156/500  
**128/128**  3s 17ms/step - loss: 0.4057


Epoch 157/500  
**128/128**  3s 20ms/step - loss: 0.4269


Epoch 158/500  
**128/128**  2s 15ms/step - loss: 0.3892


Epoch 159/500  
**128/128**  2s 15ms/step - loss: 0.3904


Epoch 160/500  
**128/128**  3s 15ms/step - loss: 0.4600


Epoch 161/500  
**128/128**  3s 15ms/step - loss: 0.3522


Epoch 162/500  
**128/128**  3s 21ms/step - loss: 0.5979


Epoch 163/500  
**128/128**  5s 17ms/step - loss: 4.7109


Epoch 164/500  
**128/128**  2s 16ms/step - loss: 0.7212


Epoch 165/500  
**128/128**  2s 15ms/step - loss: 0.5770


Epoch 166/500  
**128/128**  2s 16ms/step - loss: 0.4874


Epoch 167/500  
**128/128**  3s 21ms/step - loss: 0.4519


Epoch 168/500  
**128/128**  2s 15ms/step - loss: 0.4520

Epoch 169/500  
**128/128**  2s 15ms/step - loss: 0.4770

Epoch 170/500  
**128/128**  2s 16ms/step - loss: 0.4024


Epoch 171/500  
**128/128**  3s 15ms/step - loss: 0.3816


Epoch 172/500  
**128/128**  3s 19ms/step - loss: 0.3607

Epoch 173/500  
**128/128**  2s 19ms/step - loss: 0.3557























Epoch 174/500  
**128/128**  2s 15ms/step - loss: 0.3654

Epoch 175/500  
**128/128**  2s 15ms/step - loss: 0.3367

Epoch 176/500  
**128/128**  3s 16ms/step - loss: 0.3259

Epoch 177/500  
**128/128**  3s 16ms/step - loss: 0.3503  
Epoch 178/500  
**128/128**  3s 22ms/step - loss: 0.4251  
Epoch 179/500  
**128/128**  4s 16ms/step - loss: 0.3659  
Epoch 180/500  
**128/128**  2s 15ms/step - loss: 0.4946  
Epoch 181/500  
**128/128**  2s 15ms/step - loss: 0.3523  
Epoch 182/500  
**128/128**  2s 17ms/step - loss: 0.3981  
Epoch 183/500  
**128/128**  3s 21ms/step - loss: 0.3205  
Epoch 184/500  
**128/128**  5s 16ms/step - loss: 0.3764  
Epoch 185/500  
**128/128**  2s 15ms/step - loss: 0.3310  
Epoch 186/500  
**128/128**  3s 15ms/step - loss: 0.2923  
Epoch 187/500  
**128/128**  3s 21ms/step - loss: 0.3115  
Epoch 188/500  
**128/128**  5s 16ms/step - loss: 0.3223  
Epoch 189/500  
**128/128**  2s 15ms/step - loss: 0.2894  
Epoch 190/500  
**128/128**  2s 15ms/step - loss: 0.3301  
Epoch 191/500  
**128/128**  3s 21ms/step - loss: 0.2706  
Epoch 192/500  
**128/128**  2s 16ms/step - loss: 0.2777  
Epoch 193/500  
**128/128**  2s 16ms/step - loss: 0.5085  
Epoch 194/500  
**128/128**  2s 15ms/step - loss: 0.2466  
Epoch 195/500  
**128/128**  2s 15ms/step - loss: 0.2453  
Epoch 196/500  
**128/128**  3s 16ms/step - loss: 0.2750  
Epoch 197/500  
**128/128**  3s 20ms/step - loss: 0.2317  
Epoch 198/500  
**128/128**  2s 15ms/step - loss: 0.2768




Epoch 199/500  
**128/128**  2s 15ms/step - loss: 0.2254  
Epoch 200/500  
**128/128**  3s 16ms/step - loss: 0.3441  
Epoch 201/500  
**128/128**  2s 15ms/step - loss: 0.2810  
Epoch 202/500  
**128/128**  3s 21ms/step - loss: 0.2543  
Epoch 203/500  
**128/128**  2s 15ms/step - loss: 0.2755  
Epoch 204/500  
**128/128**  3s 15ms/step - loss: 1.8659  
Epoch 205/500  
**128/128**  3s 16ms/step - loss: 0.3069  
Epoch 206/500  
**128/128**  2s 15ms/step - loss: 0.2313  
Epoch 207/500  
**128/128**  3s 20ms/step - loss: 0.3071  
Epoch 208/500  
**128/128**  2s 17ms/step - loss: 0.2141  
Epoch 209/500  
**128/128**  2s 15ms/step - loss: 0.2417  
Epoch 210/500  
**128/128**  2s 16ms/step - loss: 0.2879  
Epoch 211/500  
**128/128**  2s 16ms/step - loss: 0.2166  
Epoch 212/500  
**128/128**  2s 16ms/step - loss: 0.2696  
Epoch 213/500  
**128/128**  3s 21ms/step - loss: 0.2087  
Epoch 214/500  
**128/128**  2s 18ms/step - loss: 2.3168  
Epoch 215/500  
**128/128**  2s 16ms/step - loss: 0.2956  
Epoch 216/500  
**128/128**  2s 16ms/step - loss: 0.2767  
Epoch 217/500  
**128/128**  3s 15ms/step - loss: 0.2294  
Epoch 218/500  
**128/128**  3s 17ms/step - loss: 0.2534  
Epoch 219/500  
**128/128**  3s 21ms/step - loss: 0.2118  
Epoch 220/500  
**128/128**  5s 16ms/step - loss: 0.1910

Epoch 221/500  
**128/128**  2s 15ms/step - loss: 0.2223

Epoch 222/500  
**128/128**  2s 16ms/step - loss: 0.2106

Epoch 223/500  
**128/128**  3s 20ms/step - loss: 0.1994

Epoch 224/500  
**128/128**  2s 19ms/step - loss: 0.2883


Epoch 225/500  
**128/128**  2s 16ms/step - loss: 0.1985


Epoch 226/500  
**128/128**  3s 16ms/step - loss: 0.7087


Epoch 227/500  
**128/128**  2s 16ms/step - loss: 0.7216


Epoch 228/500  
**128/128**  2s 15ms/step - loss: 0.3582

Epoch 229/500  
**128/128**  3s 22ms/step - loss: 0.2885


Epoch 230/500  
**128/128**  4s 17ms/step - loss: 0.3033

Epoch 231/500  
**128/128**  2s 16ms/step - loss: 0.2793

Epoch 232/500  
**128/128**  2s 16ms/step - loss: 0.2871

Epoch 233/500  
**128/128**  3s 18ms/step - loss: 0.3209

Epoch 234/500  
**128/128**  3s 20ms/step - loss: 0.2637


Epoch 235/500  
**128/128**  2s 15ms/step - loss: 0.3171


Epoch 236/500  
**128/128**  2s 16ms/step - loss: 0.2791

Epoch 237/500  
**128/128**  2s 16ms/step - loss: 0.2764




















Epoch 238/500  
**128/128**  2s 16ms/step - loss: 0.2006























Epoch 239/500  
**128/128**  3s 20ms/step - loss: 0.2284



















Epoch 240/500  
**128/128**  5s 17ms/step - loss: 0.2068




















Epoch 241/500  
**128/128**  2s 15ms/step - loss: 0.1964







Epoch 242/500  
**128/128**  3s 15ms/step - loss: 0.2925


Epoch 243/500  
**128/128**  2s 19ms/step - loss: 0.2141  
Epoch 244/500  
**128/128**  2s 19ms/step - loss: 0.2255  
Epoch 245/500  
**128/128**  2s 16ms/step - loss: 0.1864  
Epoch 246/500  
**128/128**  3s 15ms/step - loss: 0.1811  
Epoch 247/500  
**128/128**  2s 15ms/step - loss: 0.1914  
Epoch 248/500  
**128/128**  3s 17ms/step - loss: 0.1779  
Epoch 249/500  
**128/128**  3s 20ms/step - loss: 0.2008  
Epoch 250/500  
**128/128**  2s 16ms/step - loss: 0.2364  
Epoch 251/500  
**128/128**  3s 16ms/step - loss: 0.2451  
Epoch 252/500  
**128/128**  2s 16ms/step - loss: 0.2433  
Epoch 253/500  
**128/128**  3s 16ms/step - loss: 0.1773  
Epoch 254/500  
**128/128**  3s 21ms/step - loss: 0.2410  
Epoch 255/500  
**128/128**  5s 17ms/step - loss: 0.2194  
Epoch 256/500  
**128/128**  2s 16ms/step - loss: 0.1612  
Epoch 257/500  
**128/128**  3s 16ms/step - loss: 0.1977  
Epoch 258/500  
**128/128**  3s 20ms/step - loss: 0.1680  
Epoch 259/500  
**128/128**  2s 18ms/step - loss: 0.1855  
Epoch 260/500  
**128/128**  2s 16ms/step - loss: 0.9854  
Epoch 261/500  
**128/128**  3s 16ms/step - loss: 0.1689  
Epoch 262/500  
**128/128**  2s 16ms/step - loss: 0.1570  
Epoch 263/500  
**128/128**  3s 17ms/step - loss: 0.1530  
Epoch 264/500  
**128/128**  3s 20ms/step - loss: 0.1320


Epoch 265/500  
**128/128**  5s 17ms/step - loss: 0.1310  
Epoch 266/500  
**128/128**  2s 16ms/step - loss: 0.1544  
Epoch 267/500  
**128/128**  3s 16ms/step - loss: 0.1409  
Epoch 268/500  
**128/128**  3s 21ms/step - loss: 0.1613  
Epoch 269/500  
**128/128**  5s 17ms/step - loss: 0.1503  
Epoch 270/500  
**128/128**  2s 16ms/step - loss: 0.1570  
Epoch 271/500  
**128/128**  2s 16ms/step - loss: 0.2128  
Epoch 272/500  
**128/128**  3s 21ms/step - loss: 0.1319  
Epoch 273/500  
**128/128**  5s 17ms/step - loss: 0.1525  
Epoch 274/500  
**128/128**  2s 15ms/step - loss: 0.1928  
Epoch 275/500  
**128/128**  3s 15ms/step - loss: 0.1589  
Epoch 276/500  
**128/128**  2s 19ms/step - loss: 0.1292  
Epoch 277/500  
**128/128**  3s 19ms/step - loss: 0.1819  
Epoch 278/500  
**128/128**  2s 16ms/step - loss: 5.3923  
Epoch 279/500  
**128/128**  2s 16ms/step - loss: 0.4050  
Epoch 280/500  
**128/128**  2s 15ms/step - loss: 0.3133  
Epoch 281/500  
**128/128**  2s 16ms/step - loss: 0.2962  
Epoch 282/500  
**128/128**  3s 22ms/step - loss: 0.2179  
Epoch 283/500  
**128/128**  2s 17ms/step - loss: 0.2218  
Epoch 284/500  
**128/128**  2s 16ms/step - loss: 0.2255  
Epoch 285/500  
**128/128**  3s 16ms/step - loss: 0.1798  
Epoch 286/500  
**128/128**  2s 16ms/step - loss: 0.1831


Epoch 287/500  
**128/128**  3s 19ms/step - loss: 0.1623  
Epoch 288/500  
**128/128**  2s 19ms/step - loss: 0.2101  
Epoch 289/500  
**128/128**  2s 16ms/step - loss: 0.1507  
Epoch 290/500  
**128/128**  2s 16ms/step - loss: 0.1995  
Epoch 291/500  
**128/128**  3s 16ms/step - loss: 0.1562  
Epoch 292/500  
**128/128**  2s 16ms/step - loss: 0.1680  
Epoch 293/500  
**128/128**  3s 21ms/step - loss: 0.2162  
Epoch 294/500  
**128/128**  5s 17ms/step - loss: 0.1513  
Epoch 295/500  
**128/128**  2s 16ms/step - loss: 0.1880  
Epoch 296/500  
**128/128**  3s 16ms/step - loss: 0.2669  
Epoch 297/500  
**128/128**  4s 23ms/step - loss: 0.1419  
Epoch 298/500  
**128/128**  2s 16ms/step - loss: 0.1424  
Epoch 299/500  
**128/128**  3s 16ms/step - loss: 0.1493  
Epoch 300/500  
**128/128**  3s 15ms/step - loss: 0.1665  
Epoch 301/500  
**128/128**  2s 16ms/step - loss: 0.1811  
Epoch 302/500  
**128/128**  3s 21ms/step - loss: 0.1903  
Epoch 303/500  
**128/128**  4s 16ms/step - loss: 0.1631  
Epoch 304/500  
**128/128**  2s 16ms/step - loss: 0.3680  
Epoch 305/500  
**128/128**  2s 16ms/step - loss: 0.2080  
Epoch 306/500  
**128/128**  2s 16ms/step - loss: 0.1444  
Epoch 307/500  
**128/128**  3s 22ms/step - loss: 0.1900  
Epoch 308/500  
**128/128**  4s 17ms/step - loss: 0.1617


Epoch 309/500  
**128/128**  2s 16ms/step - loss: 0.4335  
Epoch 310/500  
**128/128**  2s 15ms/step - loss: 0.1432  
Epoch 311/500  
**128/128**  3s 21ms/step - loss: 0.1358  
Epoch 312/500  
**128/128**  2s 17ms/step - loss: 0.1372  
Epoch 313/500  
**128/128**  2s 16ms/step - loss: 0.1143  
Epoch 314/500  
**128/128**  3s 16ms/step - loss: 0.1265  
Epoch 315/500  
**128/128**  3s 16ms/step - loss: 0.1608  
Epoch 316/500  
**128/128**  2s 19ms/step - loss: 0.2501  
Epoch 317/500  
**128/128**  3s 19ms/step - loss: 0.1946  
Epoch 318/500  
**128/128**  2s 16ms/step - loss: 0.1471  
Epoch 319/500  
**128/128**  2s 16ms/step - loss: 0.1652  
Epoch 320/500  
**128/128**  3s 16ms/step - loss: 0.1887  
Epoch 321/500  
**128/128**  3s 17ms/step - loss: 0.1460  
Epoch 322/500  
**128/128**  3s 22ms/step - loss: 0.1568  
Epoch 323/500  
**128/128**  2s 16ms/step - loss: 0.1373  
Epoch 324/500  
**128/128**  2s 16ms/step - loss: 0.1731  
Epoch 325/500  
**128/128**  3s 16ms/step - loss: 0.1378  
Epoch 326/500  
**128/128**  2s 16ms/step - loss: 0.5589  
Epoch 327/500  
**128/128**  3s 19ms/step - loss: 0.1581  
Epoch 328/500  
**128/128**  3s 20ms/step - loss: 0.1236  
Epoch 329/500  
**128/128**  2s 16ms/step - loss: 0.1382  
Epoch 330/500  
**128/128**  2s 15ms/step - loss: 0.1357


Epoch 331/500  
**128/128**  3s 15ms/step - loss: 0.1590  
Epoch 332/500  
**128/128**  3s 15ms/step - loss: 0.1310  
Epoch 333/500  
**128/128**  3s 22ms/step - loss: 0.1048  
Epoch 334/500  
**128/128**  2s 16ms/step - loss: 0.3335  
Epoch 335/500  
**128/128**  2s 16ms/step - loss: 0.1249  
Epoch 336/500  
**128/128**  3s 15ms/step - loss: 0.1256  
Epoch 337/500  
**128/128**  3s 16ms/step - loss: 0.1038  
Epoch 338/500  
**128/128**  2s 19ms/step - loss: 0.1511  
Epoch 339/500  
**128/128**  2s 19ms/step - loss: 0.1678  
Epoch 340/500  
**128/128**  2s 16ms/step - loss: 0.1261  
Epoch 341/500  
**128/128**  2s 16ms/step - loss: 0.1508  
Epoch 342/500  
**128/128**  2s 16ms/step - loss: 0.1957  
Epoch 343/500  
**128/128**  3s 16ms/step - loss: 1.4057  
Epoch 344/500  
**128/128**  3s 21ms/step - loss: 0.1281  
Epoch 345/500  
**128/128**  2s 17ms/step - loss: 0.1716  
Epoch 346/500  
**128/128**  2s 16ms/step - loss: 0.1345  
Epoch 347/500  
**128/128**  3s 16ms/step - loss: 0.1377  
Epoch 348/500  
**128/128**  3s 16ms/step - loss: 0.1248  
Epoch 349/500  
**128/128**  3s 22ms/step - loss: 0.1273  
Epoch 350/500  
**128/128**  4s 17ms/step - loss: 0.1068  
Epoch 351/500  
**128/128**  2s 16ms/step - loss: 0.1153  
Epoch 352/500  
**128/128**  2s 16ms/step - loss: 0.8932


Epoch 353/500  
**128/128**  3s 19ms/step - loss: 0.1225


Epoch 354/500  
**128/128**  3s 21ms/step - loss: 0.1261


Epoch 355/500  
**128/128**  2s 16ms/step - loss: 0.1092


Epoch 356/500  
**128/128**  3s 16ms/step - loss: 0.1175


Epoch 357/500  
**128/128**  2s 16ms/step - loss: 0.1112


Epoch 358/500  
**128/128**  2s 16ms/step - loss: 0.1084


Epoch 359/500  
**128/128**  3s 21ms/step - loss: 0.1183


Epoch 360/500  
**128/128**  2s 17ms/step - loss: 0.1381


Epoch 361/500  
**128/128**  2s 16ms/step - loss: 0.1348


Epoch 362/500  
**128/128**  2s 16ms/step - loss: 0.1444


Epoch 363/500  
**128/128**  3s 16ms/step - loss: 0.1450


Epoch 364/500  
**128/128**  3s 19ms/step - loss: 0.1102


Epoch 365/500  
**128/128**  3s 19ms/step - loss: 0.1196


Epoch 366/500  
**128/128**  2s 17ms/step - loss: 0.1040


Epoch 367/500  
**128/128**  2s 16ms/step - loss: 0.1196


Epoch 368/500  
**128/128**  3s 16ms/step - loss: 0.1949


Epoch 369/500  
**128/128**  2s 16ms/step - loss: 0.1084

Epoch 370/500  
**128/128**  3s 23ms/step - loss: 0.1099





Epoch 371/500  
**128/128**  2s 17ms/step - loss: 4.0592























Epoch 372/500  
**128/128**  2s 16ms/step - loss: 2.1068














Epoch 373/500  
**128/128**  3s 16ms/step - loss: 1.1548

Epoch 374/500  
**128/128**  2s 16ms/step - loss: 0.4252















Epoch 375/500  
**128/128**  3s 18ms/step - loss: 0.4681  
Epoch 376/500  
**128/128**  3s 20ms/step - loss: 0.3725  
Epoch 377/500  
**128/128**  2s 16ms/step - loss: 0.3145  
Epoch 378/500  
**128/128**  2s 16ms/step - loss: 0.3840  
Epoch 379/500  
**128/128**  3s 16ms/step - loss: 0.3189  
Epoch 380/500  
**128/128**  2s 16ms/step - loss: 0.3424  
Epoch 381/500  
**128/128**  3s 22ms/step - loss: 0.3041  
Epoch 382/500  
**128/128**  4s 17ms/step - loss: 0.2468  
Epoch 383/500  
**128/128**  2s 16ms/step - loss: 0.2320  
Epoch 384/500  
**128/128**  3s 16ms/step - loss: 0.2580  
Epoch 385/500  
**128/128**  3s 21ms/step - loss: 0.2590  
Epoch 386/500  
**128/128**  2s 17ms/step - loss: 0.2514  
Epoch 387/500  
**128/128**  2s 16ms/step - loss: 0.2142  
Epoch 388/500  
**128/128**  2s 16ms/step - loss: 0.1592  
Epoch 389/500  
**128/128**  3s 16ms/step - loss: 0.1808  
Epoch 390/500  
**128/128**  2s 16ms/step - loss: 0.1741  
Epoch 391/500  
**128/128**  3s 23ms/step - loss: 0.1685  
Epoch 392/500  
**128/128**  2s 16ms/step - loss: 0.1781  
Epoch 393/500  
**128/128**  3s 16ms/step - loss: 0.2300  
Epoch 394/500  
**128/128**  2s 15ms/step - loss: 0.1629  
Epoch 395/500  
**128/128**  2s 16ms/step - loss: 0.1608  
Epoch 396/500  
**128/128**  3s 21ms/step - loss: 0.2380

Epoch 397/500  
**128/128**  5s 17ms/step - loss: 0.1718  
Epoch 398/500  
**128/128**  2s 16ms/step - loss: 0.1610  
Epoch 399/500  
**128/128**  2s 16ms/step - loss: 0.1371  
Epoch 400/500  
**128/128**  2s 17ms/step - loss: 0.1354  
Epoch 401/500  
**128/128**  3s 22ms/step - loss: 0.1357  
Epoch 402/500  
**128/128**  2s 16ms/step - loss: 0.1468  
Epoch 403/500  
**128/128**  3s 16ms/step - loss: 0.1472  
Epoch 404/500  
**128/128**  2s 16ms/step - loss: 0.1260  
Epoch 405/500  
**128/128**  2s 16ms/step - loss: 0.1648  
Epoch 406/500  
**128/128**  2s 18ms/step - loss: 0.1369  
Epoch 407/500  
**128/128**  3s 20ms/step - loss: 0.1314  
Epoch 408/500  
**128/128**  2s 16ms/step - loss: 0.1602  
Epoch 409/500  
**128/128**  3s 16ms/step - loss: 0.1944  
Epoch 410/500  
**128/128**  2s 16ms/step - loss: 0.1332  
Epoch 411/500  
**128/128**  2s 16ms/step - loss: 0.1283  
Epoch 412/500  
**128/128**  3s 21ms/step - loss: 0.1445  
Epoch 413/500  
**128/128**  5s 17ms/step - loss: 0.1226  
Epoch 414/500  
**128/128**  2s 16ms/step - loss: 0.1158  
Epoch 415/500  
**128/128**  2s 16ms/step - loss: 0.1471  
Epoch 416/500  
**128/128**  3s 20ms/step - loss: 0.1440  
Epoch 417/500  
**128/128**  3s 21ms/step - loss: 0.1354  
Epoch 418/500  
**128/128**  5s 17ms/step - loss: 0.1248

Epoch 419/500  
**128/128**  2s 16ms/step - loss: 0.1402  
Epoch 420/500  
**128/128**  2s 16ms/step - loss: 0.3399  
Epoch 421/500  
**128/128**  3s 22ms/step - loss: 0.2733  
Epoch 422/500  
**128/128**  2s 17ms/step - loss: 0.1494  
Epoch 423/500  
**128/128**  2s 16ms/step - loss: 0.1472  
Epoch 424/500  
**128/128**  3s 16ms/step - loss: 0.1305  
Epoch 425/500  
**128/128**  3s 16ms/step - loss: 0.1290  
Epoch 426/500  
**128/128**  3s 20ms/step - loss: 0.1299  
Epoch 427/500  
**128/128**  3s 20ms/step - loss: 0.1611  
Epoch 428/500  
**128/128**  5s 17ms/step - loss: 0.1345  
Epoch 429/500  
**128/128**  2s 16ms/step - loss: 0.1238  
Epoch 430/500  
**128/128**  3s 20ms/step - loss: 0.1462  
Epoch 431/500  
**128/128**  3s 23ms/step - loss: 0.1333  
Epoch 432/500  
**128/128**  4s 18ms/step - loss: 0.1396  
Epoch 433/500  
**128/128**  2s 16ms/step - loss: 0.1194  
Epoch 434/500  
**128/128**  3s 16ms/step - loss: 0.3360  
Epoch 435/500  
**128/128**  3s 22ms/step - loss: 0.1418  
Epoch 436/500  
**128/128**  4s 17ms/step - loss: 0.1453  
Epoch 437/500  
**128/128**  2s 16ms/step - loss: 0.1131  
Epoch 438/500  
**128/128**  2s 16ms/step - loss: 0.1403  
Epoch 439/500  
**128/128**  2s 17ms/step - loss: 0.1206  
Epoch 440/500  
**128/128**  3s 21ms/step - loss: 0.1310

Epoch 441/500  
**128/128**  5s 17ms/step - loss: 0.1184  
Epoch 442/500  
**128/128**  2s 16ms/step - loss: 0.1548  
Epoch 443/500  
**128/128**  2s 16ms/step - loss: 0.1707  
Epoch 444/500  
**128/128**  3s 23ms/step - loss: 0.1600  
Epoch 445/500  
**128/128**  4s 17ms/step - loss: 0.1095  
Epoch 446/500  
**128/128**  2s 16ms/step - loss: 0.1394  
Epoch 447/500  
**128/128**  2s 16ms/step - loss: 0.1135  
Epoch 448/500  
**128/128**  3s 21ms/step - loss: 0.1101  
Epoch 449/500  
**128/128**  3s 20ms/step - loss: 0.1484  
Epoch 450/500  
**128/128**  2s 16ms/step - loss: 0.1330  
Epoch 451/500  
**128/128**  3s 16ms/step - loss: 0.1461  
Epoch 452/500  
**128/128**  2s 16ms/step - loss: 0.2305  
Epoch 453/500  
**128/128**  2s 16ms/step - loss: 0.1391  
Epoch 454/500  
**128/128**  3s 22ms/step - loss: 0.1751  
Epoch 455/500  
**128/128**  2s 18ms/step - loss: 0.1244  
Epoch 456/500  
**128/128**  2s 16ms/step - loss: 0.1211  
Epoch 457/500  
**128/128**  2s 16ms/step - loss: 0.1590  
Epoch 458/500  
**128/128**  3s 16ms/step - loss: 0.2172  
Epoch 459/500  
**128/128**  3s 19ms/step - loss: 0.1275  
Epoch 460/500  
**128/128**  3s 20ms/step - loss: 0.1253  
Epoch 461/500  
**128/128**  2s 17ms/step - loss: 0.1195  
Epoch 462/500  
**128/128**  3s 17ms/step - loss: 0.1088

Epoch 463/500  
**128/128**  2s 16ms/step - loss: 0.1417  
Epoch 464/500  
**128/128**  2s 17ms/step - loss: 0.8703  
Epoch 465/500  
**128/128**  3s 22ms/step - loss: 0.1584  
Epoch 466/500  
**128/128**  5s 18ms/step - loss: 0.1526  
Epoch 467/500  
**128/128**  2s 17ms/step - loss: 0.1530  
Epoch 468/500  
**128/128**  2s 16ms/step - loss: 0.1271  
Epoch 469/500  
**128/128**  3s 21ms/step - loss: 0.1025  
Epoch 470/500  
**128/128**  2s 19ms/step - loss: 0.1253  
Epoch 471/500  
**128/128**  2s 16ms/step - loss: 0.1050  
Epoch 472/500  
**128/128**  2s 16ms/step - loss: 0.1482  
Epoch 473/500  
**128/128**  3s 16ms/step - loss: 0.1210  
Epoch 474/500  
**128/128**  2s 17ms/step - loss: 0.0988  
Epoch 475/500  
**128/128**  3s 22ms/step - loss: 0.1233  
Epoch 476/500  
**128/128**  4s 17ms/step - loss: 0.1012  
Epoch 477/500  
**128/128**  2s 16ms/step - loss: 0.1258  
Epoch 478/500  
**128/128**  3s 16ms/step - loss: 0.1388  
Epoch 479/500  
**128/128**  3s 22ms/step - loss: 0.0889  
Epoch 480/500  
**128/128**  4s 17ms/step - loss: 0.0992  
Epoch 481/500  
**128/128**  2s 16ms/step - loss: 0.1008  
Epoch 482/500  
**128/128**  2s 16ms/step - loss: 0.0916  
Epoch 483/500  
**128/128**  3s 19ms/step - loss: 0.1448  
Epoch 484/500  
**128/128**  3s 21ms/step - loss: 0.1263

```

Epoch 485/500
128/128 ————— 5s 17ms/step - loss: 0.1077
Epoch 486/500
128/128 ————— 2s 16ms/step - loss: 0.1186
Epoch 487/500
128/128 ————— 2s 16ms/step - loss: 0.1087
Epoch 488/500
128/128 ————— 3s 22ms/step - loss: 0.0982
Epoch 489/500
128/128 ————— 5s 17ms/step - loss: 0.1113
Epoch 490/500
128/128 ————— 2s 17ms/step - loss: 0.1037
Epoch 491/500
128/128 ————— 2s 16ms/step - loss: 1.4874
Epoch 492/500
128/128 ————— 2s 18ms/step - loss: 0.3942
Epoch 493/500
128/128 ————— 3s 20ms/step - loss: 0.1447
Epoch 494/500
128/128 ————— 2s 16ms/step - loss: 0.1395
Epoch 495/500
128/128 ————— 3s 16ms/step - loss: 0.1562
Epoch 496/500
128/128 ————— 3s 16ms/step - loss: 0.1228
Epoch 497/500
128/128 ————— 2s 16ms/step - loss: 0.1293
Epoch 498/500
128/128 ————— 3s 23ms/step - loss: 0.1372
Epoch 499/500
128/128 ————— 4s 17ms/step - loss: 0.1470
Epoch 500/500
128/128 ————— 2s 16ms/step - loss: 0.1523
32/32 ————— 1s 12ms/step

```

```

In [15]: # Split data into training and testing for GDP Per Capita
X_train_pc, X_test_pc, y_train_pc, y_test_pc = train_test_split(X_lstm, y_gdp_per_capita, test_size=0.2, random_state=42)

# Building the LSTM Model
model_gdp_pc = Sequential()
model_gdp_pc.add(LSTM(50, return_sequences=True, input_shape=(X_train_pc.shape[1], 1)))
model_gdp_pc.add(Dropout(0.2))
model_gdp_pc.add(LSTM(50, return_sequences=False))
model_gdp_pc.add(Dropout(0.2))
model_gdp_pc.add(Dense(25))


```


```
model_gdp_pc.add(Dense(1))


# Compile the model
model_gdp_pc.compile(optimizer=Adam(learning_rate=0.001), loss='mean_squared_error')


# Train the model
model_gdp_pc.fit(X_train_pc, y_train_pc, batch_size=32, epochs=500)


# Predicting GDP Per Capita
pred_gdp_pc = model_gdp_pc.predict(X_test_pc)
```


Epoch 1/500  
**128/128**  4s 20ms/step - loss: 27.4917


Epoch 2/500  
**128/128**  5s 16ms/step - loss: 2.9432


Epoch 3/500  
**128/128**  2s 15ms/step - loss: 2.7936


Epoch 4/500  
**128/128**  3s 15ms/step - loss: 2.8612


Epoch 5/500  
**128/128**  3s 20ms/step - loss: 2.8951


Epoch 6/500  
**128/128**  5s 16ms/step - loss: 2.8118


Epoch 7/500  
**128/128**  2s 15ms/step - loss: 2.8858


Epoch 8/500  
**128/128**  3s 15ms/step - loss: 2.8678


Epoch 9/500  
**128/128**  3s 19ms/step - loss: 2.8209


Epoch 10/500  
**128/128**  2s 18ms/step - loss: 2.7625


Epoch 11/500  
**128/128**  2s 15ms/step - loss: 2.7313


Epoch 12/500  
**128/128**  2s 15ms/step - loss: 2.8288


Epoch 13/500  
**128/128**  2s 15ms/step - loss: 2.7651


Epoch 14/500  
**128/128**  3s 15ms/step - loss: 2.8090


Epoch 15/500  
**128/128**  3s 21ms/step - loss: 2.7918


Epoch 16/500  
**128/128**  2s 16ms/step - loss: 2.7776


Epoch 17/500  
**128/128**  2s 15ms/step - loss: 2.8912

Epoch 18/500  
**128/128**  2s 15ms/step - loss: 2.7358


Epoch 19/500  
**128/128**  2s 15ms/step - loss: 2.7697


Epoch 20/500  
**128/128**  3s 16ms/step - loss: 2.7632


Epoch 21/500  
**128/128**  3s 20ms/step - loss: 2.7048


Epoch 22/500  
**128/128**  5s 16ms/step - loss: 2.8943





Epoch 23/500  
**128/128**  2s 15ms/step - loss: 2.6814


Epoch 24/500  
**128/128**  3s 15ms/step - loss: 2.7112


Epoch 25/500  
**128/128**  3s 23ms/step - loss: 2.7009


Epoch 26/500  
**128/128**  4s 16ms/step - loss: 2.7579


Epoch 27/500  
**128/128**  2s 15ms/step - loss: 2.6203


Epoch 28/500  
**128/128**  3s 16ms/step - loss: 2.6115


Epoch 29/500  
**128/128**  3s 22ms/step - loss: 2.7116


Epoch 30/500  
**128/128**  2s 16ms/step - loss: 2.6306


Epoch 31/500  
**128/128**  2s 15ms/step - loss: 2.5945


Epoch 32/500  
**128/128**  2s 15ms/step - loss: 2.7535


Epoch 33/500  
**128/128**  3s 15ms/step - loss: 2.6546


Epoch 34/500  
**128/128**  3s 20ms/step - loss: 2.6411


Epoch 35/500  
**128/128**  5s 17ms/step - loss: 2.5880


Epoch 36/500  
**128/128**  2s 15ms/step - loss: 2.5145


Epoch 37/500  
**128/128**  3s 15ms/step - loss: 2.5827


Epoch 38/500  
**128/128**  2s 19ms/step - loss: 2.5863


Epoch 39/500  
**128/128**  2s 18ms/step - loss: 2.5400























Epoch 40/500  
**128/128**  2s 15ms/step - loss: 2.5471









Epoch 41/500  
**128/128**  3s 15ms/step - loss: 2.4888

Epoch 42/500  
**128/128**  3s 16ms/step - loss: 2.6560

Epoch 43/500  
**128/128**  2s 18ms/step - loss: 2.5479

Epoch 44/500  
**128/128**  3s 20ms/step - loss: 2.4905

Epoch 45/500  
**128/128**  5s 17ms/step - loss: 2.4567  
Epoch 46/500  
**128/128**  2s 15ms/step - loss: 2.5394  
Epoch 47/500  
**128/128**  3s 16ms/step - loss: 2.5131  
Epoch 48/500  
**128/128**  3s 21ms/step - loss: 2.4896  
Epoch 49/500  
**128/128**  2s 16ms/step - loss: 3.0256  
Epoch 50/500  
**128/128**  2s 15ms/step - loss: 2.8009  
Epoch 51/500  
**128/128**  2s 15ms/step - loss: 2.6400  
Epoch 52/500  
**128/128**  2s 15ms/step - loss: 2.5567  
Epoch 53/500  
**128/128**  2s 17ms/step - loss: 2.4561  
Epoch 54/500  
**128/128**  3s 20ms/step - loss: 2.4818  
Epoch 55/500  
**128/128**  5s 17ms/step - loss: 2.4807  
Epoch 56/500  
**128/128**  2s 15ms/step - loss: 2.4387  
Epoch 57/500  
**128/128**  2s 16ms/step - loss: 2.5367  
Epoch 58/500  
**128/128**  3s 21ms/step - loss: 2.3740  
Epoch 59/500  
**128/128**  5s 17ms/step - loss: 2.5075  
Epoch 60/500  
**128/128**  2s 16ms/step - loss: 2.4162  
Epoch 61/500  
**128/128**  3s 16ms/step - loss: 2.4183  
Epoch 62/500  
**128/128**  3s 21ms/step - loss: 2.4768  
Epoch 63/500  
**128/128**  2s 18ms/step - loss: 2.3808  
Epoch 64/500  
**128/128**  2s 15ms/step - loss: 2.5068  
Epoch 65/500  
**128/128**  3s 15ms/step - loss: 2.4523  
Epoch 66/500  
**128/128**  3s 15ms/step - loss: 2.3890


Epoch 67/500  
**128/128**  2s 17ms/step - loss: 2.4420  
Epoch 68/500  
**128/128**  3s 20ms/step - loss: 2.3262  
Epoch 69/500  
**128/128**  2s 16ms/step - loss: 2.3340  
Epoch 70/500  
**128/128**  3s 15ms/step - loss: 2.4323  
Epoch 71/500  
**128/128**  2s 15ms/step - loss: 2.3839  
Epoch 72/500  
**128/128**  3s 15ms/step - loss: 2.4123  
Epoch 73/500  
**128/128**  3s 21ms/step - loss: 2.4121  
Epoch 74/500  
**128/128**  2s 15ms/step - loss: 2.4154  
Epoch 75/500  
**128/128**  3s 16ms/step - loss: 2.3716  
Epoch 76/500  
**128/128**  2s 16ms/step - loss: 2.4196  
Epoch 77/500  
**128/128**  2s 16ms/step - loss: 2.4288  
Epoch 78/500  
**128/128**  2s 19ms/step - loss: 2.3606  
Epoch 79/500  
**128/128**  2s 18ms/step - loss: 2.4305  
Epoch 80/500  
**128/128**  2s 16ms/step - loss: 2.4108  
Epoch 81/500  
**128/128**  3s 16ms/step - loss: 2.4235  
Epoch 82/500  
**128/128**  2s 16ms/step - loss: 2.4326  
Epoch 83/500  
**128/128**  3s 17ms/step - loss: 2.3248  
Epoch 84/500  
**128/128**  3s 21ms/step - loss: 2.4256  
Epoch 85/500  
**128/128**  2s 15ms/step - loss: 2.4019  
Epoch 86/500  
**128/128**  2s 15ms/step - loss: 2.3553  
Epoch 87/500  
**128/128**  2s 15ms/step - loss: 2.4319  
Epoch 88/500  
**128/128**  2s 15ms/step - loss: 2.3000

Epoch 89/500  
**128/128**  3s 19ms/step - loss: 2.4691

Epoch 90/500  
**128/128**  3s 20ms/step - loss: 2.3638

Epoch 91/500  
**128/128**  5s 17ms/step - loss: 2.4044

Epoch 92/500  
**128/128**  2s 15ms/step - loss: 2.4210

Epoch 93/500  
**128/128**  2s 16ms/step - loss: 2.4268


Epoch 94/500  
**128/128**  3s 21ms/step - loss: 2.3425


Epoch 95/500  
**128/128**  2s 17ms/step - loss: 2.4313


Epoch 96/500  
**128/128**  2s 16ms/step - loss: 2.4381


Epoch 97/500  
**128/128**  3s 16ms/step - loss: 2.3672


Epoch 98/500  
**128/128**  2s 16ms/step - loss: 2.3500

Epoch 99/500  
**128/128**  3s 19ms/step - loss: 2.4033

Epoch 100/500  
**128/128**  3s 19ms/step - loss: 2.4213


Epoch 101/500  
**128/128**  2s 16ms/step - loss: 2.3339

Epoch 102/500  
**128/128**  3s 16ms/step - loss: 2.4548


Epoch 103/500  
**128/128**  3s 16ms/step - loss: 2.3422


Epoch 104/500  
**128/128**  2s 16ms/step - loss: 2.4687


Epoch 105/500  
**128/128**  3s 21ms/step - loss: 2.3821























Epoch 106/500  
**128/128**  5s 16ms/step - loss: 2.4294




















Epoch 107/500  
**128/128**  2s 15ms/step - loss: 2.3388






















Epoch 108/500  
**128/128**  2s 16ms/step - loss: 2.2741























Epoch 109/500  
**128/128**  3s 20ms/step - loss: 2.3734

Epoch 110/500  
**128/128**  2s 17ms/step - loss: 2.3843























Epoch 111/500  
**128/128**  2s 16ms/step - loss: 2.4131  
Epoch 112/500  
**128/128**  3s 16ms/step - loss: 2.3639  
Epoch 113/500  
**128/128**  2s 16ms/step - loss: 2.4181  
Epoch 114/500  
**128/128**  3s 18ms/step - loss: 2.4427  
Epoch 115/500  
**128/128**  3s 20ms/step - loss: 2.3449  
Epoch 116/500  
**128/128**  2s 16ms/step - loss: 2.3823  
Epoch 117/500  
**128/128**  2s 16ms/step - loss: 2.3682  
Epoch 118/500  
**128/128**  3s 16ms/step - loss: 2.3903  
Epoch 119/500  
**128/128**  3s 16ms/step - loss: 2.3471  
Epoch 120/500  
**128/128**  3s 20ms/step - loss: 2.3618  
Epoch 121/500  
**128/128**  2s 16ms/step - loss: 2.3746  
Epoch 122/500  
**128/128**  3s 16ms/step - loss: 2.3729  
Epoch 123/500  
**128/128**  2s 16ms/step - loss: 2.3950  
Epoch 124/500  
**128/128**  2s 16ms/step - loss: 2.3738  
Epoch 125/500  
**128/128**  3s 21ms/step - loss: 2.3929  
Epoch 126/500  
**128/128**  2s 17ms/step - loss: 2.4241  
Epoch 127/500  
**128/128**  2s 16ms/step - loss: 2.4218  
Epoch 128/500  
**128/128**  2s 16ms/step - loss: 2.4120  
Epoch 129/500  
**128/128**  2s 15ms/step - loss: 2.3864  
Epoch 130/500  
**128/128**  3s 17ms/step - loss: 2.3646  
Epoch 131/500  
**128/128**  3s 22ms/step - loss: 2.4253  
Epoch 132/500  
**128/128**  2s 16ms/step - loss: 2.3783























Epoch 133/500  
**128/128**  3s 16ms/step - loss: 2.4140  
Epoch 134/500  
**128/128**  2s 16ms/step - loss: 2.4235  
Epoch 135/500  
**128/128**  3s 16ms/step - loss: 2.3450  
Epoch 136/500  
**128/128**  3s 20ms/step - loss: 2.3977  
Epoch 137/500  
**128/128**  5s 17ms/step - loss: 2.3536  
Epoch 138/500  
**128/128**  2s 16ms/step - loss: 2.4564  
Epoch 139/500  
**128/128**  3s 16ms/step - loss: 2.3863  
Epoch 140/500  
**128/128**  3s 22ms/step - loss: 2.2712  
Epoch 141/500  
**128/128**  2s 16ms/step - loss: 2.3252  
Epoch 142/500  
**128/128**  3s 16ms/step - loss: 2.4414  
Epoch 143/500  
**128/128**  2s 16ms/step - loss: 2.4444  
Epoch 144/500  
**128/128**  3s 16ms/step - loss: 2.2995  
Epoch 145/500  
**128/128**  3s 21ms/step - loss: 2.3955  
Epoch 146/500  
**128/128**  2s 17ms/step - loss: 2.3994  
Epoch 147/500  
**128/128**  2s 16ms/step - loss: 2.4263  
Epoch 148/500  
**128/128**  3s 16ms/step - loss: 2.3391  
Epoch 149/500  
**128/128**  2s 16ms/step - loss: 2.4054  
Epoch 150/500  
**128/128**  3s 18ms/step - loss: 2.4050  
Epoch 151/500  
**128/128**  3s 21ms/step - loss: 2.3037  
Epoch 152/500  
**128/128**  2s 16ms/step - loss: 2.4304  
Epoch 153/500  
**128/128**  2s 16ms/step - loss: 2.3072  
Epoch 154/500  
**128/128**  3s 16ms/step - loss: 2.4005























Epoch 155/500  
**128/128**  2s 16ms/step - loss: 2.3807  
Epoch 156/500  
**128/128**  3s 20ms/step - loss: 2.3234  
Epoch 157/500  
**128/128**  5s 17ms/step - loss: 2.4123  
Epoch 158/500  
**128/128**  2s 16ms/step - loss: 2.3988  
Epoch 159/500  
**128/128**  2s 16ms/step - loss: 2.3938  
Epoch 160/500  
**128/128**  3s 19ms/step - loss: 2.4224  
Epoch 161/500  
**128/128**  3s 20ms/step - loss: 2.4248  
Epoch 162/500  
**128/128**  2s 16ms/step - loss: 2.3830  
Epoch 163/500  
**128/128**  3s 16ms/step - loss: 2.4343  
Epoch 164/500  
**128/128**  3s 16ms/step - loss: 2.4537  
Epoch 165/500  
**128/128**  2s 16ms/step - loss: 2.4361  
Epoch 166/500  
**128/128**  3s 22ms/step - loss: 2.4346  
Epoch 167/500  
**128/128**  2s 16ms/step - loss: 2.3691  
Epoch 168/500  
**128/128**  2s 16ms/step - loss: 2.3925  
Epoch 169/500  
**128/128**  3s 16ms/step - loss: 2.3585  
Epoch 170/500  
**128/128**  2s 16ms/step - loss: 2.4151  
Epoch 171/500  
**128/128**  3s 22ms/step - loss: 2.4293  
Epoch 172/500  
**128/128**  2s 16ms/step - loss: 2.3422  
Epoch 173/500  
**128/128**  2s 16ms/step - loss: 2.4021  
Epoch 174/500  
**128/128**  2s 16ms/step - loss: 2.3187  
Epoch 175/500  
**128/128**  3s 16ms/step - loss: 2.3639  
Epoch 176/500  
**128/128**  3s 20ms/step - loss: 2.3862























Epoch 177/500  
**128/128**  5s 18ms/step - loss: 2.3867  
Epoch 178/500  
**128/128**  2s 16ms/step - loss: 2.2939  
Epoch 179/500  
**128/128**  2s 16ms/step - loss: 2.3701  
Epoch 180/500  
**128/128**  2s 19ms/step - loss: 2.3129  
Epoch 181/500  
**128/128**  3s 21ms/step - loss: 2.3695  
Epoch 182/500  
**128/128**  2s 15ms/step - loss: 2.3860  
Epoch 183/500  
**128/128**  3s 15ms/step - loss: 2.3837  
Epoch 184/500  
**128/128**  3s 16ms/step - loss: 2.3606  
Epoch 185/500  
**128/128**  3s 16ms/step - loss: 2.4356  
Epoch 186/500  
**128/128**  3s 21ms/step - loss: 2.3510  
Epoch 187/500  
**128/128**  5s 17ms/step - loss: 2.4003  
Epoch 188/500  
**128/128**  2s 16ms/step - loss: 2.3145  
Epoch 189/500  
**128/128**  3s 16ms/step - loss: 2.3558  
Epoch 190/500  
**128/128**  3s 22ms/step - loss: 2.4056  
Epoch 191/500  
**128/128**  2s 18ms/step - loss: 2.3333  
Epoch 192/500  
**128/128**  2s 16ms/step - loss: 2.3054  
Epoch 193/500  
**128/128**  3s 16ms/step - loss: 2.2565  
Epoch 194/500  
**128/128**  3s 16ms/step - loss: 2.2907  
Epoch 195/500  
**128/128**  2s 18ms/step - loss: 2.3493  
Epoch 196/500  
**128/128**  3s 20ms/step - loss: 2.2892  
Epoch 197/500  
**128/128**  5s 17ms/step - loss: 2.3443  
Epoch 198/500  
**128/128**  2s 16ms/step - loss: 2.2648


























Epoch 199/500  
**128/128**  2s 16ms/step - loss: 2.2156  
Epoch 200/500  
**128/128**  3s 21ms/step - loss: 2.2800  
Epoch 201/500  
**128/128**  5s 17ms/step - loss: 2.3421  
Epoch 202/500  
**128/128**  2s 16ms/step - loss: 2.2125  
Epoch 203/500  
**128/128**  3s 16ms/step - loss: 2.2898  
Epoch 204/500  
**128/128**  3s 21ms/step - loss: 2.2452  
Epoch 205/500  
**128/128**  2s 18ms/step - loss: 2.2560  
Epoch 206/500  
**128/128**  2s 16ms/step - loss: 2.2329  
Epoch 207/500  
**128/128**  2s 16ms/step - loss: 2.5391  
Epoch 208/500  
**128/128**  2s 16ms/step - loss: 2.5184  
Epoch 209/500  
**128/128**  2s 16ms/step - loss: 2.3717  
Epoch 210/500  
**128/128**  3s 22ms/step - loss: 2.3803  
Epoch 211/500  
**128/128**  5s 17ms/step - loss: 2.4153  
Epoch 212/500  
**128/128**  2s 16ms/step - loss: 2.4244  
Epoch 213/500  
**128/128**  2s 16ms/step - loss: 2.5038  
Epoch 214/500  
**128/128**  2s 19ms/step - loss: 2.3387  
Epoch 215/500  
**128/128**  3s 19ms/step - loss: 2.4610  
Epoch 216/500  
**128/128**  2s 16ms/step - loss: 2.4797  
Epoch 217/500  
**128/128**  2s 16ms/step - loss: 2.3697  
Epoch 218/500  
**128/128**  2s 16ms/step - loss: 2.4568  
Epoch 219/500  
**128/128**  2s 16ms/step - loss: 2.4123  
Epoch 220/500  
**128/128**  3s 23ms/step - loss: 2.2480


Epoch 221/500  
**128/128**  2s 17ms/step - loss: 2.2430  
Epoch 222/500  
**128/128**  2s 16ms/step - loss: 2.2676  
Epoch 223/500  
**128/128**  3s 16ms/step - loss: 2.3374  
Epoch 224/500  
**128/128**  3s 16ms/step - loss: 2.1194  
Epoch 225/500  
**128/128**  3s 20ms/step - loss: 1.8975  
Epoch 226/500  
**128/128**  2s 18ms/step - loss: 1.6704  
Epoch 227/500  
**128/128**  2s 16ms/step - loss: 1.5898  
Epoch 228/500  
**128/128**  3s 16ms/step - loss: 2.2772  
Epoch 229/500  
**128/128**  3s 16ms/step - loss: 1.4846  
Epoch 230/500  
**128/128**  3s 21ms/step - loss: 1.1684  
Epoch 231/500  
**128/128**  2s 19ms/step - loss: 1.0416  
Epoch 232/500  
**128/128**  2s 16ms/step - loss: 1.0839  
Epoch 233/500  
**128/128**  2s 16ms/step - loss: 1.0811  
Epoch 234/500  
**128/128**  2s 16ms/step - loss: 1.0832  
Epoch 235/500  
**128/128**  2s 16ms/step - loss: 0.9961  
Epoch 236/500  
**128/128**  3s 22ms/step - loss: 0.9256  
Epoch 237/500  
**128/128**  2s 16ms/step - loss: 0.8960  
Epoch 238/500  
**128/128**  2s 16ms/step - loss: 0.9617  
Epoch 239/500  
**128/128**  2s 16ms/step - loss: 0.9774  
Epoch 240/500  
**128/128**  2s 16ms/step - loss: 0.9902  
Epoch 241/500  
**128/128**  3s 18ms/step - loss: 0.8443  
Epoch 242/500  
**128/128**  3s 19ms/step - loss: 0.8609


Epoch 243/500  
**128/128**  2s 16ms/step - loss: 0.9354  
Epoch 244/500  
**128/128**  3s 16ms/step - loss: 0.8529  
Epoch 245/500  
**128/128**  3s 16ms/step - loss: 0.8084  
Epoch 246/500  
**128/128**  2s 18ms/step - loss: 0.9850  
Epoch 247/500  
**128/128**  3s 21ms/step - loss: 0.8334  
Epoch 248/500  
**128/128**  2s 16ms/step - loss: 0.8710  
Epoch 249/500  
**128/128**  3s 16ms/step - loss: 0.8544  
Epoch 250/500  
**128/128**  3s 16ms/step - loss: 0.7968  
Epoch 251/500  
**128/128**  3s 16ms/step - loss: 1.9135  
Epoch 252/500  
**128/128**  3s 22ms/step - loss: 1.1579  
Epoch 253/500  
**128/128**  4s 17ms/step - loss: 0.8898  
Epoch 254/500  
**128/128**  2s 16ms/step - loss: 0.7769  
Epoch 255/500  
**128/128**  2s 16ms/step - loss: 0.6642  
Epoch 256/500  
**128/128**  3s 23ms/step - loss: 0.8220  
Epoch 257/500  
**128/128**  4s 17ms/step - loss: 0.6541  
Epoch 258/500  
**128/128**  2s 16ms/step - loss: 0.5848  
Epoch 259/500  
**128/128**  2s 16ms/step - loss: 0.5938  
Epoch 260/500  
**128/128**  2s 18ms/step - loss: 0.5404  
Epoch 261/500  
**128/128**  3s 22ms/step - loss: 0.6255  
Epoch 262/500  
**128/128**  4s 17ms/step - loss: 0.5154  
Epoch 263/500  
**128/128**  2s 16ms/step - loss: 0.5223  
Epoch 264/500  
**128/128**  2s 16ms/step - loss: 0.6981


Epoch 265/500  
**128/128**  3s 23ms/step - loss: 0.6523  
Epoch 266/500  
**128/128**  4s 17ms/step - loss: 0.4854  
Epoch 267/500  
**128/128**  2s 16ms/step - loss: 0.5511  
Epoch 268/500  
**128/128**  3s 16ms/step - loss: 0.5157  
Epoch 269/500  
**128/128**  3s 21ms/step - loss: 0.5427  
Epoch 270/500  
**128/128**  2s 19ms/step - loss: 0.4812  
Epoch 271/500  
**128/128**  2s 16ms/step - loss: 0.4953  
Epoch 272/500  
**128/128**  2s 16ms/step - loss: 0.5080  
Epoch 273/500  
**128/128**  3s 16ms/step - loss: 0.4460  
Epoch 274/500  
**128/128**  3s 19ms/step - loss: 0.4598  
Epoch 275/500  
**128/128**  3s 22ms/step - loss: 0.5118  
Epoch 276/500  
**128/128**  2s 16ms/step - loss: 0.5832  
Epoch 277/500  
**128/128**  2s 16ms/step - loss: 0.4782  
Epoch 278/500  
**128/128**  2s 16ms/step - loss: 0.4736  
Epoch 279/500  
**128/128**  2s 16ms/step - loss: 0.4176  
Epoch 280/500  
**128/128**  3s 20ms/step - loss: 0.4458  
Epoch 281/500  
**128/128**  5s 18ms/step - loss: 0.4027  
Epoch 282/500  
**128/128**  2s 16ms/step - loss: 0.4838  
Epoch 283/500  
**128/128**  3s 16ms/step - loss: 0.4209  
Epoch 284/500  
**128/128**  3s 20ms/step - loss: 0.4955  
Epoch 285/500  
**128/128**  5s 17ms/step - loss: 0.3784  
Epoch 286/500  
**128/128**  2s 16ms/step - loss: 0.4654


Epoch 287/500  
**128/128**  2s 16ms/step - loss: 0.5012  
Epoch 288/500  
**128/128**  2s 18ms/step - loss: 0.4090  
Epoch 289/500  
**128/128**  3s 23ms/step - loss: 0.3522  
Epoch 290/500  
**128/128**  4s 17ms/step - loss: 0.4240  
Epoch 291/500  
**128/128**  2s 16ms/step - loss: 0.4211  
Epoch 292/500  
**128/128**  3s 16ms/step - loss: 0.4503  
Epoch 293/500  
**128/128**  3s 23ms/step - loss: 0.4287  
Epoch 294/500  
**128/128**  2s 16ms/step - loss: 0.3457  
Epoch 295/500  
**128/128**  3s 16ms/step - loss: 0.3465  
Epoch 296/500  
**128/128**  2s 16ms/step - loss: 0.3455  
Epoch 297/500  
**128/128**  2s 16ms/step - loss: 0.4617  
Epoch 298/500  
**128/128**  2s 18ms/step - loss: 0.3378  
Epoch 299/500  
**128/128**  3s 23ms/step - loss: 0.3389  
Epoch 300/500  
**128/128**  4s 17ms/step - loss: 0.4215  
Epoch 301/500  
**128/128**  2s 16ms/step - loss: 0.3167  
Epoch 302/500  
**128/128**  2s 16ms/step - loss: 0.3849  
Epoch 303/500  
**128/128**  3s 22ms/step - loss: 0.3514  
Epoch 304/500  
**128/128**  2s 17ms/step - loss: 0.3893  
Epoch 305/500  
**128/128**  2s 16ms/step - loss: 0.2987  
Epoch 306/500  
**128/128**  2s 16ms/step - loss: 0.4035  
Epoch 307/500  
**128/128**  3s 16ms/step - loss: 0.4264  
Epoch 308/500  
**128/128**  3s 19ms/step - loss: 0.2901


Epoch 309/500  
**128/128**  3s 20ms/step - loss: 0.2991


Epoch 310/500  
**128/128**  5s 17ms/step - loss: 0.2638


Epoch 311/500  
**128/128**  2s 16ms/step - loss: 0.2709


Epoch 312/500  
**128/128**  2s 17ms/step - loss: 0.2311


Epoch 313/500  
**128/128**  3s 21ms/step - loss: 0.2412

Epoch 314/500  
**128/128**  5s 17ms/step - loss: 0.2265


Epoch 315/500  
**128/128**  2s 16ms/step - loss: 0.2362


Epoch 316/500  
**128/128**  2s 16ms/step - loss: 0.3403


Epoch 317/500  
**128/128**  3s 22ms/step - loss: 0.2369


Epoch 318/500  
**128/128**  2s 16ms/step - loss: 0.2530


Epoch 319/500  
**128/128**  3s 16ms/step - loss: 0.2213


Epoch 320/500  
**128/128**  3s 16ms/step - loss: 0.2349

Epoch 321/500  
**128/128**  3s 16ms/step - loss: 0.2646

Epoch 322/500  
**128/128**  3s 21ms/step - loss: 0.2292


Epoch 323/500  
**128/128**  5s 17ms/step - loss: 0.2362

Epoch 324/500  
**128/128**  2s 17ms/step - loss: 0.2094


Epoch 325/500  
**128/128**  2s 16ms/step - loss: 0.2286











Epoch 326/500  
**128/128**  2s 19ms/step - loss: 0.2346


Epoch 327/500  
**128/128**  3s 20ms/step - loss: 0.2216


Epoch 328/500  
**128/128**  5s 18ms/step - loss: 0.2207


Epoch 329/500  
**128/128**  2s 16ms/step - loss: 0.1855

Epoch 330/500  
**128/128**  2s 17ms/step - loss: 0.2346


Epoch 331/500  
**128/128**  3s 23ms/step - loss: 0.2263  
Epoch 332/500  
**128/128**  4s 17ms/step - loss: 0.1808  
Epoch 333/500  
**128/128**  2s 16ms/step - loss: 0.2190  
Epoch 334/500  
**128/128**  2s 16ms/step - loss: 0.2000  
Epoch 335/500  
**128/128**  2s 18ms/step - loss: 0.1596  
Epoch 336/500  
**128/128**  3s 22ms/step - loss: 0.2010  
Epoch 337/500  
**128/128**  2s 16ms/step - loss: 0.2156  
Epoch 338/500  
**128/128**  3s 16ms/step - loss: 0.1685  
Epoch 339/500  
**128/128**  2s 16ms/step - loss: 0.1727  
Epoch 340/500  
**128/128**  2s 16ms/step - loss: 0.2029  
Epoch 341/500  
**128/128**  3s 20ms/step - loss: 0.2076  
Epoch 342/500  
**128/128**  3s 20ms/step - loss: 0.1800  
Epoch 343/500  
**128/128**  2s 16ms/step - loss: 0.1947  
Epoch 344/500  
**128/128**  3s 16ms/step - loss: 0.1892  
Epoch 345/500  
**128/128**  3s 16ms/step - loss: 0.1467  
Epoch 346/500  
**128/128**  2s 17ms/step - loss: 0.1791  
Epoch 347/500  
**128/128**  3s 21ms/step - loss: 0.1525  
Epoch 348/500  
**128/128**  5s 17ms/step - loss: 0.1726  
Epoch 349/500  
**128/128**  2s 16ms/step - loss: 0.2226  
Epoch 350/500  
**128/128**  2s 17ms/step - loss: 0.1592  
Epoch 351/500  
**128/128**  3s 23ms/step - loss: 0.1786  
Epoch 352/500  
**128/128**  2s 17ms/step - loss: 0.1569


Epoch 353/500  
**128/128**  2s 16ms/step - loss: 0.2058


Epoch 354/500  
**128/128**  3s 17ms/step - loss: 0.1642


Epoch 355/500  
**128/128**  3s 17ms/step - loss: 0.1952


Epoch 356/500  
**128/128**  3s 22ms/step - loss: 0.1442


Epoch 357/500  
**128/128**  2s 17ms/step - loss: 0.1553


Epoch 358/500  
**128/128**  2s 16ms/step - loss: 0.1782


Epoch 359/500  
**128/128**  3s 16ms/step - loss: 0.1568


Epoch 360/500  
**128/128**  2s 16ms/step - loss: 0.1363


Epoch 361/500  
**128/128**  3s 19ms/step - loss: 0.1560


Epoch 362/500  
**128/128**  3s 21ms/step - loss: 0.1435


Epoch 363/500  
**128/128**  2s 16ms/step - loss: 0.1378


Epoch 364/500  
**128/128**  3s 16ms/step - loss: 0.1286


Epoch 365/500  
**128/128**  3s 16ms/step - loss: 0.1481


Epoch 366/500  
**128/128**  4s 35ms/step - loss: 0.1504


Epoch 367/500  
**128/128**  3s 26ms/step - loss: 0.1813


Epoch 368/500  
**128/128**  4s 17ms/step - loss: 0.1908


Epoch 369/500  
**128/128**  3s 17ms/step - loss: 0.6201

Epoch 370/500  
**128/128**  3s 17ms/step - loss: 0.1678





















Epoch 371/500  
**128/128**  3s 22ms/step - loss: 0.2096


Epoch 372/500  
**128/128**  5s 17ms/step - loss: 0.1359


Epoch 373/500  
**128/128**  2s 16ms/step - loss: 0.1469


Epoch 374/500  
**128/128**  2s 16ms/step - loss: 0.2175





Epoch 375/500  
**128/128**  3s 21ms/step - loss: 0.1705  
Epoch 376/500  
**128/128**  5s 17ms/step - loss: 0.1774  
Epoch 377/500  
**128/128**  2s 16ms/step - loss: 0.1447  
Epoch 378/500  
**128/128**  2s 16ms/step - loss: 0.1430  
Epoch 379/500  
**128/128**  2s 19ms/step - loss: 0.2563  
Epoch 380/500  
**128/128**  3s 21ms/step - loss: 0.2197  
Epoch 381/500  
**128/128**  2s 17ms/step - loss: 0.1558  
Epoch 382/500  
**128/128**  3s 24ms/step - loss: 0.1411  
Epoch 383/500  
**128/128**  3s 24ms/step - loss: 0.1383  
Epoch 384/500  
**128/128**  5s 21ms/step - loss: 0.1511  
Epoch 385/500  
**128/128**  2s 16ms/step - loss: 0.1703  
Epoch 386/500  
**128/128**  2s 16ms/step - loss: 0.1529  
Epoch 387/500  
**128/128**  3s 16ms/step - loss: 0.1459  
Epoch 388/500  
**128/128**  2s 17ms/step - loss: 0.0954  
Epoch 389/500  
**128/128**  3s 22ms/step - loss: 0.1466  
Epoch 390/500  
**128/128**  2s 18ms/step - loss: 0.1821  
Epoch 391/500  
**128/128**  2s 18ms/step - loss: 0.1679  
Epoch 392/500  
**128/128**  2s 18ms/step - loss: 0.1635  
Epoch 393/500  
**128/128**  2s 16ms/step - loss: 0.1209  
Epoch 394/500  
**128/128**  3s 20ms/step - loss: 0.1289  
Epoch 395/500  
**128/128**  5s 17ms/step - loss: 0.1239  
Epoch 396/500  
**128/128**  2s 16ms/step - loss: 0.1183


Epoch 397/500  
**128/128**  2s 17ms/step - loss: 0.1080


Epoch 398/500  
**128/128**  2s 17ms/step - loss: 0.1174


Epoch 399/500  
**128/128**  3s 21ms/step - loss: 0.1837


Epoch 400/500  
**128/128**  2s 16ms/step - loss: 0.1330


Epoch 401/500  
**128/128**  2s 16ms/step - loss: 0.1363


Epoch 402/500  
**128/128**  3s 16ms/step - loss: 0.1353


Epoch 403/500  
**128/128**  2s 16ms/step - loss: 0.1454


Epoch 404/500  
**128/128**  3s 23ms/step - loss: 0.1554


Epoch 405/500  
**128/128**  4s 17ms/step - loss: 0.1020


Epoch 406/500  
**128/128**  2s 16ms/step - loss: 0.1551


Epoch 407/500  
**128/128**  2s 16ms/step - loss: 0.1073


Epoch 408/500  
**128/128**  3s 22ms/step - loss: 0.1209


Epoch 409/500  
**128/128**  3s 20ms/step - loss: 0.1684


Epoch 410/500  
**128/128**  2s 16ms/step - loss: 0.1653


Epoch 411/500  
**128/128**  2s 16ms/step - loss: 0.1025


Epoch 412/500  
**128/128**  3s 17ms/step - loss: 0.1211


Epoch 413/500  
**128/128**  3s 18ms/step - loss: 0.1208



















Epoch 414/500  
**128/128**  3s 24ms/step - loss: 0.1582





















Epoch 415/500  
**128/128**  4s 18ms/step - loss: 0.0987























Epoch 416/500  
**128/128**  2s 16ms/step - loss: 0.1611

Epoch 417/500  
**128/128**  2s 16ms/step - loss: 0.0980

Epoch 418/500  
**128/128**  3s 20ms/step - loss: 0.1205

Epoch 419/500  
**128/128**  5s 17ms/step - loss: 0.1005  
Epoch 420/500  
**128/128**  2s 16ms/step - loss: 0.1108  
Epoch 421/500  
**128/128**  3s 16ms/step - loss: 0.1240  
Epoch 422/500  
**128/128**  3s 20ms/step - loss: 0.1064  
Epoch 423/500  
**128/128**  5s 17ms/step - loss: 0.0989  
Epoch 424/500  
**128/128**  2s 16ms/step - loss: 0.1265  
Epoch 425/500  
**128/128**  3s 16ms/step - loss: 0.1117  
Epoch 426/500  
**128/128**  3s 19ms/step - loss: 0.1238  
Epoch 427/500  
**128/128**  3s 21ms/step - loss: 0.1101  
Epoch 428/500  
**128/128**  5s 18ms/step - loss: 0.1042  
Epoch 429/500  
**128/128**  2s 16ms/step - loss: 0.1099  
Epoch 430/500  
**128/128**  2s 17ms/step - loss: 0.1274  
Epoch 431/500  
**128/128**  3s 23ms/step - loss: 0.0931  
Epoch 432/500  
**128/128**  2s 16ms/step - loss: 0.1502  
Epoch 433/500  
**128/128**  3s 16ms/step - loss: 0.0929  
Epoch 434/500  
**128/128**  3s 17ms/step - loss: 0.1772  
Epoch 435/500  
**128/128**  2s 17ms/step - loss: 0.1003  
Epoch 436/500  
**128/128**  3s 24ms/step - loss: 0.1448  
Epoch 437/500  
**128/128**  2s 16ms/step - loss: 0.0811  
Epoch 438/500  
**128/128**  3s 16ms/step - loss: 0.0764  
Epoch 439/500  
**128/128**  2s 16ms/step - loss: 0.1062  
Epoch 440/500  
**128/128**  3s 16ms/step - loss: 0.0783

Epoch 441/500  
**128/128**  3s 22ms/step - loss: 0.3835  
Epoch 442/500  
**128/128**  2s 17ms/step - loss: 0.0916  
Epoch 443/500  
**128/128**  2s 16ms/step - loss: 0.0886  
Epoch 444/500  
**128/128**  3s 16ms/step - loss: 0.0871  
Epoch 445/500  
**128/128**  2s 16ms/step - loss: 0.1147  
Epoch 446/500  
**128/128**  2s 18ms/step - loss: 0.0996  
Epoch 447/500  
**128/128**  3s 21ms/step - loss: 0.1055  
Epoch 448/500  
**128/128**  2s 17ms/step - loss: 0.1009  
Epoch 449/500  
**128/128**  2s 17ms/step - loss: 0.1058  
Epoch 450/500  
**128/128**  3s 16ms/step - loss: 0.1159  
Epoch 451/500  
**128/128**  2s 16ms/step - loss: 0.0843  
Epoch 452/500  
**128/128**  3s 23ms/step - loss: 0.0862  
Epoch 453/500  
**128/128**  2s 18ms/step - loss: 0.0860  
Epoch 454/500  
**128/128**  2s 17ms/step - loss: 0.1266  
Epoch 455/500  
**128/128**  2s 17ms/step - loss: 0.1285  
Epoch 456/500  
**128/128**  2s 17ms/step - loss: 0.1064  
Epoch 457/500  
**128/128**  2s 18ms/step - loss: 0.1375  
Epoch 458/500  
**128/128**  3s 23ms/step - loss: 0.1756  
Epoch 459/500  
**128/128**  2s 16ms/step - loss: 0.0782  
Epoch 460/500  
**128/128**  3s 17ms/step - loss: 0.0797  
Epoch 461/500  
**128/128**  2s 17ms/step - loss: 0.0835  
Epoch 462/500  
**128/128**  2s 17ms/step - loss: 0.0979

Epoch 463/500  
**128/128**  3s 21ms/step - loss: 0.0734  
Epoch 464/500  
**128/128**  3s 19ms/step - loss: 0.0781  
Epoch 465/500  
**128/128**  2s 16ms/step - loss: 0.1427  
Epoch 466/500  
**128/128**  3s 16ms/step - loss: 0.0663  
Epoch 467/500  
**128/128**  3s 16ms/step - loss: 0.0688  
Epoch 468/500  
**128/128**  2s 18ms/step - loss: 0.0697  
Epoch 469/500  
**128/128**  3s 21ms/step - loss: 0.0893  
Epoch 470/500  
**128/128**  2s 16ms/step - loss: 0.1253  
Epoch 471/500  
**128/128**  2s 17ms/step - loss: 0.0640  
Epoch 472/500  
**128/128**  2s 17ms/step - loss: 0.0704  
Epoch 473/500  
**128/128**  2s 17ms/step - loss: 0.0970  
Epoch 474/500  
**128/128**  3s 23ms/step - loss: 0.0885  
Epoch 475/500  
**128/128**  4s 18ms/step - loss: 0.0969  
Epoch 476/500  
**128/128**  2s 16ms/step - loss: 0.0798  
Epoch 477/500  
**128/128**  2s 17ms/step - loss: 0.0759  
Epoch 478/500  
**128/128**  3s 19ms/step - loss: 0.0854  
Epoch 479/500  
**128/128**  3s 20ms/step - loss: 0.0809  
Epoch 480/500  
**128/128**  2s 17ms/step - loss: 0.0971  
Epoch 481/500  
**128/128**  2s 17ms/step - loss: 0.0863  
Epoch 482/500  
**128/128**  2s 16ms/step - loss: 0.0683  
Epoch 483/500  
**128/128**  2s 17ms/step - loss: 0.2538  
Epoch 484/500  
**128/128**  3s 23ms/step - loss: 0.1124

```

Epoch 485/500
128/128 ————— 2s 18ms/step - loss: 0.0751
Epoch 486/500
128/128 ————— 2s 16ms/step - loss: 0.0595
Epoch 487/500
128/128 ————— 3s 16ms/step - loss: 0.0697
Epoch 488/500
128/128 ————— 2s 17ms/step - loss: 0.1072
Epoch 489/500
128/128 ————— 3s 20ms/step - loss: 0.2016
Epoch 490/500
128/128 ————— 3s 20ms/step - loss: 0.0797
Epoch 491/500
128/128 ————— 5s 17ms/step - loss: 0.0645
Epoch 492/500
128/128 ————— 2s 17ms/step - loss: 0.0688
Epoch 493/500
128/128 ————— 2s 17ms/step - loss: 0.0661
Epoch 494/500
128/128 ————— 3s 22ms/step - loss: 0.1054
Epoch 495/500
128/128 ————— 2s 17ms/step - loss: 0.0818
Epoch 496/500
128/128 ————— 2s 17ms/step - loss: 0.1201
Epoch 497/500
128/128 ————— 3s 17ms/step - loss: 0.0616
Epoch 498/500
128/128 ————— 2s 17ms/step - loss: 0.0655
Epoch 499/500
128/128 ————— 3s 24ms/step - loss: 0.0594
Epoch 500/500
128/128 ————— 4s 18ms/step - loss: 0.0910
32/32 ————— 1s 13ms/step

```

In [16]: `from sklearn.metrics import mean_squared_error, r2_score`

```

# Evaluating GDP Model
mse_gdp = mean_squared_error(y_test, pred_gdp)
r2_gdp = r2_score(y_test, pred_gdp)
print(f"GDP Model - MSE: {mse_gdp}, R2: {r2_gdp}")

# Evaluating GDP Per Capita Model
mse_gdp_pc = mean_squared_error(y_test_pc, pred_gdp_pc)

```

```
r2_gdp_pc = r2_score(y_test_pc, pred_gdp_pc)
print(f"GDP Per Capita Model - MSE: {mse_gdp_pc}, R2: {r2_gdp_pc}")
```

GDP Model - MSE: 0.04693979024887085, R2: 0.9914343995142781

GDP Per Capita Model - MSE: 0.030671848354972584, R2: 0.9873810983418025

These results indicate the performance of Long Short-Term Memory (LSTM) model for two different GDP-related predictions.

### 1. GDP Model:

- **Mean Squared Error (MSE):** 0.0469
- **R-squared ( $R^2$ ):** 0.9914

The MSE of 0.0469 is relatively low, suggesting that the model's predictions are close to the actual values, with minimal error. An  $R^2$  value of 0.9914 is very high, indicating that approximately 99.14% of the variance in GDP can be explained by the model. This means your model has a strong fit to the GDP data.

### 2. GDP Per Capita Model:

- **Mean Squared Error (MSE):** 0.0307
- **R-squared ( $R^2$ ):** 0.9874

Similarly, the MSE of 0.0307 is low, showing that the model is making accurate predictions with minimal error. The  $R^2$  value of 0.9874 is also very high, meaning that about 98.74% of the variance in GDP per capita is explained by the model. This indicates a strong fit to the GDP per capita data as well.

## Summary:

- Both models exhibit excellent performance, with very high  $R^2$  values indicating that they are well-suited to predict GDP and GDP per capita.
- The low MSE values for both models show that the predictions are close to the actual values, confirming the models' accuracy and reliability.

```
In [17]: import matplotlib.pyplot as plt

# Define the metrics for each model
models = ['GDP Model', 'GDP Per Capita Model']
mse_values = [mse_gdp, mse_gdp_pc]
r2_values = [r2_gdp, r2_gdp_pc]

# Create a figure and axis
fig, ax1 = plt.subplots(figsize=(10, 6))
```

```
# Plot MSE
ax1.bar(models, mse_values, color='blue', alpha=0.6, label='MSE')
ax1.set_xlabel('Model')
ax1.set_ylabel('Mean Squared Error (MSE)', color='blue')
ax1.tick_params(axis='y', labelcolor='blue')

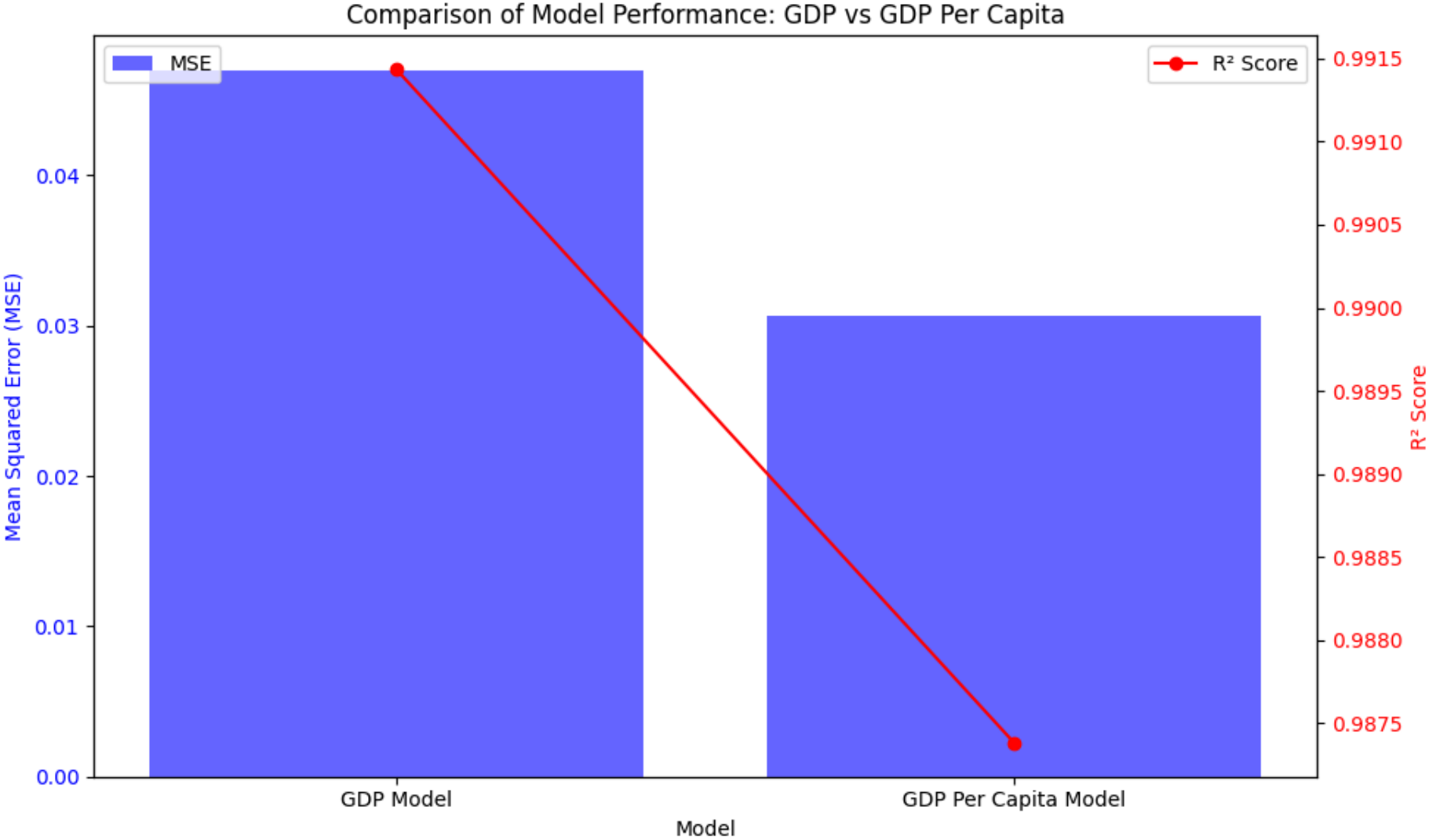
# Create a second y-axis to plot R2 scores
ax2 = ax1.twinx()
ax2.plot(models, r2_values, color='red', marker='o', label='R2 Score')
ax2.set_ylabel('R2 Score', color='red')
ax2.tick_params(axis='y', labelcolor='red')

# Add titles and labels
plt.title('Comparison of Model Performance: GDP vs GDP Per Capita')
fig.tight_layout()

# Add Legends
ax1.legend(loc='upper left')
ax2.legend(loc='upper right')

# Show the plot
plt.show()
```





The graph presents a comparative analysis of two models—one based on GDP and the other on GDP Per Capita. The performance metrics shown are Mean Squared Error (MSE) and R<sup>2</sup> Score.

Interpretation:

- 1. **MSE (Mean Squared Error):**

- Represented by the blue bars on the left y-axis.
- The GDP Model has a higher MSE than the GDP Per Capita Model, indicating that the GDP Model has higher errors in its predictions.
- The lower MSE in the GDP Per Capita Model suggests it is more accurate in predicting the target variable.

## 2. $R^2$ Score:

- Represented by the red line on the right y-axis.
- The GDP Model has a slightly higher  $R^2$  score than the GDP Per Capita Model, indicating that it explains slightly more variance in the data.
- The downward trend in the  $R^2$  score from the GDP Model to the GDP Per Capita Model suggests that while the GDP Per Capita Model has lower errors (better MSE), it slightly sacrifices the explained variance.

## Conclusion:

- **Trade-off Between MSE and  $R^2$ :** The plot indicates a trade-off where the GDP Per Capita Model reduces prediction errors (lower MSE) at the cost of a small decrease in the proportion of variance explained (lower  $R^2$  score). This suggests that depending on the application, one might prefer the GDP Per Capita Model for its accuracy or the GDP Model for its explanatory power.

This visual helps in understanding which model might be more suitable depending on the specific goals of the analysis, whether it's minimizing error or maximizing the explained variance.