

AI Coffe Club (09/01/2020)

Activation Functions

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Name	Function	Derivative	Range
Sigmoid	$\sigma(x) = \frac{1}{1+e^{-x}}$	$\sigma'(x) = \sigma(x)(1 - \sigma(x))$	$(0, 1)$
Hyperbolic Tangent	$\sigma(x) = \frac{e^{2x}-1}{e^{2x}+1}$	$\sigma'(x) = 1 - \sigma(x)^2$	$(-1, 1)$
ReLU	$\sigma(x) = \begin{cases} 0 & x \leq 0 \\ x & x > 0 \end{cases}$	$\sigma(x) = \begin{cases} 0 & x \leq 0 \\ x & x > 0 \end{cases}$	$[0, \infty)$
Leaky ReLU	$\sigma(x) = \begin{cases} 0.01x & x \leq 0 \\ x & x > 0 \end{cases}$	$\sigma(x) = \begin{cases} 0.01 & x \leq 0 \\ x & x > 0 \end{cases}$	$(-\infty, \infty)$
Parametric ReLU	$\sigma(x) = \begin{cases} \alpha x & x \leq 0 \\ x & x > 0 \end{cases}$	$\sigma(x) = \begin{cases} \alpha & x \leq 0 \\ x & x > 0 \end{cases}$	$(-\infty, \infty)$
ELU	$\sigma(x) = \begin{cases} \alpha(e^x - 1) & x \leq 0 \\ x & x > 0 \end{cases}$	$\sigma(x) = \begin{cases} \alpha + \sigma(x) & x \leq 0 \\ x & x > 0 \end{cases}$	$(-\alpha, \infty)$
Softplus	$\sigma(x) = \ln(1 + e^x)$	$\sigma'(x) = \frac{1}{1+e^{-x}}$	$(0, \infty)$
Swish	$\sigma(x) = \frac{x}{1+e^{-\beta x}}$	$\sigma'(x) = \beta \sigma(x) + \frac{1}{1+e^{-\beta x}}(1 - \beta \sigma(x))$	

1 Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}} \quad (1)$$

$$\sigma'(x) = \sigma(x)(1 - \sigma(x)) \quad (2)$$

2 Hyperbolic Tangent

$$\sigma(x) = \tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} = \frac{e^{2x} - 1}{e^{2x} + 1} \quad (3)$$

$$\sigma'(x) = 1 - \sigma(x)^2 \quad (4)$$

3 Rectified Linear Unit

$$\sigma(x) = \begin{cases} 0 & x \leq 0 \\ x & x > 0 \end{cases} \quad (5)$$

$$\sigma'(x) = \begin{cases} 0 & x \leq 0 \\ 1 & x > 0 \end{cases} \quad (6)$$

4 Leaky Rectified Linear Unit

$$\sigma(x) = \begin{cases} 0.01x & x \leq 0 \\ x & x > 0 \end{cases} \quad (7)$$

$$\sigma'(x) = \begin{cases} 0.01 & x \leq 0 \\ 1 & x > 0 \end{cases} \quad (8)$$

5 Parametric Rectified Linear Unit

$$\sigma(x) = \begin{cases} \alpha x & x \leq 0 \\ x & x > 0 \end{cases} \quad (9)$$

$$\sigma'(x) = \begin{cases} \alpha & x \leq 0 \\ 1 & x > 0 \end{cases} \quad (10)$$

6 Exponential Linear Unit

$$\sigma(x) = \begin{cases} \alpha(e^x - 1) & x \leq 0 \\ x & x > 0 \end{cases} \quad (11)$$

$$\sigma'(x) = \begin{cases} \alpha + \sigma(x) & x \leq 0 \\ 1 & x > 0 \end{cases} \quad (12)$$

7 Softplus

$$\sigma(x) = \ln(1 + e^x) \quad (13)$$

$$\sigma'(x) = \frac{1}{1 + e^{-x}} \quad (14)$$

8 Swish

$$\sigma(x) = \frac{x}{1 + e^{-x}} \quad (15)$$

$$\sigma'(x) = x\sigma(x) \quad (16)$$