

Assignment 2

SMAI Assignemnt 2
Roll No : 2018113003

Problem 1

False.

There is still an unavoidable error as Y is probabilistic, thus predicting Y is often impossible even if the models's estimate $P(Y)$ is perfect, The perfect predition of $P(Y)$ in itself isn't necceasarly true as Naive Bayes is linear.

Problem 3

Part 1

Given :

$$\begin{aligned}P(\text{Pos}/\text{Cov}) &= 0.9 \\P(\text{Neg}/\text{Cov}') &= 0.97 \\P(\text{Cov}) &= 0.08\end{aligned}$$

Pos -> Positive on Test

Neg -> Negative on Test

Cov -> Corona Positive

Cov' -> Complement of Corona (Corona Negative)

To Find :

$$P(\text{Cov}/\text{Pos})$$

Solution :

$$\begin{aligned}P(\text{Cov}/\text{Pos}) &= (P(\text{Pos}/\text{Cov})P(\text{Cov}))/P(\text{Pos}) \\&= (0.9 * 0.08)/P(\text{Pos}) \\P(\text{Pos}) &= P(\text{Pos}/\text{Cov})P(\text{Cov}) + P(\text{Pos}/\text{Cov}')P(\text{Cov}') \\&= 0.9 * 0.08 + 0.03 * 0.92 \\&= 0.0996 \\P(\text{Cov}/\text{Pos}) &= 0.027/0.0996 \\&= 720/996 \\&= 0.7228\end{aligned}$$

Conclusion

$P(\text{Cov}/\text{Pos}) > 0.5 \Rightarrow$ Probably detect as Corona Positive

Part 2

Given :

$$P(\text{Cov}) = 0.6, \text{ other values as given above}$$

To Find :

$$P(\text{Cov}/\text{Pos})$$

Solution :

$$\begin{aligned}P(\text{Cov}/\text{Pos}) &= (P(\text{Pos}/\text{Cov})P(\text{Cov}))/P(\text{Pos}) \\&= 0.9 * (0.6/P(\text{Pos}))\end{aligned}$$

$$\begin{aligned}P(\text{Pos}) &= P(\text{Pos}/\text{Cov})P(\text{Cov}) + P(\text{Pos}/\text{Cov}')P(\text{Cov}') \\&= 0.9*0.6 + 0.03*0.4 \\&= 0.552\end{aligned}$$

$$\begin{aligned}P(\text{Cov}/\text{Pos}) &= 0.54/0.552 \\&= 540/552 \\&= 0.9781\end{aligned}$$

Conclusion

$P(\text{Cov}/\text{Pos})$ very close to 1, thus highly certain.