

Two protons are a distance of $8 \times 10^{-9} \text{ m}$ apart. What is the electric potential energy of the system.

$$U_g = -\frac{1}{4\pi\epsilon} \frac{Q_1 Q_2}{r}$$

$$= 2.88 \times 10^{-20} \text{ J}$$

Remember that the charge of e is $1.6 \times 10^{-19} \text{ C}$

If the two protons move closer together, the potential energy will ____.

Increase

A proton and electron are a distance of $8 \times 10^{-9} \text{ m}$ apart. What is the electric potential energy of the system?

Negative of the first answer.

$$U_g = -2.88 \times 10^{-20} \text{ J}$$

If the proton and electron move closer together the potential energy ____.

Decreases.

In a location in outer space far from all other objects, a nucleus whose mass is $3.355192 \times 10^{-25} \text{ kg}$ and which is initially at rest undergoes spontaneous "alpha" decay. The original nucleus disappears, and two new particles appear: a He-4 nucleus of mass $6.640678 \times 10^{-27} \text{ kg}$ (an "alpha particle" consisting of two protons and two neutrons) and a new nucleus of mass $3.288706 \times 10^{-25} \text{ kg}$. These new particles move far away from each other, because they repel each other electrically (both are positively charged).

Because the calculations involve the small difference of (comparatively) large numbers, you need to keep 7 significant figures in your calculations, and you need to use the more accurate value for the speed of light, $2.99792 \times 10^8 \text{ m/s}$.

Choose all particles as the system.

Initial state: Original nucleus, at rest.

Final state: Alpha particle + new nucleus, far from each other.

What is the rest energy of the original nucleus?

$$E_i = mc^2$$

$$= 3.355e-25 \text{ J}$$

What is the rest energy of the two new particle?

$$E_f = E_a + E_n$$

$$= c^2(m_a + m_n)$$

$$= 3.015e-8 \text{ J}$$

What is the sum of kinetic energy of the system

$$K = E_f - E_i$$

$$= 7.120e-13 \text{ J}$$

Use energy conservation to find the final speed of a basketball dropped from a height of 2.02m.

$$\Delta E = W$$

$$W = E_f - E_i$$

$$W = \cancel{U_f} + \cancel{K_f} - \cancel{U_i} - K_i$$

$$F_g d = \cancel{\frac{1}{2}} m v^2$$

$$v^2 = \frac{2F_g d}{m}$$

$$v^2 = \frac{\cancel{2} g m d}{\cancel{m}}$$

$$v^2 = 2gd$$

$$v = \sqrt{2gd}$$

$$= 6.292 \text{ m/s}$$

A comet is in an elliptical orbit around the Sun. Its closest approach to the sun is a distance of $4.6 \times 10^7 \text{ m}$ at which point its speed is $9.4 \times 10^4 \text{ m/s}$. Its farthest distance from the sun is far from the orbit of Pluto. What is its speed when it is $6 \times 10^8 \text{ m}$ from the sun.

$$U_i + K_i = \cancel{U_f} + K_f$$

$$-\frac{\cancel{G} M_s M_s}{r_i} + \frac{1}{2} \cancel{M_s} V_i^2 = \frac{1}{2} \cancel{M_s} V_f^2$$

$$V_f^2 = -\frac{2GM_s}{r} + V_i^2$$

$$V_f = \sqrt{-\frac{2GM_s}{r_i} + V_i^2}$$

$$= 55151 \text{ m/s}$$

The radius of Jupiter is $7.15 \times 10^7 \text{ m}$ and has a mass of $1.9 \times 10^{27} \text{ kg}$.
An object is launched straight up from the surface.

What initial speed is needed so that when the object is far from Jupiter its speed is $2.35 \times 10^4 \text{ m/s}$?

$$E_f = E_i + W$$

$$r_i = 7.15 \times 10^7 \text{ m}$$

$$M_J = 1.9 \times 10^{27} \text{ kg}$$

$$V_f = 2.35 \times 10^4 \text{ m/s}$$

$$\cancel{U_f} + K_f = U_i + K_i + 0$$

$$\frac{1}{2} \cancel{M_o} V_f^2 = - \frac{GM_J \cancel{M_o}}{r_i} + \frac{1}{2} \cancel{M_o} V_i^2$$

$$\frac{1}{2} V_f^2 = - \frac{GM_J}{r_i} + \frac{1}{2} V_i^2$$

$$V_i^2 = \frac{2GM_J}{r_i} + V_f^2$$

$$V_i = \sqrt{\frac{2GM_J}{r_i} + V_f^2}$$

$$= 64133 \text{ m/s}$$

What is the escape velocity?

$$V_i = \sqrt{\frac{2GM_J}{r_i} + \cancel{V_f^2}}$$

$$= 59672 \text{ m/s}$$