

A straight wire of length 0.74 m carries a conventional current of 0.7 amperes. What is the magnitude of the magnetic field made by the current at a location 3.2 cm from the wire? Use both the exact formula and the approximate formula to calculate the field.

(a) result using exact formula

$B =$ T

(b) result using approximate formula

$B =$ T

Part One

$$B = \frac{\mu_0}{4\pi} \frac{LI}{r \sqrt{r^2 + (\frac{L}{2})^2}}$$

$$= 4.359 \times 10^{-6} \text{ T}$$

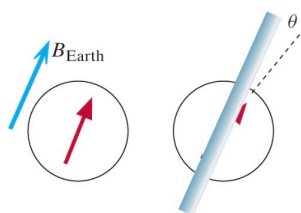
Part Two

$$B = \frac{\mu_0}{4\pi} \frac{2I}{r}$$

$$= 4.375 \times 10^{-6} \text{ T}$$

Deflecting a compass needle

When you bring a current-carrying wire down onto the top of a compass, aligned with the original direction of the needle and 7 mm above the needle, the needle deflects by $\theta = 9$ degrees (see the figure).



(a) Which of the following statements are correct? Select all that apply.

- ☐ The magnetic field under the wire, due to the current, points North.
- ☒ Conventional current in the wire is flowing downward (South).
- ☒ The magnetic field under the wire, due to the current, points to the East.
- ☒ Electron current in the wire is flowing upward (North).
- ☐ Conventional current in the wire flows upward (North).
- ☐ The magnetic field under the wire, due to the current, points to the West.



(b) Calculate the amount of conventional current flowing in the wire. The measurement was made at a location where the horizontal component of the Earth's magnetic field is $B_{\text{Earth}} \approx 2$

$\times 10^{-5}$ tesla.

A

$$\tan(\theta) = \frac{|\vec{B}_{\text{wire}}|}{|\vec{B}_{\text{Earth}}|}$$

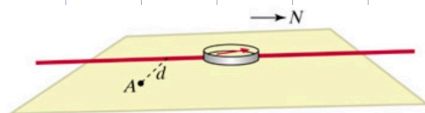
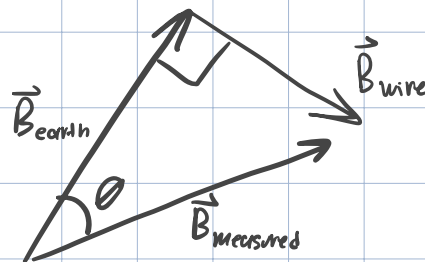
$$|\vec{B}_{\text{wire}}| = \tan(\theta) |\vec{B}_{\text{earth}}|$$

$$\frac{\mu_0}{4\pi} \frac{2I}{r} = \tan(\theta) |\vec{B}_{\text{earth}}|$$

$$I = \frac{1}{2} r \tan(\theta) |\vec{B}_{\text{earth}}| \frac{1}{\frac{\mu_0}{4\pi}}$$

$$= \frac{1}{2 \frac{\mu_0}{4\pi}} r \tan(\theta) |\vec{B}_{\text{earth}}|$$

$$= 0.11087 \text{ A}$$



A long current-carrying wire, oriented North-South, lies on a table (it is connected to batteries which are not shown). A compass lies **on top of the wire**, with the compass needle about **3 mm** above the wire. With the current running, the compass deflects **13** degrees to the **West**. At this location, the horizontal component of the Earth's magnetic field is about $2\text{e-}5$ tesla.

What is the magnitude of the magnetic field at location A, on the table top, a distance **2.8** cm to the East of the wire, due only to the current in the wire?

$|\vec{B}| =$ tesla

What is the direction of the magnetic field at location A, due only to the current in the wire?

Equation from the problem above

$$I = \frac{1}{2 \frac{\mu_0}{4\pi}} r_{\text{compass}} \tan(\theta) B_{\text{earth}}$$

$$B_{\text{obs}} = \frac{\mu_0}{4\pi} \frac{2 \left(\frac{1}{2 \frac{\mu_0}{4\pi}} r_{\text{compass}} \tan(\theta) B_{\text{earth}} \right)}{r_{\text{obs}}}$$

$$= \frac{r_{\text{compass}} \tan(\theta) B_{\text{earth}}}{r_{\text{obs}}}$$

$$= 4.947\text{e-}7 \text{ T}$$

