

Homework 1

Use a separate piece of paper for each problem. Solutions with clear reasoning and correct results receive full points. Solutions with clear reasoning and incorrect results receive 3/4 of the total points. Solutions with current results but no rationale receive no points.

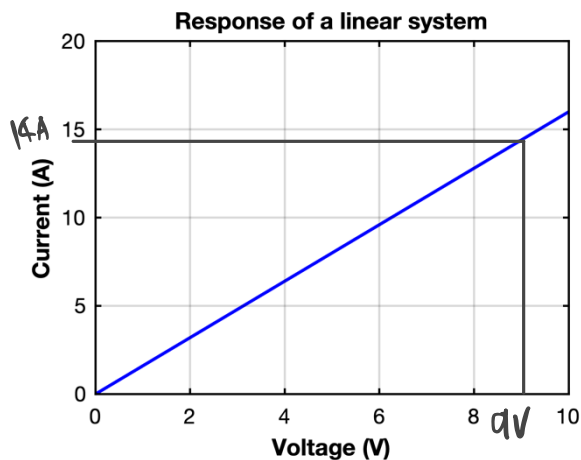
Problem 1: A piece of iron is cut into a rectangular shape with dimensions of 1 m long, 10 cm wide and 50 mm tall.

- What is the resistance? (5 points)
- If the materials is changed to copper and using the same dimensions what is the resistance? (10 points)
- What would be the dimensions of a rectangular shape piece of copper such as the resistance value is same as in "a)"? (5 points)

$$\rho_{\text{fe}} = 1 \times 10^{-7} \, \Omega \cdot \text{m}, \rho_{\text{cu}} = 1.68 \times 10^{-8} \, \Omega \cdot \text{m}.$$

Problem 2: Analyze the following IV curve and:

- Find the slope. (3 points)
- If this is a single resistor connected to a 9 V ideal battery, what is the current that flows across the resistor? (2 points)



Problem 3: A thermistor is a temperature dependent resistor whose resistance is modeled via the modified Steinhart Hart equation:

$$\frac{1}{T} = \frac{1}{T_0} + \frac{1}{B} \ln \left(\frac{R}{R_0} \right)$$

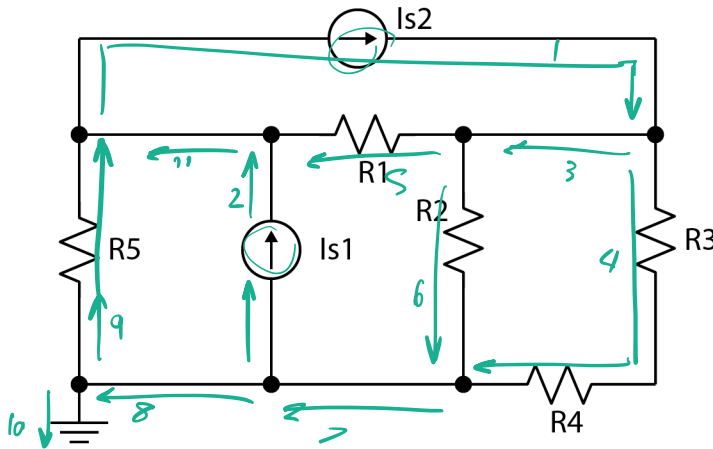
where R_0 is the resistance value at a reference temperature T_0 , and B is the thermistor parameter given by the vendor in units of Kelvin [K]. Consider a thermistor sold by Murata (NCP03WF104) whose $R_0 = 100 \, \text{k}\Omega$ at $T_0 = 25 \, ^\circ\text{C}$ and $B = 4250 \, \text{K}$.

- Calculate the Resistance value at $15 \, ^\circ\text{C}$. (5 points)
- Calculate the Resistance value at $35 \, ^\circ\text{C}$. (5 points)
- What is the change in resistance between those two temperatures. (5 points)

Problem 4: In a circular gold conductor 100 m long and 1mm in diameter flows a 5A current. What is the voltage across that conductor? (10 points)

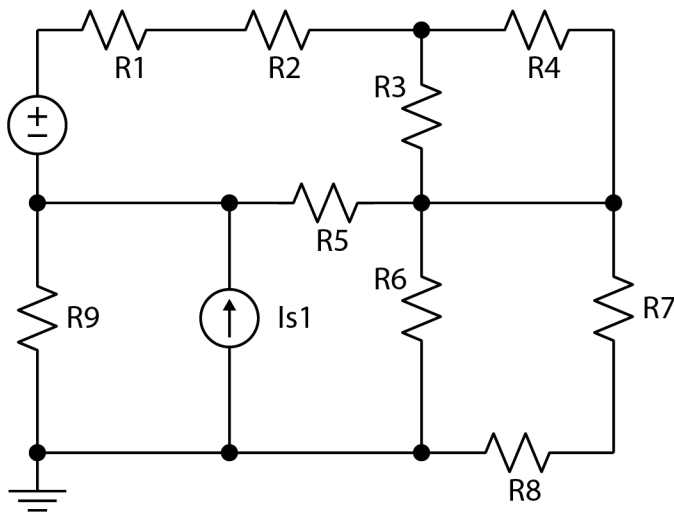
Problem 5: Consider the following electrical circuit.

- Identify the number of nodes, branches, and loops. (10 points)
- Write the KVL equation on all the loops. (15 points)



Problem 6: Consider the following electrical circuit.

- Identify the number of nodes, branches, and loops. (10 points)
- Write the KCL equation at each node. Define your current. (15 points)



Problem 1a

$$R = \rho_{rc} \frac{L}{A}$$

$$A = wh$$

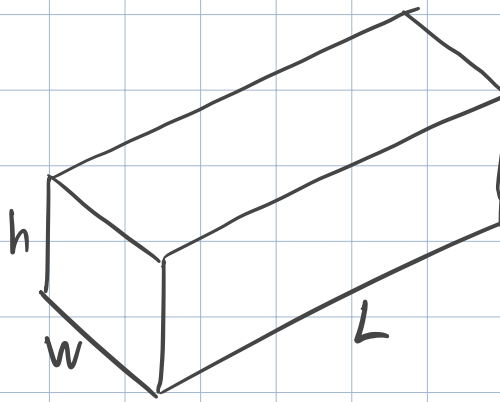
$$R = \rho_{rc} \frac{L}{wh}$$

$$L = 1 \text{ m}$$

$$\begin{aligned} w &= 10 \text{ cm} \\ &= 0.1 \text{ m} \end{aligned}$$

$$\begin{aligned} h &= 50 \text{ mm} \\ &= 0.05 \text{ m} \end{aligned}$$

$$R = 2e-5 \Omega$$



Problem 1b

$$R = \rho_{cu} \frac{L}{wh}$$

$$L = 1 \text{ m}$$

$$w = 0.1 \text{ m}$$

$$h = 0.05 \text{ m}$$

$$R = 3.36e-6 \Omega$$

Problem 1c

$$R = \rho_{cu} \frac{L}{wh}$$

Let only L change to change resistance

$$\frac{R}{\rho_{cu}} = \frac{L}{wh}$$

$$L = \frac{Rwh}{\rho_{cu}}$$

$$R = 2e^{-5} \Omega$$

$$w = 0.1 \text{ m}$$

$$h = 0.05 \text{ m}$$

$$L = 5.95 \text{ m}$$

Problem 2a

$$P_1 = (0, 0)$$

$$P_2 = (6, 9)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{9}{6}$$

$$= \frac{3}{2}$$

Problem 2b

14 A, see graph above for work

Problem 3a

$$\frac{1}{T} = \frac{1}{T_0} + \frac{1}{B} \ln\left(\frac{R}{R_0}\right)$$

$$R_0 = 100 \text{ k}\Omega = 100,000 \Omega$$

$$100 \text{ k}\Omega \cdot \frac{1000 \Omega}{1 \text{ k}\Omega}$$

$$B\left(\frac{1}{T} - \frac{1}{T_0}\right) = \ln\left(\frac{R}{R_0}\right)$$

$$T_0 = 25^\circ \text{C} = 298.15 \text{ K}$$

$$\frac{R}{R_0} = e^{B\left(\frac{1}{T} - \frac{1}{T_0}\right)}$$

$$B = 4250 \text{ K}$$

$$R(T) = R_0 e^{B\left(\frac{1}{T} - \frac{1}{T_0}\right)}$$

$$R(13^\circ \text{C}) = R(288.15 \text{ K}) = 164,000 \Omega$$

Problem 3b

$$R(35^\circ \text{C}) = R(308.15 \text{ K}) = 62,965 \Omega$$

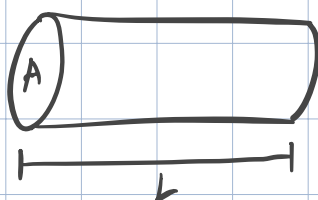
Problem 3c

$$R(15^\circ \text{C}) - R(35^\circ \text{C}) = 101035 \Omega$$

Problem 4

$$R = \rho \frac{L}{A}$$

$$A = \pi r^2$$



$$\text{Ohm's Law : } R = \frac{V}{I}$$

$$\frac{V}{I} = \rho \frac{L}{A}$$

$$V = \frac{\rho L I}{A}$$

$$L = 100 \text{ m}$$

$$I = 5 \text{ A}$$

$$d = 1 \text{ mm} \\ = 0.001 \text{ m}$$

$$V = \frac{\rho L I}{\pi r^2}$$

$$2r = d \rightarrow r = \frac{d}{2}$$

$$V = \frac{\rho L I}{\pi \left(\frac{d}{2}\right)^2}$$

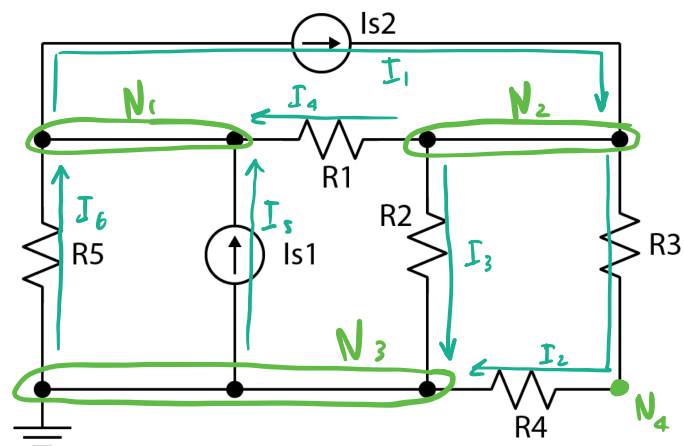
$$= 15.534 \text{ V}$$

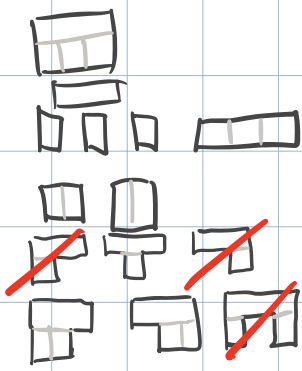
Problem 5a

Nodes : 4

Branches : 6

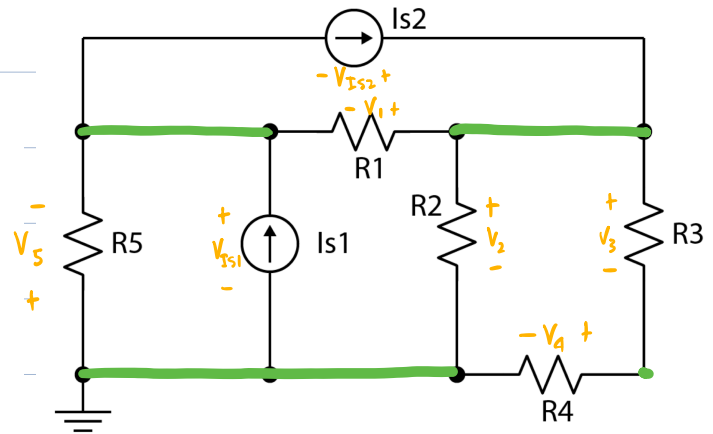
Loops : 11





Problem 5b

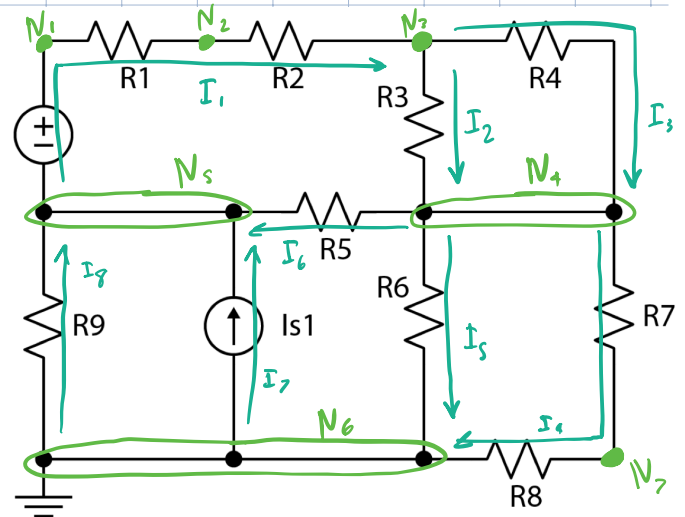
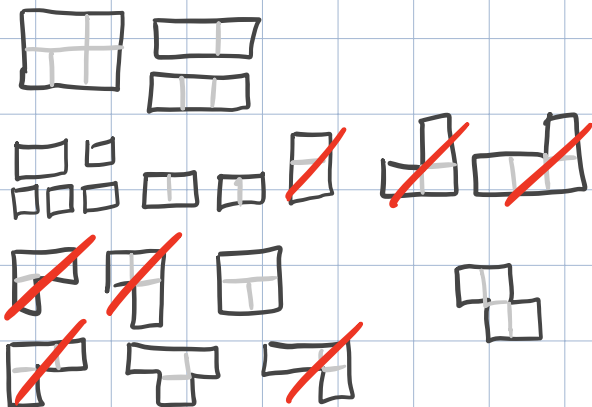
- KVL on Loop: $R5 - Is1 \rightarrow V5 + V_{Is1} = 0$
- KVL on loop: $Is1 - R1 - R2 \rightarrow -V_{Is1} - V_1 + V_2 = 0$
- KVL on loop: $R2 - R3 - R4 \rightarrow -V_2 + V_3 + V_4 = 0$
- KVL on loop: $Is2 - R1 \rightarrow V_1 - V_{Is2} = 0$
- KVL on loop: $R5 - R1 - R2 \rightarrow V5 - V_1 + V_2 = 0$
- KVL on loop: $Is1 - R1 - R3 - R4 \rightarrow -V_{Is1} - V_1 + V_3 + V_4 = 0$
- KVL on loop: $Is1 - Is2 - R2 \rightarrow -V_{Is1} - V_{Is2} + V_2 = 0$
- KVL on loop: $R5 - R1 - R3 - R4 \rightarrow V5 - V_1 + V_3 + V_4 = 0$
- KVL on loop: $R5 - Is2 - R2 \rightarrow V5 - V_{Is2} + V_2 = 0$
- KVL on loop: $Is1 - Is2 - R3 - R4 \rightarrow -V_{Is1} - V_{Is2} + V_3 + V_4 = 0$
- KVL on loop: $R5 - Is2 - R3 - R4 \rightarrow V5 - V_{Is2} + V_3 + V_4 = 0$



← From the key

Problem 6a

Nodes: 7
Branches: 8
Loops: 15





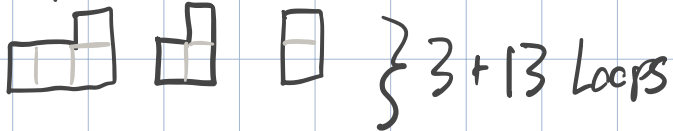
Problem 6a

Nodes: 7

Branches: 9

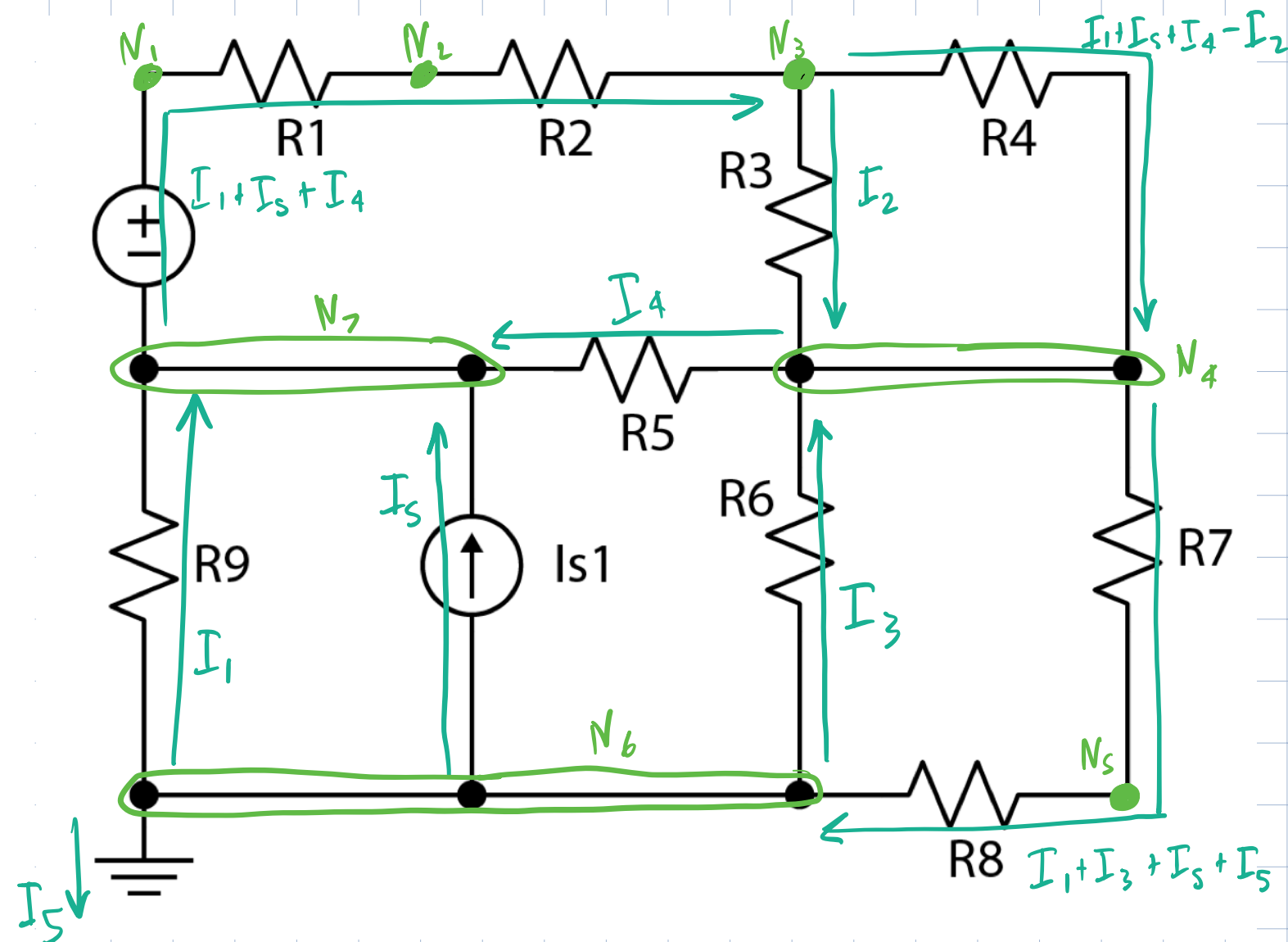
Loops: 16

All previous loops in Q5 and



Problem 6b

5 backyards - 1 current source = 4 unknowns



$$N_1: I_1 + I_s + I_4 - (I_1 + I_s + I_4) = 0$$

$$N_2: I_1 + I_s + I_4 - (I_1 + I_s + I_4) = 0$$

$$N_3: -(I_1 + I_s + I_4) + I_2 + (I_1 + I_s + I_4 - I_2) = 0$$

$$N_4: \cancel{-(I_1 + I_s + I_4 - I_2)} - I_2 - I_3 \cancel{-(I_1 + I_3 + I_s + I_5)} + I_4 = 0$$

$$-I_2 - I_3 + I_4 = 0$$

$$N_5: -(I_1 + I_3 + I_s + I_5) + (I_1 + I_3 + I_s + I_5)$$

$$N_6: -(\cancel{I_1} + \cancel{I_3} + I_s + \cancel{I_5}) + \cancel{I_3} + \cancel{I_5} + \cancel{I_1} + I_6 = 0$$

$$-I_s + I_6 = 0$$

$$N_2: -I_4 - I_s - I_1 + (I_1 + I_s + I_4) = 0$$