

A chain of 40 identical springs linked end to end has a stiffness of  $470 \text{ N/m}$ . What is the stiffness of one spring?

$$k_{n \text{ springs}} = \frac{1}{n} k_{1 \text{ spring}}$$

$$470 = \frac{1}{40} k_{1 \text{ spring}}$$

$$k_{1 \text{ spring}} = 18800 \text{ N/m}$$

10 identical springs are placed side by side and are connected to a massive block. The stiffness of the 10 springs combined is  $4400 \text{ N/m}$ . What is the stiffness of one spring?

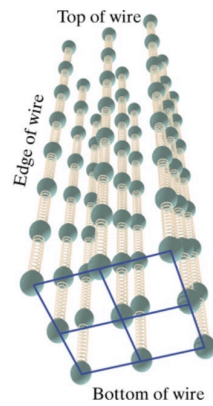
$$k_{n \text{ springs}} = n \cdot k_{1 \text{ spring}}$$

$$4400 = 10 k_{1 \text{ spring}}$$

$$k_{1 \text{ spring}} = 440 \text{ N/m}$$

One mole of **iron** ( $6 \times 10^{23}$  atoms) has a mass of **56** grams, and its density is **7.87** grams per cubic centimeter, so the center-to-center distance between atoms is  $2.28 \times 10^{-10}$  m. You have a long thin bar of **iron**, **2.1** m long, with a square cross section, **0.11** cm on a side.

You hang the rod vertically and attach a **125** kg mass to the bottom, and you observe that the bar becomes **1.06** cm longer. From these measurements, it is possible to determine the stiffness of one interatomic bond in **iron**.



1) What is the spring stiffness of the entire wire, considered as a single macroscopic (large scale), very stiff spring?

$$k_s = \boxed{\phantom{000000}} \text{ N/m}$$

2) How many side-by-side atomic chains (long springs) are there in this wire? This is the same as the number of atoms on the bottom surface of the **iron** wire. Note that the cross-sectional area of one **iron** atom is  $(2.28 \times 10^{-10})^2 \text{ m}^2$ .

$$\text{Number of side-by-side long chains of atoms} = \boxed{\phantom{000000}}$$

3) How many interatomic bonds are there in one atomic chain running the length of the wire?

$$\text{Number of bonds in total length} = \boxed{\phantom{000000}}$$

4) What is the stiffness of a single interatomic "spring"?

$$k_{s,i} = \boxed{\phantom{000000}} \text{ N/m}$$

An interatomic bond in **iron** is stiffer than a slinky, but less stiff than a pogo stick. The stiffness of a single interatomic bond is very much smaller than the stiffness of the entire wire.

Part One

$$F = k_s$$

$$mg = k_s$$

$$(125 \text{ kg})(9.8 \text{ m/s}^2) = k(0.011 \text{ m})$$

$$k_{\text{wire}} = 1.1557 \times 10^5 \text{ N/m}$$

Part Two

$$N_{\text{parallel}} = W_{\text{atoms}}^2$$

$$= \left( \frac{0.0011 \text{ m}}{2.28 \times 10^{-10} \text{ m}} \right)^2$$

$$= 2.327e13 \text{ atoms}$$

Part 3

$$n_{\text{series}} = \left( \frac{2.1 \text{ m}}{2.28e-10 \text{ m}} \right)$$

$$= 9.211e9$$

Part 4

$$k_{\text{wire}} = \left( \frac{1}{n_{\text{series}} \cdot n_{\text{parallel}}} \right) k_{\text{bond}}$$

$$k_{\text{bond}} = \frac{k_{\text{wire}} n_{\text{series}}}{n_{\text{parallel}}}$$

$$= 45.746 \text{ N/m}$$

A hanging wire made of Iron with a diameter of 0.12 cm is 2.8 m long initially. When a mass of 120 kg is hung from it, it stretches 0.0146 m. 1 mol Fe = 56 grams and its density is 7.87 g/cm<sup>3</sup>. What is Young's modulus?

$$\text{Stress} = \frac{F_t}{A}$$

$$= \frac{mg}{\pi \left( \frac{d}{2} \right)^2}$$

$$= 1.0398e9 \text{ N/m}^2$$

$$\text{Strain} = \frac{\Delta L}{L}$$

$$= \frac{0.0146 \text{ m}}{2.8 \text{ m}}$$

$$= 5.214e-3$$

$$Y = \frac{\text{Stress}}{\text{Strain}} = 1.994 \text{e}11 \text{ N/m}^2$$

Find the spring stiffness if the diameter of one atom of Iron is  $2.28 \text{e}-10$ .

$$Y = \frac{k_b}{d}$$

$$k_b = Yd$$

$$= 45.467$$