

The mass of the sun is $2e30$ kg, and the mass of the Earth is $6e24$ kg.
The distance from the sun to the earth is $1.5e11$ m.

Calculate the magnitude of the gravitational force exerted by the Sun on the Earth.

$$\begin{aligned} |\vec{F}_g| &= G \frac{m_s m_e}{|\vec{r}|^2} \\ &= 6.7e-11 \frac{2e30 \cdot 6e24}{1.5e11^2} \\ &= 3.5733e22 \text{ N} \end{aligned}$$

Calculate the magnitude of the gravitational force exerted by the Earth on the Sun.

Same magnitude

$$|\vec{F}_g| = 3.5733e22 \text{ N}$$

Calculate the magnitude of the gravitational force exerted by Mercury on a 60 kg human standing on the surface of Mercury. Mercury has a mass of $3.3e23$ kg and a radius of $2.4e6$ m.

$$|\vec{F}_g| = G \frac{m_1 m_2}{|\vec{r}|^2}$$

$$\hookrightarrow |\vec{r}| = 2.4e6 \text{ m}$$

$$|\vec{F}_g| = 230.3125$$

A planet of mass $3e24$ kg is at location $\langle 5e11, -5e11, 0 \rangle$. A star of mass $4e30$ kg is at location $\langle -5e11, 5e11, 0 \rangle$.

What is the position vector from the planet to the star?

$$\begin{aligned}\vec{r}_{p \rightarrow s} &= \vec{r}_s - \vec{r}_p \\ &= \langle -10e11, 10e11, 0 \rangle \text{ m}\end{aligned}$$

What is the magnitude of this vector?

$$\begin{aligned}|\vec{r}_{p \rightarrow s}| &= \sqrt{(-10e11)^2 + (10e11)^2} \\ &= 1.4142e12 \text{ m}\end{aligned}$$

What is the unit vector of this vector?

$$\begin{aligned}\hat{r}_{p \rightarrow s} &= \frac{\vec{r}}{|\vec{r}|} \\ &= \langle -0.7071, 0.7071, 0 \rangle\end{aligned}$$

What is the magnitude of force exerted on the planet by the star?

$$\begin{aligned}|\vec{F}_g| &= G \frac{m_1 m_2}{|\vec{r}|^2} \\ &= 4.0326e20 \text{ N}\end{aligned}$$

What is the force vector for the force exerted on the planet by the star?

$$\vec{F}_g = |\vec{F}_g| \hat{r}$$

$$= \langle -2.8155e20, 2.8155e20, 0 \rangle \text{ N}$$

A planet of mass $7e24 \text{ kg}$ is at location $\langle -3e11, 8e11, 0 \rangle \text{ m}$. A star of mass $9e30 \text{ kg}$ is at location $\langle 5e11, -5e11, 0 \rangle \text{ m}$. What is the force exerted on the planet by the star?

$$\vec{F}_{\text{gravity on p by s}} = |\vec{F}_g| \cdot \hat{r}_{p \text{ to } s}$$

$$\hookrightarrow |\vec{F}_g| = G \frac{m_1 m_2}{|\vec{r}_{p \text{ to } s}|^2}$$

$$\hookrightarrow \vec{r}_{p \text{ to } s} = \vec{r}_s \text{ to } \vec{r}_p$$

$$= \langle 8e11, -13e11 \rangle \text{ m}$$

$$\hookrightarrow |\vec{r}_{p \text{ to } s}| = 1.5264e12 \text{ m}$$

$$|\vec{F}_g| = 1.8116e21$$

$$\hookrightarrow \hat{r}_{p \text{ to } s} = \frac{\vec{r}}{|\vec{r}|}$$

$$= \langle 0.5241, -0.8517, 0 \rangle$$

$$\vec{F}_{\text{gravity on p by s}} = \langle 9.495e20, -1.543e21, 0 \rangle$$

