

# Prim算法和Dijkstra算法实验报告

2021100733

陈旭天

## • 手工部分

下午 10:40 11月20日周日 88%

随手记

Prim 算法求最小生成树  $V = \{0, 1, 2, 3, 4, 5\}$

$U = \{0\}$   $TE = \emptyset$

①

$U = \{0, 5\}$   $TE = \{(0, 5)\}$

①  
⑤

$U = \{0, 4, 5\}$   $TE = \{(0, 5), (4, 5)\}$

①  
⑤  
④

$U = \{0, 3, 4, 5\}$   $TE = \{(0, 5), (4, 5), (4, 3)\}$

①  
⑤  
④  
③

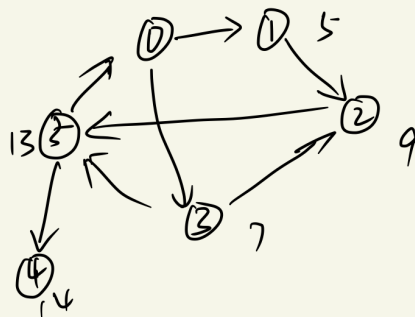
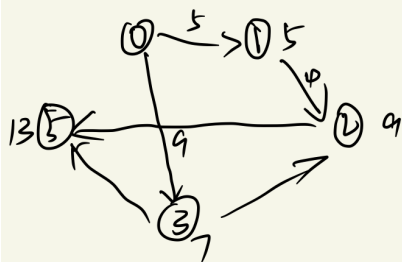
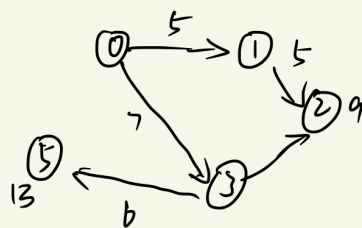
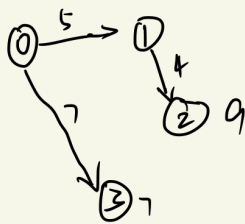
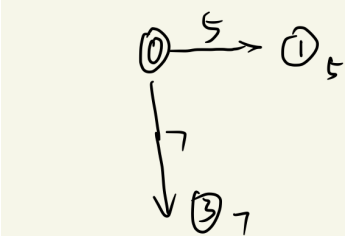
$U = \{0, 2, 3, 4, 5\}$   $TE = \{(0, 5), (5, 4), (4, 3), (3, 2)\}$

①  
⑤  
④  
③  
②

$U = \{0, 1, 2, 3, 4, 5\}$   $TE = \{(0, 5), (5, 4), (4, 3), (3, 2), (2, 1)\}$

①  
⑤  
④  
③  
②  
①

①  
⑤  
④  
③  
②  
①



1 : 5  
 2 : 9  
 3 : 7  
 5 : 13  
 4 : 14

## 实验源码

- Source Code for Prim

```

#include<iostream>
#include<vector>
using namespace std;
void prim(vector<vector<int>> &VGraph, vector<int> &lowcost,
vector<int> &closest, vector<bool> &visited)
{
    int size = lowcost.size();
    visited[0] = true;
    for (int i = 1; i < size; i++)
    {
        lowcost[i] = VGraph[0][i];
        closest[i] = 0;
        visited[i] = false;
    }
    cout << "0";
    int weight = 0;
    for (int i = 0; i < size; i++)
    {
        int min = 99999;
        int index = 1;
        for (int j = 0; j < size; j++)
        {
            if (lowcost[j] < min&&!visited[j])
            {
                min = lowcost[j];
                index = j;
            }
        }
        if (index == 1 && min == 99999)
        {
            cout <<
"\n the value of min shengcheng Tree is:"
<< weight<<endl;
            return;
        }
        else
        {
            weight += min;
        }
        cout << " -> " << index;
        visited[index] = true;
        for (int j = 1; j <size; j++)
        {
            if ((VGraph[index][j]<lowcost[j]) && (!visited[j]))
            {
                lowcost[j] = VGraph[index][j];
                closest[j] = index;
            }
        }
    }
}

```

```

}
int main()
{
    int M, N;
    cin >>M>>N;
    vector<vector<int>> VGraph(M);
    vector<int> lowcost(M);
    vector<int> closest(M);
    vector<bool> visited(M);
    for (int i = 0; i < M; i++)
    {
        VGraph[i].resize(M);
    }
    for (int i = 0; i < M; i++)
    {
        for (int j = 0; j < M; j++)
        {
            VGraph[i][j] = 99999;
        }
    }
    for (int i = 0; i < N; i++)
    {
        int a, b;
        cin >> a >> b;
        int length;
        cin >> length;
        VGraph[a][b] = VGraph[b][a] = length;
    }
    prim(VGraph, lowcost, closest, visited);
}

```

- `Source Code for Dijkstra`

```

#include<stdlib.h>
#include<vector>
#include<cstdio>
#include<iostream>

#define NumVertex 6
#define NumEdge 10
#define NotAVertex (-1)
#define Infinity 10000

using namespace std;

struct edge
{
    int from;
    int to;
    int value;
    /* data */
};

typedef struct edge Graph[NumEdge];

struct vertex
{
    vector<pair<int,int>> List;
    bool known;
    int dist;
    int path;
    /* data */
};

typedef struct vertex Table[NumVertex];

// typedef int vertex;

void ReadGraph(Graph G,Table T){
    for(int i = 0;i < NumEdge;++i){
        T[G[i].from].List.push_back(make_pair(G[i].to,G[i].value));
    }
}

void InitTable(int start,Graph G,Table T){
    ReadGraph(G,T);
    for(int i = 0;i < NumVertex; ++i){
        T[i].known = false;
        T[i].dist = Infinity;
        T[i].path = NotAVertex;
    }
}

```

```

    T[start].dist = 0;
}

void PrintPath(int V, Table T){

    if(T[V].path != NotAVertex){
        PrintPath(T[V].path, T);
        //recursion to print shortest path to V.
        printf(" to");
    }
    printf("%d",V);
}

void Dijkstra( Table T){
    int V = NumVertex - 1, W;
    int cnt = 1;
    for(;;){
        for(int i = 0; i < NumVertex; ++i){
            if(!T[i].known && T[i].dist < Infinity){
                if(T[V].dist > T[i].dist) V = i;
            }
        }
        T[V].known = true;
        cnt++;
        for(pair<int,int> a:T[V].List){
            W = a.first;
            if(!T[W].known){
                if(T[V].dist + a.second < T[W].dist){
                    T[W].dist = T[V].dist + a.second;
                    // update the shortest path for each W
                    T[W].path = V;
                    // update the closest vertex for W
                }
            }
        };

        }
        V = W;    // refresh the value of V is quite crucial.
        if(cnt == NumVertex){
            break;
        }
    }
}

int main(void){
    Graph G = {{0,1,5},{0,3,7},{1,2,4},
               {3,2,5},{3,5,6},{2,0,8},
               {2,5,9},{5,0,3},{5,4,1},
               {4,3,5}};

    Table T;
    InitTable(0,G,T);
}

```

```

Dijkstra(T);
// T[5].path = 4;
cout << "the path to 1: ";
PrintPath(1,T);
printf("\n");
cout << "the path to 2: ";
PrintPath(2,T);
printf("\n");
cout << "the path to 3: ";
PrintPath(3,T);
printf("\n");
cout << "the path to 4: ";
PrintPath(4,T);
printf("\n");
cout << "the path to 5: ";
PrintPath(5,T);
return 0;
}

```

- 实验程序输出验证

- Prim

```

0 1 5
0 3 7
1 2 4
3 2 5
3 5 6
2 0 8
2 5 9
5 0 3
5 4 1
4 3 5
0 -> 5 -> 4 -> 1 -> 2 -> 3
the value of min shengcheng Tree is:18

```

- Dijkstra

```
PS C:\Users\36126\c语言\DataStructureEX> cd "c:\
jkstra } ; if ($?) { .\Dijkstra }
the path to 1: 0 to1
the path to 2: 0 to1 to2
the path to 3: 0 to3
the path to 4: 0 to3 to5 to4
the path to 5: 0 to3 to5
```