IN3050 assignment 3

April 22, 2022

1 IN3050/IN4050 Mandatory Assignment 3: Unsupervised Learning

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1.0.1 Rules

website: Before begin the exercise, review the rules atthis you https://www.uio.no/english/studies/examinations/compulsory-activities/mn-ifi-mandatory.html , in particular the paragraph on cooperation. This is an individual assignment. not allowed to deliver together or copy/share source-code/answers with others. Read also the "Routines for handling suspicion of cheating and attempted cheating at the University of Oslo" https://www.uio.no/english/about/regulations/studies-examinations/routinescheating.html By submitting this assignment, you confirm that you are familiar with the rules and the consequences of breaking them.

1.0.2 Delivery

Deadline: Friday, April 22, 2022, 23:59

Your submission should be delivered in Devilry. You may redeliver in Devilry before the deadline, but include all files in the last delivery, as only the last delivery will be read. You are recommended to upload preliminary versions hours (or days) before the final deadline.

1.0.3 What to deliver?

You are recommended to solve the exercise in a Jupyter notebook, but you might solve it in a Python program if you prefer.

If you choose Jupyter, you should deliver the notebook. You should answer all questions and explain what you are doing in Markdown. Still, the code should be properly commented. The notebook should contain results of your runs. In addition, you should make a pdf of your solution which shows the results of the runs.

If you prefer not to use notebooks, you should deliver the code, your run results, and a pdf-report where you answer all the questions and explain your work.

Your report/notebook should contain your name and username.

Deliver one single zipped folder (.zip, .tgz or .tar.gz) which contains your complete solution.

Important: if you weren't able to finish the assignment, use the PDF report/Markdown to elaborate on what you've tried and what problems you encountered. Students who have made an effort and attempted all parts of the assignment will get a second chance even if they fail initially. This exercise will be graded PASS/FAIL.

1.0.4 Goals of the exercise

This exercise has three parts. The first part is focused on Principal Component Analysis (PCA). You will go through some basic theory, and implent PCA from scratch to do compression and visualization of data.

The second part focuses on clustering using K-means. You will use scikit-learn to run K-means clustering, and use PCA to visualize the results.

The last part ties supervised and unsupervised learning together in an effort to evaluate the output of K-means using a logistic regression for multi-class classification approach.

The master students will also have to do one extra part about tuning PCA to balance compression with information lost.

1.0.5 Tools

You may freely use code from the weekly exercises and the published solutions. In the first part about PCA you may **NOT** use ML libraries like scikit-learn. In the K-means part and beyond we encurage the use of scikit-learn to iterate quickly on the problems.

1.0.6 Beware

This is a new assignment. There might occur typos or ambiguities. If anything is unclear, do not hesitate to ask. Also, if you think some assumptions are missing, make your own and explain them!

1.1 Principal Component Analysis (PCA)

In this section, you will work with the PCA algorithm in order to understand its definition and explore its uses.

1.1.1 Principle of Maximum Variance: what is PCA supposed to do?

First of all, let us recall the principle/assumption of PCA:

- 1. What is the variance?
- 2. What is the covariance?
- 3. How do we compute the covariance matrix?

- 4. What is the meaning of the principle of maximum variance?
- 5. Why do we need this principle?
- 6. Does the principle always apply?

Answers: Enter your answers here. 1) Variance determines the distance between the scatter points around the exploratory data. A higher variance means a wider radius of exploration

- 2) Covariance is the direction of the eigenvectors in which the scatter points are placed
- 3) Covariance can be calculated by matrix multiplying the transposed of the matrix with the non-transposed matrix. The answer determines the direction of the eigenvectors in the scatter plot
- 4) By finding the maximum variance we are finding the weights of the eigenvectors in our covariance.
- 5) By applying this principle we minimize the mean squared error.
- 6) This principle wont apply when dealing with diagonal matrices.

1.2 Implementation: how is PCA implemented?

Here we implement the basic steps of PCA and we assemble them.

1.2.1 Importing libraries

We start importing the *numpy* library for performing matrix computations, the *pyplot* library for plotting data, and the *syntheticdata* module to import synthetic data.

```
[3]: import numpy as np import matplotlib.pyplot as plt import syntheticdata
```

1.2.2 Centering the Data

Implement a function with the following signature to center the data as explained in Marsland.

```
[13]: def center_data(A):
    # INPUT:
    # A    [NxM] numpy data matrix (N samples, M features)
    #
    # OUTPUT:
    # X    [NxM] numpy centered data matrix (N samples, M features)

m = np.mean(A, axis = 0)
A -= m
```

```
return A
```

Test your function checking the following assertion on testcase:

1.2.3 Computing Covariance Matrix

Implement a function with the following signature to compute the covariance matrix as explained in *Marsland*.

```
[15]: def compute_covariance_matrix(A):
    # INPUT:
    # A    [NxM] centered numpy data matrix (N samples, M features)
    #
    # OUTPUT:
    # C    [MxM] numpy covariance matrix (M features, M features)
    #
    # Do not apply centering here. We assume that A is centered before this
    → function is called.
    C = np.cov(np.transpose(A))
    return C
```

Test your function checking the following assertion on testcase:

1.2.4 Computing eigenvalues and eigenvectors

Use the linear algebra package of numpy and its function np.linalg.eig() to compute eigenvalues and eigenvectors. Notice that we take the real part of the eigenvectors and eigenval-

ues. The covriance matrix *should* be a symmetric matrix, but the actual implementation in compute_covariance_matrix() can lead to small round off errors that lead to tiny imaginary additions to the eigenvalues and eigenvectors. These are purely numerical artifacts that we can safely remove.

Note: If you decide to NOT use np.linalg.eig() you must make sure that the eigenvalues you compute are of unit length!

Test your function checking the following assertion on testcase:

```
[18]: testcase = np.array([[2,0,0],[0,5,0],[0,0,3]])
    answer1 = np.array([2.,5.,3.])
    answer2 = np.array([[1.,0.,0.],[0.,1.,0.],[0.,0.,1.]]))
    x,y = compute_eigenvalue_eigenvectors(testcase)
    np.testing.assert_array_almost_equal(x, answer1)
    np.testing.assert_array_almost_equal(y, answer2)
```

1.2.5 Sorting eigenvalues and eigenvectors

Implement a function with the following signature to sort eigenvalues and eigenvectors as explained in *Marsland*.

Remember that eigenvalue eigval[i] corresponds to eigenvector eigvec[:,i].

```
[19]: def sort_eigenvalue_eigenvectors(eigval, eigvec):
    # INPUT:
    # eigval [D] numpy vector of eigenvalues
    # eigvec [DxD] numpy array of eigenvectors
#
# OUTPUT:
```

```
# sorted_eigval [D] numpy vector of eigenvalues
# sorted_eigvec [DxD] numpy array of eigenvectors

indices = np.argsort(eigval)
indices = indices[::-1]
eigvec = eigvec[:, indices]
eigval = eigval[indices]

sorted_eigval = eigval
sorted_eigvec = eigvec

return sorted_eigval, sorted_eigvec
```

Test your function checking the following assertion on testcase:

```
[20]: testcase = np.array([[2,0,0],[0,5,0],[0,0,3]])
    answer1 = np.array([5.,3.,2.])
    answer2 = np.array([[0.,0.,1.],[1.,0.,0.],[0.,1.,0.]]))
    x,y = compute_eigenvalue_eigenvectors(testcase)
    x,y = sort_eigenvalue_eigenvectors(x,y)
    np.testing.assert_array_almost_equal(x, answer1)
    np.testing.assert_array_almost_equal(y, answer2)
```

1.2.6 PCA Algorithm

Implement a function with the following signature to compute PCA as explained in *Marsland* using the functions implemented above.

```
[21]: def pca(A,m):
          # INPUT:
          # A
                 [NxM] numpy data matrix (N samples, M features)
                 integer number denoting the number of learned features (m <= M)
          # m
          # OUTPUT:
          # pca_eigvec
                          [Mxm] numpy matrix containing the eigenvectors (M_
       \rightarrow dimensions, m eigenvectors)
          # P
                           [Nxm] numpy PCA data matrix (N samples, m features)
          A_centered = center_data(A)
          C = compute_covariance_matrix(A_centered)
          eigval,eigvec = compute_eigenvalue_eigenvectors(C)
          sorted_eigval, sorted_eigvec = sort_eigenvalue_eigenvectors(eigval,eigvec)
          if m > 0:
              sorted_eigvec = sorted_eigvec[:,:m]
```

```
pca_eigvec = sorted_eigvec

P = np.dot(np.transpose(sorted_eigvec), np.transpose(A))
return pca_eigvec, P.T
```

Test your function checking the following assertion on testcase:

1.3 Understanding: how does PCA work?

We now use the PCA algorithm you implemented on a toy data set in order to understand its inner workings.

1.3.1 Loading the data

The module synthetic data provides a small synthetic dataset of dimension [100x2] (100 samples, 2 features).

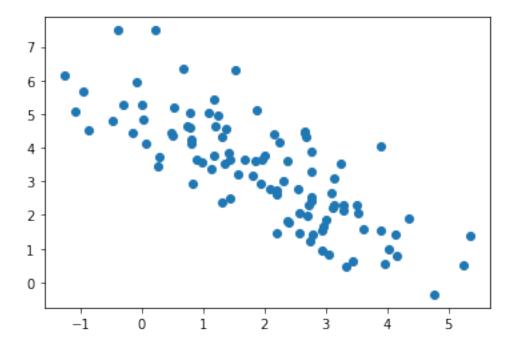
```
[23]: X = syntheticdata.get_synthetic_data1()
```

1.3.2 Visualizing the data

Visualize the synthetic data using the function scatter() from the matplotlib library.

```
[24]: plt.scatter(X[:,0],X[:,1])
```

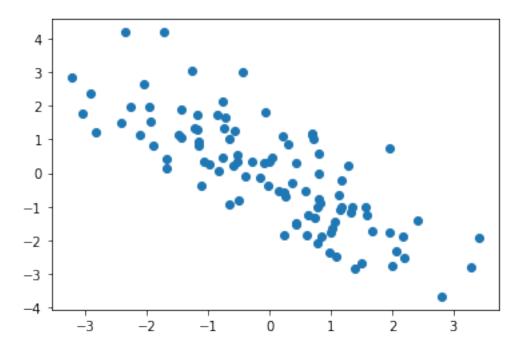
[24]: <matplotlib.collections.PathCollection at 0x7fbaeda77700>



1.3.3 Visualize the centered data

Notice that the data visualized above is not centered on the origin (0,0). Use the function defined above to center the data, and the replot it.

[25]: <matplotlib.collections.PathCollection at 0x7fbaed97edf0>



1.3.4 Visualize the first eigenvector

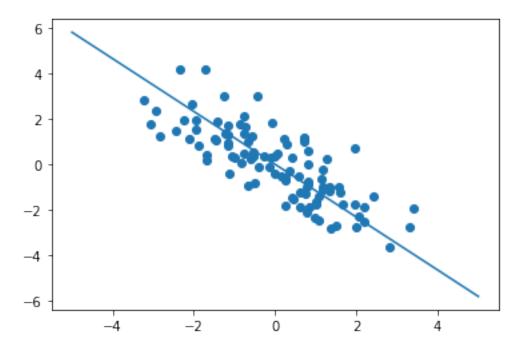
Visualize the vector defined by the first eigenvector. To do this you need: - Use the PCA() function to recover the eigenvectors - Plot the centered data as done above - The first eigenvector is a 2D vector (x0,y0). This defines a vector with origin in (0,0) and head in (x0,y0). Use the function plot() from matplotlib to plot a line over the first eigenvector.

```
[26]: pca_eigvec, _ = pca(X, m=0)
first_eigvec = pca_eigvec[0]

plt.scatter(_X[:,0],_X[:,1])

x = np.linspace(-5, 5, 1000)
y = first_eigvec[1]/first_eigvec[0] * x
plt.plot(x,y)
```

[26]: [<matplotlib.lines.Line2D at 0x7fbaed8fdbb0>]

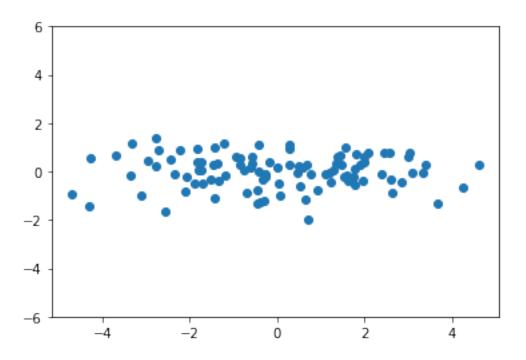


1.3.5 Visualize the PCA projection

Finally, use the PCA() algorithm to project on a single dimension and visualize the result using again the scatter() function.

```
[27]:    _,P = pca(X, m=0)
    plt.scatter(P[:,0],P[:,1])
    plt.ylim(-6,6)
```

[27]: (-6.0, 6.0)



1.4 Evaluation: when are the results of PCA sensible?

So far we have used PCA on synthetic data. Let us now imagine we are using PCA as a preprocessing step before a classification task. This is a common setup with high-dimensional data. We explore when the use of PCA is sensible.

1.4.1 Loading the first set of labels

The function get_synthetic_data_with_labels1() from the module syntethicdata provides a first labeled dataset.

```
[28]: X,y = syntheticdata.get_synthetic_data_with_labels1()
```

1.4.2 Running PCA

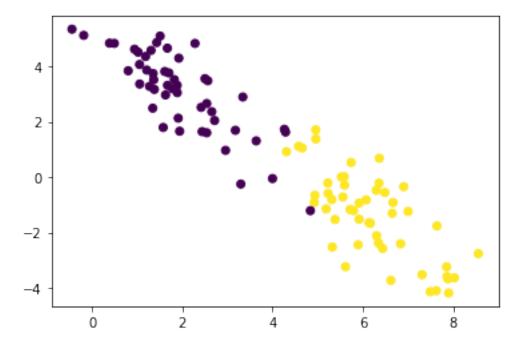
Process the data using the PCA algorithm and project it in one dimension. Plot the labeled data using *scatter()* before and after running PCA. Comment on the results.

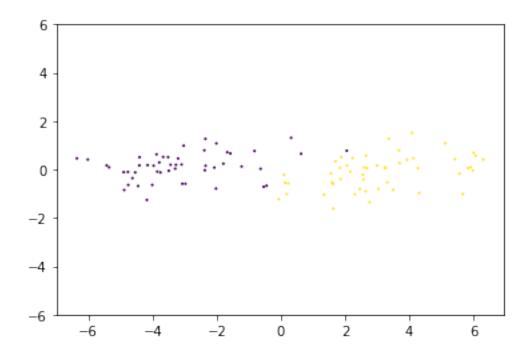
```
[29]: plt.scatter(X[:,0],X[:,1],c=y[:,0])

plt.figure()
   _,P = pca(X, m=0)
   plt.scatter(P[:,0],P[:,1],np.ones(P.shape[0]),c=y[:,0])
```

plt.ylim(-6,6)

[29]: (-6.0, 6.0)





Comment: The covariance of this plot is on the negative values.

1.4.3 Loading the second set of labels

The function $get_synthetic_data_with_labels2()$ from the module syntethicdata provides a second labeled dataset.

```
[30]: X,y = syntheticdata.get_synthetic_data_with_labels2()
```

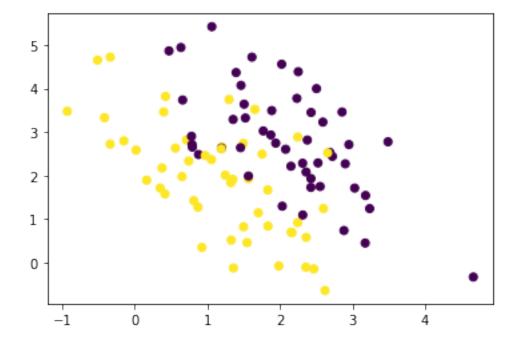
1.4.4 Running PCA

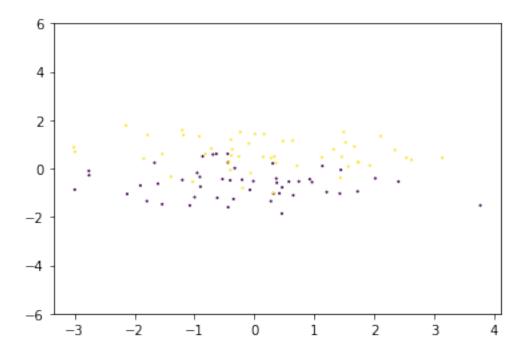
As before, process the data using the PCA algorithm and project it in one dimension. Plot the labeled data using *scatter()* before and after running PCA. Comment on the results.

```
[31]: plt.scatter(X[:,0],X[:,1],c=y[:,0])

plt.figure()
   _,P = pca(X, m=0)
plt.scatter(P[:,0],P[:,1],np.ones(P.shape[0]),c=y[:,0])
plt.ylim(-6,6)
```

[31]: (-6.0, 6.0)





Comment: Whilst here we have a covariance that closes in on zero.

How would the result change if you were to consider the second eigenvector? Or if you were to consider both eigenvectors?

Yes the eigenvector should help a fair bit in cetralizing the data and if we were to place both it should help even more.

1.5 Case study 1: PCA for visualization

We now consider the *iris* dataset, a simple collection of data (N=150) describing iris flowers with four (M=4) features. The features are: Sepal Length, Sepal Width, Petal Length and Petal Width. Each sample has a label, identifying each flower as one of 3 possible types of iris: Setosa, Versicolour, and Virginica.

Visualizing a 4-dimensional dataset is impossible; therefore we will use PCA to project our data in 2 dimensions and visualize it.

1.5.1 Loading the data

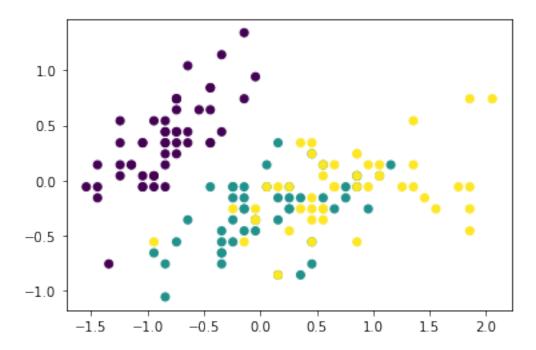
The function $get_iris_data()$ from the module syntethicdata returns the iris dataset. It returns a data matrix of dimension [150x4] and a label vector of dimension [150].

1.5.2 Visualizing the data by selecting features

Try to visualize the data (using label information) by randomly selecting two out of the four features of the data. You may try different pairs of features.

```
[33]: rng = np.random.randint(4)
rng1 = np.random.randint(4)
    _X = center_data(X)
plt.scatter(_X[:,rng],_X[:,rng1], c=y)
```

[33]: <matplotlib.collections.PathCollection at 0x7fbaed7a07f0>



1.5.3 Visualizing the data by PCA

Process the data using PCA and visualize it (using label information). Compare with the previous visualization and comment on the results.

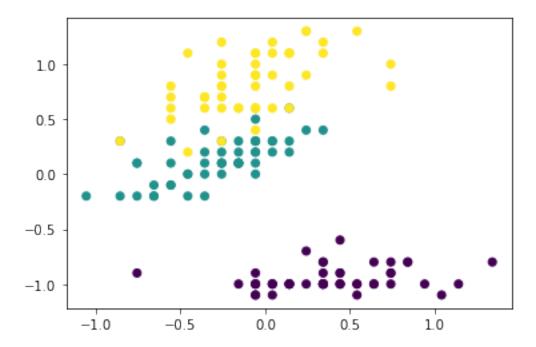
```
[74]: rng = np.random.randint(4)
rng1 = np.random.randint(4)

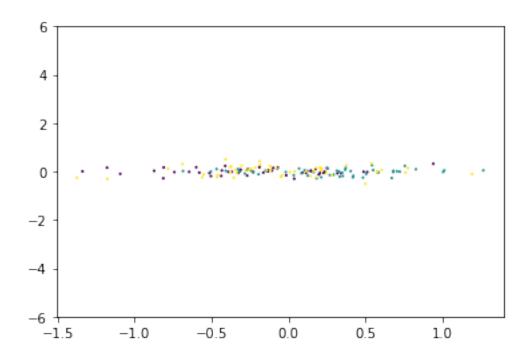
plt.scatter(X[:,rng],X[:,rng1],c=y)

plt.figure()
   _,P = pca(X, m=0)
```

```
plt.scatter(P[:,rng],P[:,rng1],np.ones(P.shape[0]),c=y)
plt.ylim(-6,6)
```

[74]: (-6.0, 6.0)





After some runs of the program it seems that the PCA version alligns quite a bit with the plot above it

1.6 Case study 2: PCA for compression

We now consider the faces in the wild (lfw) dataset, a collection of pictures (N=1280) of people. Each pixel in the image is a feature (M=2914).

1.6.1 Loading the data

The function $get_lfw_data()$ from the module syntethicdata returns the lfw dataset. It returns a data matrix of dimension [1280x2914] and a label vector of dimension [1280]. It also returns two parameters, h and w, reporting the height and the width of the images (these parameters are necessary to plot the data samples as images). Beware, it might take some time to download the data. Be patient:)

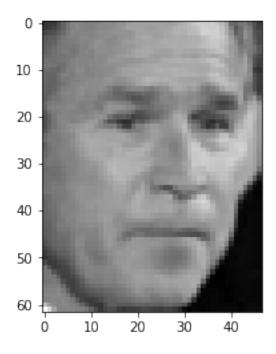
1.6.2 Inspecting the data

Choose one datapoint to visualize (first coordinate of the matrix X) and use the function imshow() to plot and inspect some of the pictures.

Notice that imshow receives as a first argument an image to be plot; the image must be provided as a rectangular matrix, therefore we reshape a sample from the matrix X to have height h and width w. The parameter cmap specifies the color coding; in our case we will visualize the image in black-and-white with different gradations of grey.

```
[36]: plt.imshow(X[0,:].reshape((h, w)), cmap=plt.cm.gray)
```

[36]: <matplotlib.image.AxesImage at 0x7fbaed6102b0>



1.6.3 Implementing a compression-decompression function

Implement a function that first uses PCA to project samples in low-dimensions, and the reconstruct the original image.

Hint: Most of the code is the same as the previous PCA() function you implemented. You may want to refer to *Marsland* to check out how reconstruction is performed.

```
#Computing the indices
indices = np.argsort(eigval)
indices = indices[::-1][:m]
eigvec = eigvec[:,indices]
eigval = eigval[indices]
for i in range(np.shape(eigvec)[1]):
    eigvec[:,i] / np.linalg.norm(eigvec[:,i])*np.sqrt(eigval[i])

x = np.dot(np.transpose(eigvec), np.transpose(A))

y = np.transpose(np.dot(eigvec, x)) + norm #tips Marshland page 137

Ahat = y
pca_eigvec = eigvec
return Ahat
```

1.6.4 Compressing and decompressing the data

Use the implemented function to encode and decode the data by projecting on a lower dimensional space of dimension 200 (m=200).

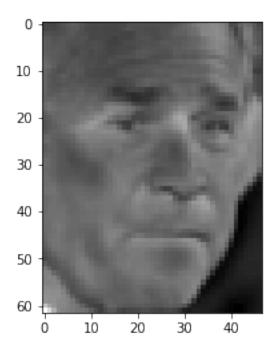
```
[38]: Xhat = encode_decode_pca(X,200)
```

1.6.5 Inspecting the reconstructed data

Use the function imshow to plot and compare original and reconstructed pictures. Comment on the results.

```
[39]: plt.imshow(X[0,:].reshape((h, w)), cmap=plt.cm.gray)
```

[39]: <matplotlib.image.AxesImage at 0x7fbaec85f760>

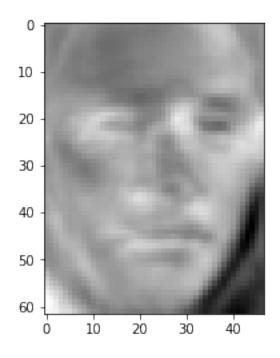


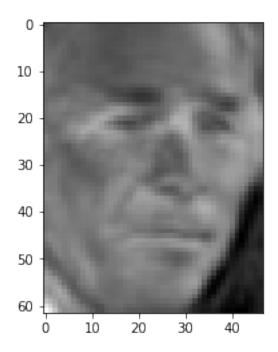
Comment: Enter your comment here.

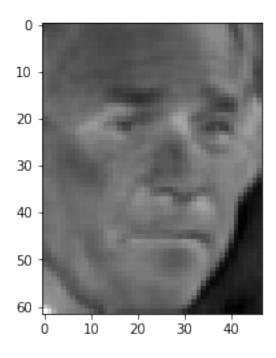
1.6.6 Evaluating different compressions

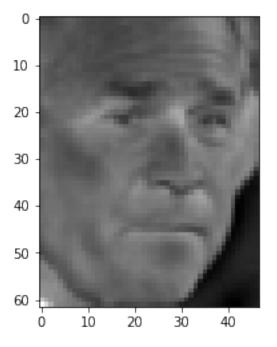
Use the previous setup to generate compressed images using different values of low dimensions in the PCA algorithm (e.g.: 100, 200, 500, 1000). Plot and comment on the results.

Here is the plots of the different values









As we increase the pixels used during the runs we get a more defined and better sharpness on our fellows face, overall this is quite neat as i can imagine this can be fairly usefull in visalizations of far away stars or molecules considering how bad the quality of those imagings can be.

1.7 Master Students: PCA Tuning

If we use PCA for compression or decompression, it may be not trivial to decide how many dimensions to keep. In this section we review a principled way to decide how many dimensions to keep.

The number of dimensions to keep is the only *hyper-parameter* of PCA. A method designed to decide how many dimensions/eigenvectors is the *proportion of variance*:

$$POV = \frac{\sum_{i=1}^{m} \lambda_i}{\sum_{j=1}^{M} \lambda_j},$$

where λ are eigenvalues, M is the dimensionality of the original data, and m is the chosen lower dimensionality.

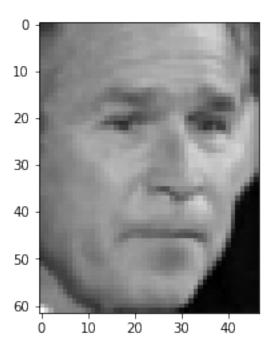
Using the POV formula we may select a number M of dimensions/eigenvalues so that the proportion of variance is, for instance, equal to 95%.

Implement a new PCA for encoding and decoding that receives in input not the number of dimensions for projection, but the amount of proportion of variance to be preserved.

```
[46]: def encode_decode_pca_with_pov(A,p):
    # INPUT:
    # A     [NxM] numpy data matrix (N samples, M features)
    # p     float number between 0 and 1 denoting the POV to be preserved
#
# OUTPUT:
# Ahat [NxM] numpy PCA reconstructed data matrix (N samples, M features)
# m     integer reporting the number of dimensions selected

m = None
Ahat = None
return Ahat,m
```

Import the *lfw* dataset using the *get_lfw_data()* in *syntheticdata*. Use the implemented function to encode and decode the data by projecting on a lower dimensional space such that POV=0.9. Use the function *imshow* to plot and compare original and reconstructed pictures. Comment on the results.



<Figure size 432x288 with 0 Axes>

Comment: Enter your comment here.

2 K-Means Clustering (Bachelor and master students)

In this section you will use the k-means clustering algorithm to perform unsupervised clustering. Then you will perform a qualitative assessment of the results.

2.0.1 Importing scikit-learn library

We start importing the module cluster.KMeans from the standard machine learning library scikit-learn.

```
[]: from sklearn.cluster import KMeans
```

2.0.2 Loading the data

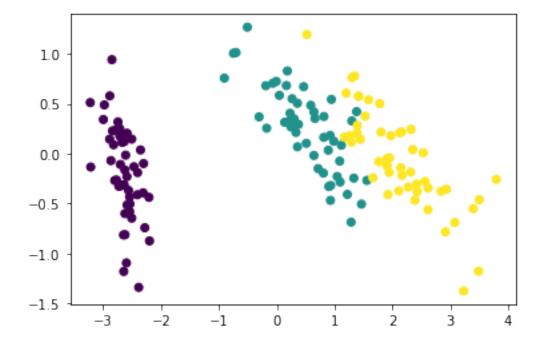
We will use once again the *iris* data set. The function $get_iris_data()$ from the module syntethic data returns the *iris* dataset. It returns a data matrix of dimension [150x4] and a label vector of dimension [150].

2.0.3 Projecting the data using PCA

To allow for visualization, we project our data in two dimensions as we did previously. This step is not necessary, and we may want to try to use k-means later without the PCA pre-processing. However, we use PCA, as this will allow for an easy visualization.

```
[51]: _,P = pca(X,2)
plt.scatter(P[:,0],P[:,1], c=y)
```

[51]: <matplotlib.collections.PathCollection at 0x7fbaed6c4970>



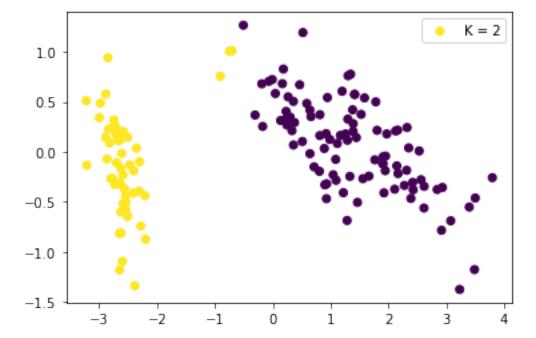
2.0.4 Running k-means

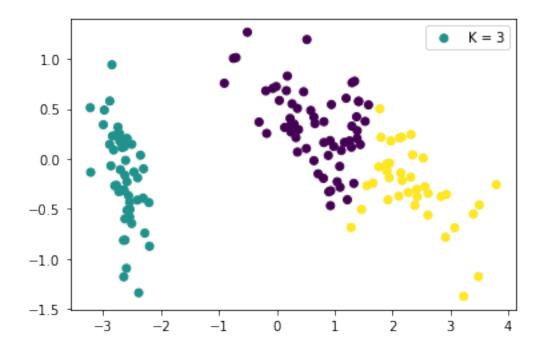
We will now consider the *iris* data set as an unlabeled set, and perform clustering to this unlabeled set. We can compare the results of the clustering to the lableled calsses.

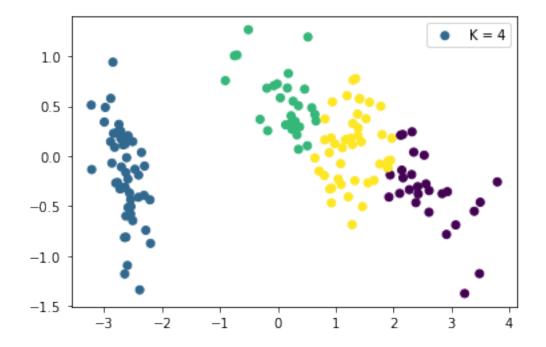
Use the class KMeans to fit and predict the output of the k-means algorithm on the projected data. Run the algorithm using the following values of $k = \{2, 3, 4, 5\}$.

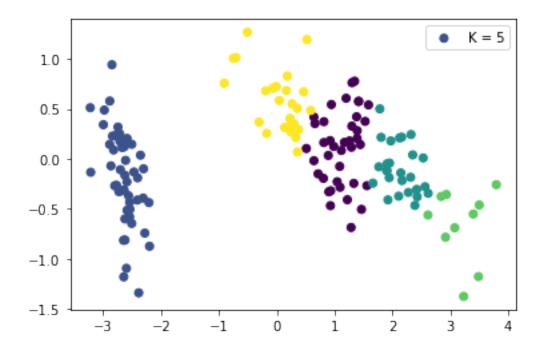
```
[52]: data = []
    yhat2 = []

for i in [2,3,4,5]:
        KM = KMeans(n_clusters = i)
        title = "K = " + str(i)
        yhat2 = KM.fit_predict(P)
        plt.scatter(P[:,0], P[:,1], c = yhat2, label = title)
        plt.legend()
        plt.show()
        data.append(yhat2)
        data = np.asarray(data)
```









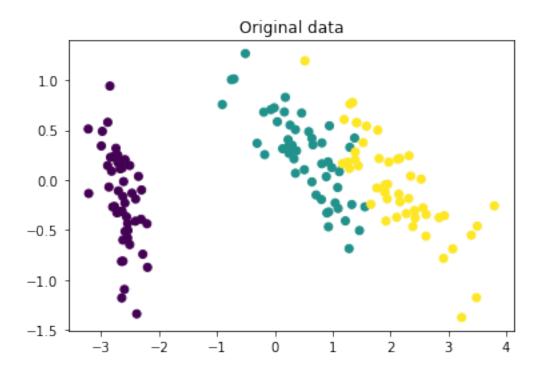
2.0.5 Qualitative assessment

Plot the results of running the k-means algorithm, compare with the true labels, and comment.

```
[53]: #plt.scatter(P[:,0],P[:,1],c=None)
#plt.title('k=2')
"""Answer is above"""

plt.figure()
plt.scatter(P[:,0],P[:,1],c=y)
plt.title('Original data')
```

[53]: Text(0.5, 1.0, 'Original data')



During the run of the clusters it seems as expected that the final two clusters do the best job in splitting up the major cluster on the right giving us the quess that as expected it should have the highest accuracies out of the bunch

3 Quantitative Assessment of K-Means (Bachelor and master students)

We used k-means for clustering and we assessed the results qualitatively by visualizing them. However, we often want to be able to measure in a quantitative way how good the clustering was. To do this, we will use a classification task to evaluate numerically the goodness of the representation learned via k-means.

Reload the *iris* dataset. Import a standard LogisticRegression classifier from the module sklearn.linear_model. Use the k-means representations learned previously (yhat2,...,yhat5) and the true label to train the classifier. Evaluate your model on the training data (we do not have a test set, so this procedure will assess the model fit instead of generalization) using the accuracy_score() function from the *sklearn.metrics* module. Plot a graph showing how the accuracy score varies when changing the value of k. Comment on the results.

- Train a Logistic regression model using the first two dimensions of the PCA of the iris data set as input, and the true classes as targets.
- Report the model fit/accuracy on the training set.
- For each value of K:
 - One-Hot-Encode the classes output by the K-means algorithm.

- Train a Logistic regression model on the K-means classes as input vs the real classes as targets.
- Calculate model fit/accuracy vs. value of K.
- Plot your results in a graph and comment on the K-means fit.

```
[75]: X,y = syntheticdata.get_iris_data()
      def k_dimension(A, k):
          k vals = []
          for i in range(A.shape[0]):
              k_d = np.zeros((i+2, A[1].shape[0]))
              for j in range(k[i]):
                  k_d[j] = (A[i] == j)
              k_vals.append(k_d)
          return np.asarray(k_vals)
      k_dim = np.zeros((4,150))
      k_{vals} = [2,3,4,5]
      for i in range(4):
          eig, data = pca(X,2)
          KM = KMeans(n_clusters=k_vals[i])
          yhat2 = KM.fit_predict(data)
          k_dim[i,:] = yhat2
      K_trains = k_dimension(k_fits,k_vals)
```

/tmp/ipykernel_547/3208965975.py:11: VisibleDeprecationWarning: Creating an ndarray from ragged nested sequences (which is a list-or-tuple of lists-or-tuples-or ndarrays with different lengths or shapes) is deprecated. If you meant to do this, you must specify 'dtype=object' when creating the ndarray. return np.asarray(k_vals)

```
[78]: from sklearn.linear_model import LogisticRegression
    from sklearn import metrics

k_vals = [2,3,4,5]
N = 100
    accuracy = np.zeros((4,N))
    accuracy_list = np.zeros(4)
    x = np.arange(4)
    for j in range(N):
        for i in range(4):
            K_out = K_trains[i].T
            cl = LogisticRegression(solver="lbfgs", multi_class="auto")
            cl.fit(K_out, y)
            accuracy[i,j] = cl.score(K_out, y)*100
```

```
for i in range(4):
    accuracy_list[i] = np.sum(accuracy[i,:])/N
    print(f"The accuracy at K-cluster {str(i+2)} is: {accuracy_list[i]:.2f}%")

The accuracy at K-cluster 2 is: 66.67%
    The accuracy at K-cluster 3 is: 88.67%
    The accuracy at K-cluster 4 is: 84.67%
    The accuracy at K-cluster 5 is: 89.33%

[77]: x = np.arange(10)
    for i in range(4):
        title = "K-" + str(i+2)
        plt.plot(x, accuracy[i,:10], label=title)

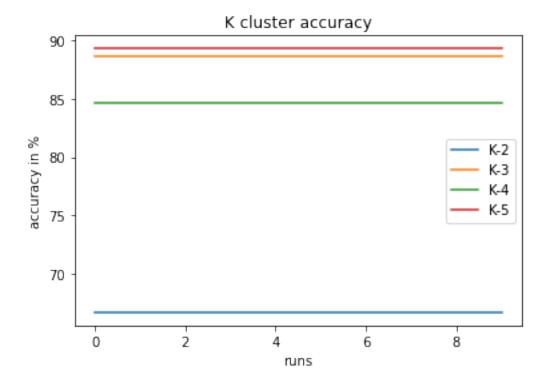
plt.xlabel("runs")

plt.ylabel("accuracy in %")

plt.title("K cluster accuracy")

plt.legend()
```

[77]: <matplotlib.legend.Legend at 0x7fbaed5a6070>



Interestingly for some reason k_3 has an quite the high accuracy, though based on talking with others who have done this assignment this fenomenon is shared with everyone i have spoke to. Asides from that it runs fine

4 Conclusions

In this notebook we studied **unsupervised learning** considering two important and representative algorithms: **PCA** and **k-means**.

First, we implemented the PCA algorithm step by step; we then run the algorithm on synthetic data in order to see its working and evaluate when it may make sense to use it and when not. We then considered two typical uses of PCA: for **visualization** on the *iris* dataset, and for **compression-decompression** on the *lfw* dateset.

We then moved to consider the k-means algorithm. In this case we used the implementation provided by *scikit-learn* and we applied it to another prototypical unsupervised learning problem: **clustering**; we used *k-means* to process the *iris* dataset and we evaluated the results visually.

In the final part, we considered two additional questions that may arise when using the above algorithms. For PCA, we considered the problem of **selection of hyper-parameters**, that is, how we can select the hyper-parameter of ou algorithm in a reasonable fashion. For k-means, we considered the problem of the **quantitative evaluation** of our results, that is, how can we measure the performance or usefulness of our algorithms.