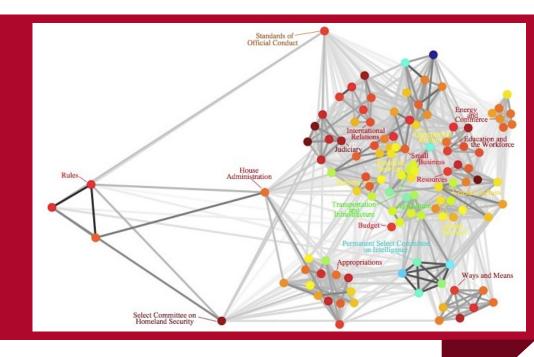
# **Automatic Control Theory**

Chapter 2



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# A CH2: Mathematical Models of Systems

#### **Review**

- Transfer function
- Laplace Transform
- Block Diagram reduction

#### what is next

- > Unit impulse response function
- > Different types of Transfer function

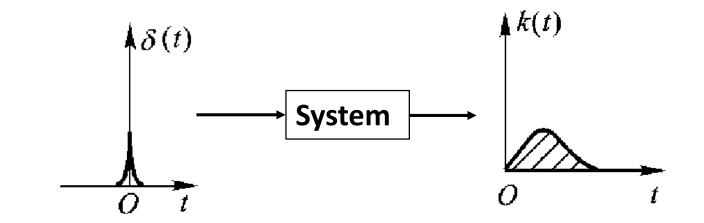


## Unit impulse response function

unit impulse function

$$\delta(t)$$

unit impulse response



$$L[\delta(t)] = 1, L[k(t)] = K(s)$$

$$\Phi(s) = \frac{K(s)}{1} = K(s)$$



# Unit impulse response function

Arbitrary function input r(t) —— System —— ouput c(t)

$$C(s) = \Phi(s) \cdot R(s) = K(s) \cdot R(s)$$

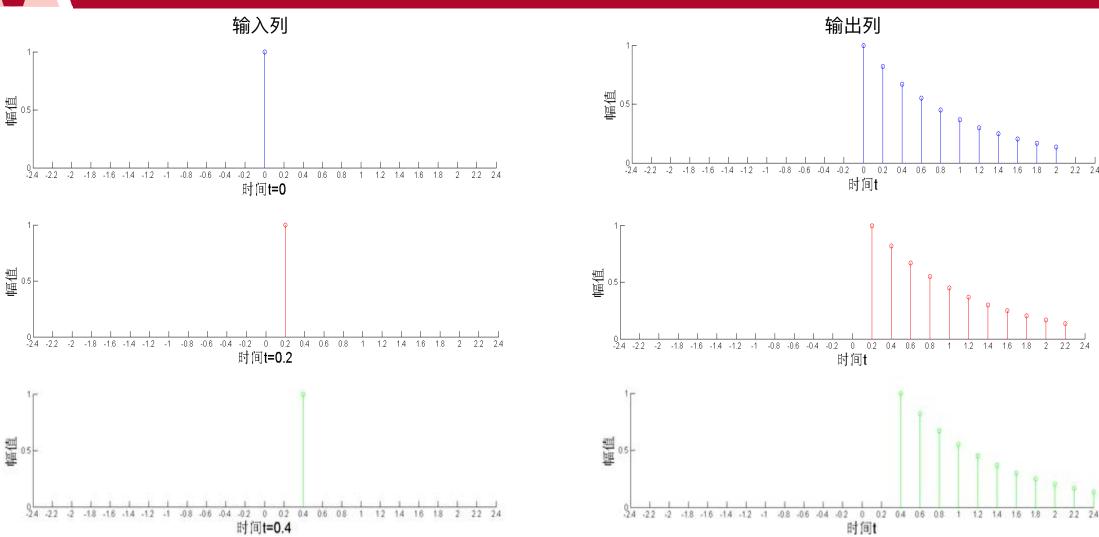
$$c(t) = L^{-1}[K(s) \cdot R(s)]$$
$$= \int_0^t r(\tau)k(t-\tau)d\tau$$

卷积! 时域上的卷积等效复域的点积

**Convolution function** 



#### Convolution function





### **Convolution function**

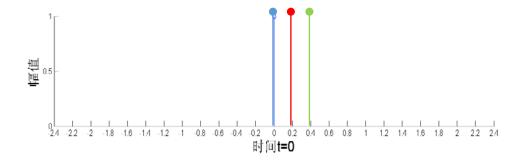
$$\int_{0}^{t} r(\tau)k(t-\tau)\mathrm{d}\tau$$

时间的反转 越先进去作用靠前 距离t反应最微弱

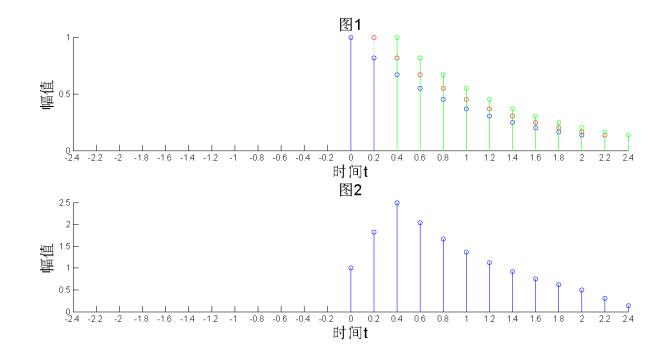
越晚出去距离t越及时

r(t)像权重

卷积:将输出分段后多个输入叠加



如果我想要很多未知输入得到很多未知输出 我只需要得到一次脉冲函数和脉冲响应函数 用该脉冲函数构成我想要的输入,卷积就可以得到输出 非常牛!



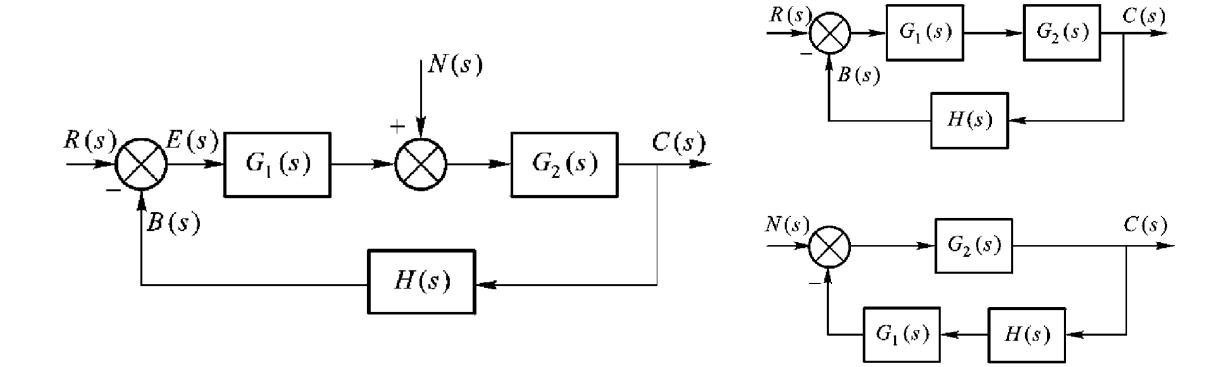


#### **Transfer function:**

The ratio of the Laplace transform of the output variable to the Laplace transform of the input variable, with all initial conditions assumed to be zero.

Different definitions: input variable output variable



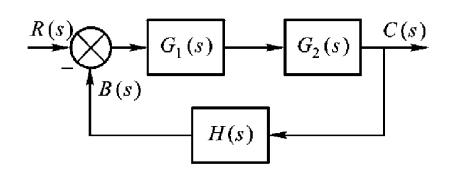


Different definitions: input variable output variable



(1) input variable: R(s)

n(t) = 0!



$$\Phi(s) = \frac{C(s)}{R(s)} = \frac{G_1(s)G_2(s)}{1 + G_1(s)G_2(s)H(s)}$$

$$C(s) = \Phi(s)R(s) = \frac{G_1(s)G_2(s)}{1 + G_1(s)G_2(s)H(s)}R(s)$$

(2) output variable: N(s)

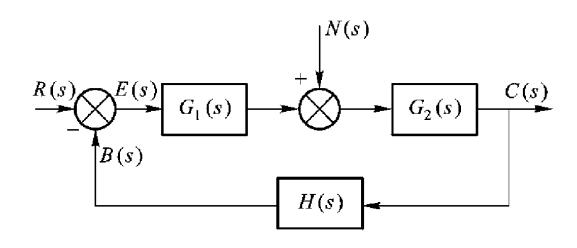
r(t) = 0!

$$M(s)$$
 $G_2(s)$ 
 $G_1(s)$ 
 $H(s)$ 

$$\Phi_{\rm n}(s) = \frac{C(s)}{N(s)} = \frac{G_2(s)}{1 + G_1(s)G_2(s)H(s)}$$

$$C(s) = \Phi_{n}(s)N(s) = \frac{G_{2}(s)}{1 + G_{1}(s)G_{2}(s)H(s)}N(s)$$





$$C_{\Sigma}(s) = \frac{G_{1}(s)G_{2}(s)}{1 + G_{1}(s)G_{2}(s)H(s)}R(s) + \frac{G_{2}(s)}{1 + G_{1}(s)G_{2}(s)H(s)}N(s)$$

More details in Chapter 3 The performance of feedback control systems



#### 核心

- Unit impulse response function
- Convolution function

续

• Chapter 3 The performance of feedback control systems