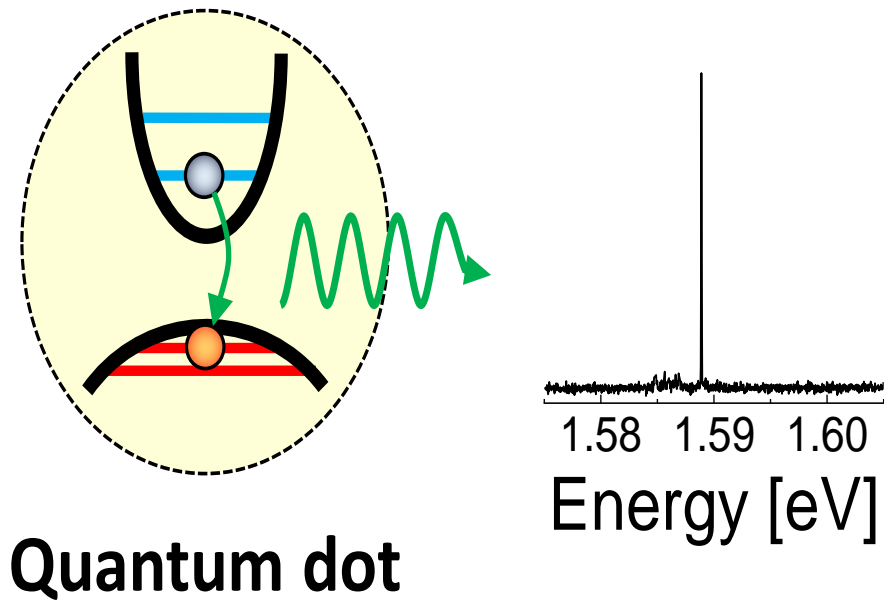
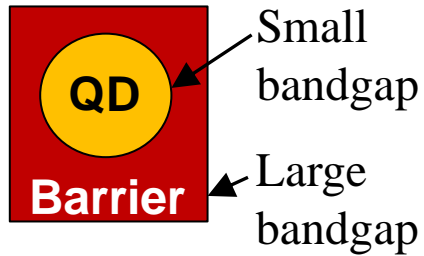


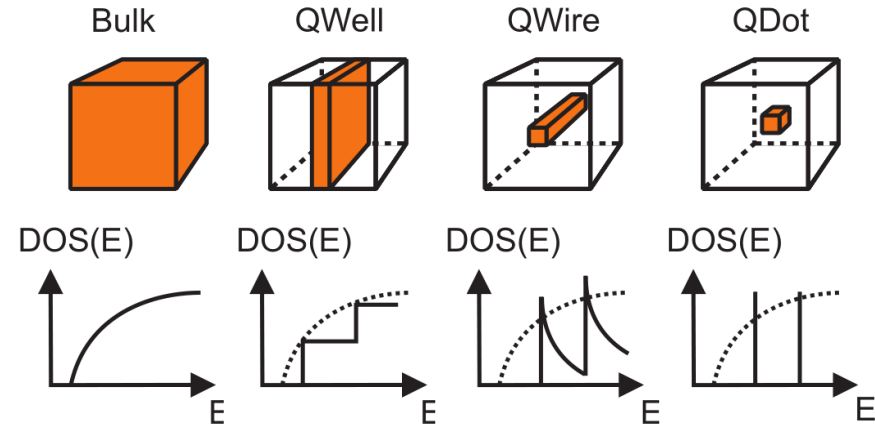
# Praktikumsversuch: Photolumineszenz von Halbleiter-Quantenpunkten



# Semiconductor Quantum Dots (QD)



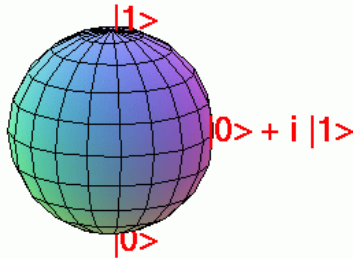
**Artificial atoms**  
(size  $\lesssim 50$  nm)  
discrete density of states (DOS) with quantized energy levels



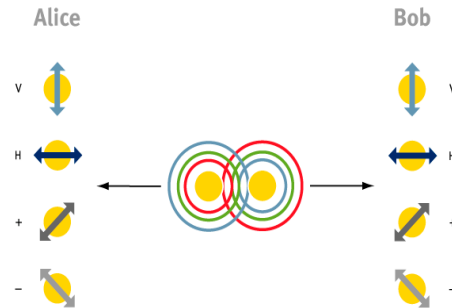
## Applications

- **Laser, Solar cells:** dense QD ensembles
- **Quantum information:** single QDs

**QuBits** for quantum computing



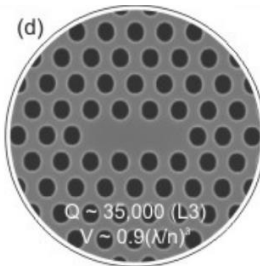
**Entangled photons** for quantum cryptography



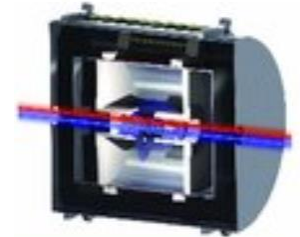
**Quantum sensors,**  
....

- **Integration:**

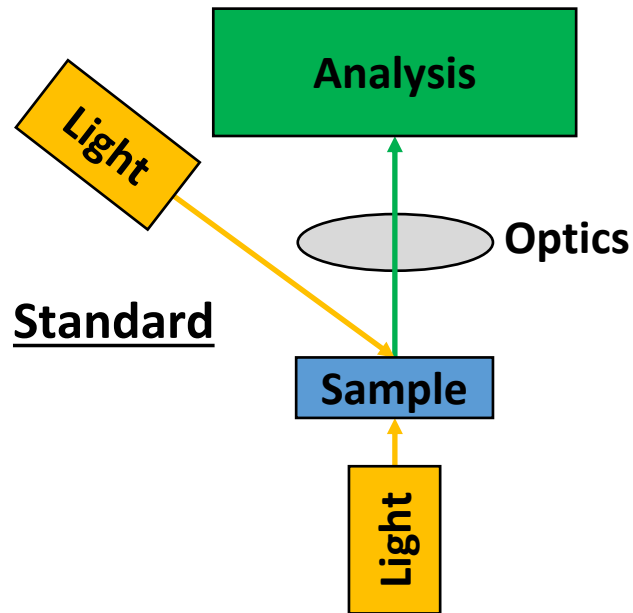
**Photonic environment**  
Quantum photonic integrated circuits,  
quantum network



Rb vapour cell as a **quantum memory**



# Optical Spectroscopy

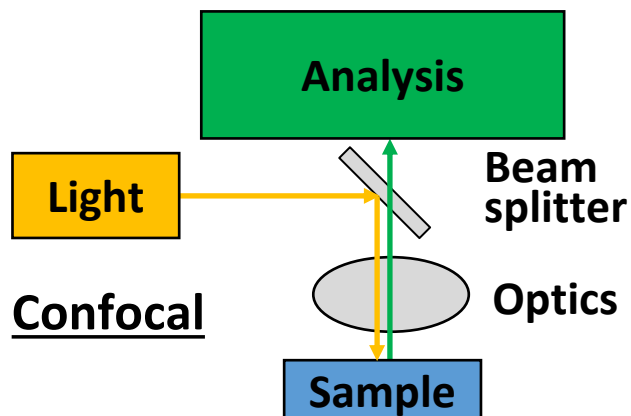


*Luminescence: „cold light“*

*Photoluminescence: inelastic light scattering*

## Photoluminescence (PL) spectroscopy:

- Excitation by laser in reflection
- Often excitation / emission through one objective
- Spectral analysis of the emission
- Information: energy of the states inside the sample (absolute energy)



## Raman spectroscopy:

- Setup like PL, in addition precise laser filter
- Information: energy loss in the sample (energy relative to the laser energy)

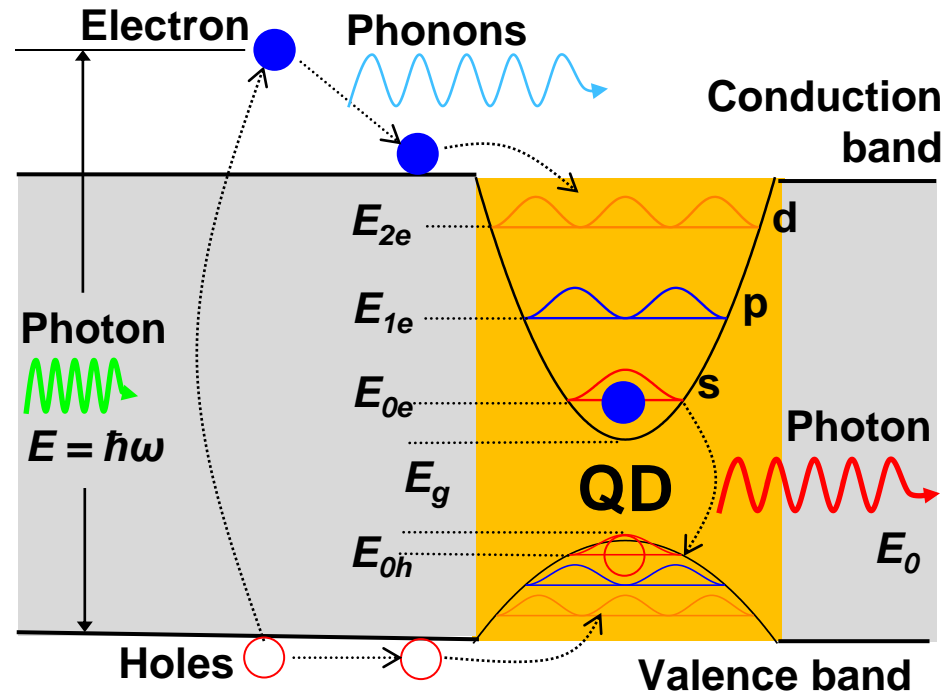
# Photoluminescence (PL) Spectroscopy on QDs

## PL spectroscopy:

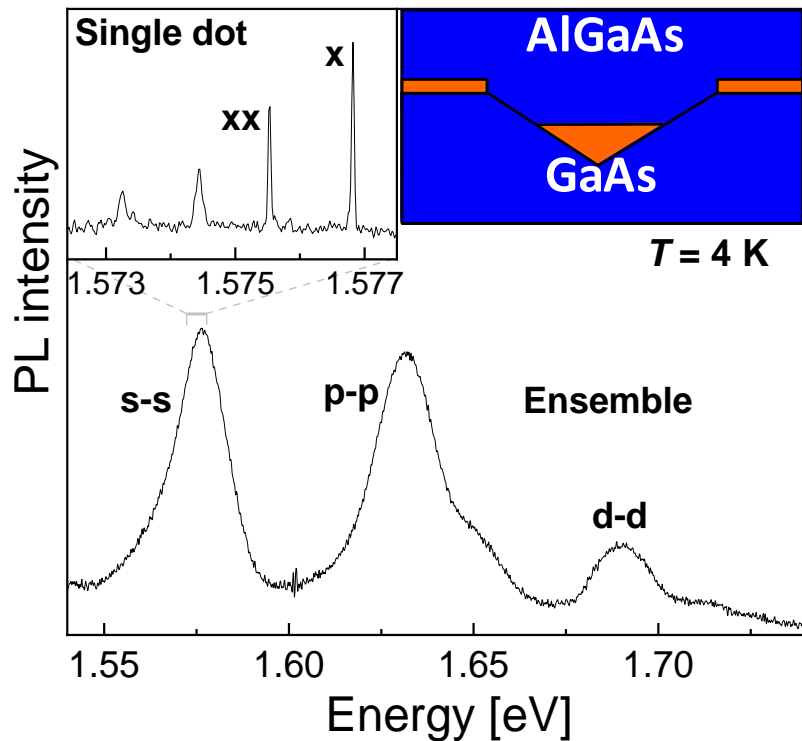
- Excitation with monochromatic light either resonantly or non-resonantly into the barrier material generates electron-hole-pairs (excitons)
- Excitons diffuse into positions with lowest energy (e.g. QD states)
- The excess energy is relaxed by phonon emission (Raman effect)
- Radiative recombination of excitons by emission of photons with energy:

$E_n = E_g + E_{ne} + E_{nh} - E_C$ , with bandgap energy  $E_g$  of the QD material, electron and hole quantization energies  $E_{ne}, E_{nh}$ , exciton binding energy  $E_C$  (Coulomb interaction)

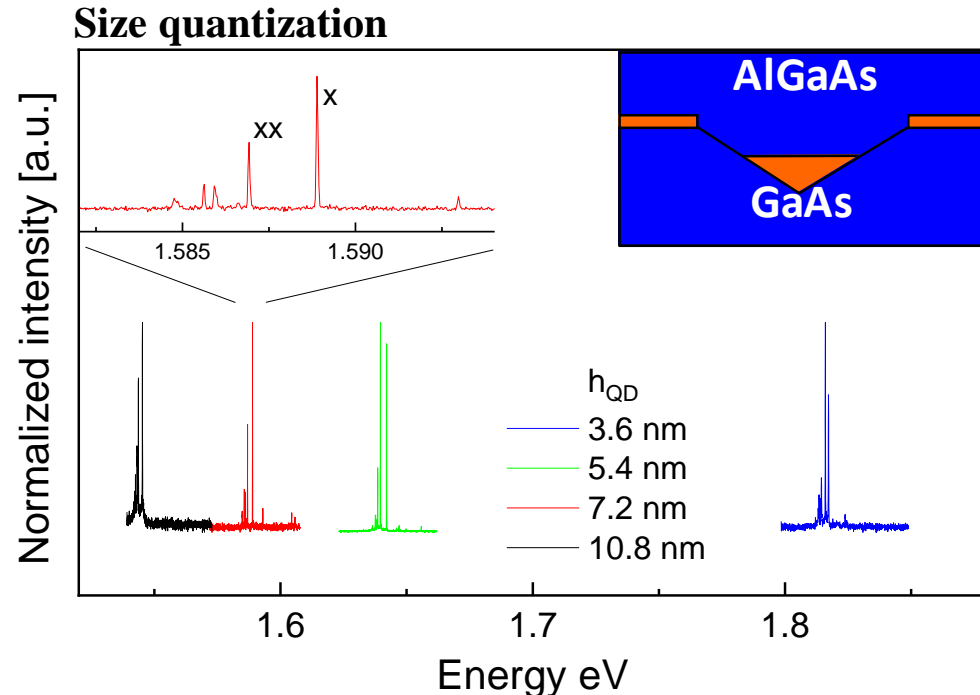
- Optical selection rules: transitions between e-h states with equal quantum numbers have the highest probability
- In GaAs, the light-hole (lh) density of states (DOS) is 6% of the total DOS (hh+lh): heavy holes (hh) dominate the PL emission



# PL Spectra: Example GaAs QDs



[*Appl. Phys. Lett.* **94**, 183113 (2009),  
*New Journal of Physics* **14** (2012)]



## Ensemble (macro-PL):

- QD shell structure: splitting by quantization energy  $\Delta E = 5\text{-}100\text{ meV}$
- Linewidth: 10-50 meV, broadened by QD size fluctuation (Gaussian distribution)

## Single-dot (mikro-PL, confocal microscope):

- Excitonic complexes, splitting by Coulomb-interaction  $\Delta E = 0.5\text{-}3\text{ meV}$
- Linewidth: natural linewidth a few  $\mu\text{eV}$  (Lorentzian distribution)  
often broadened by fluctuating charges

# Harmonic Oscillator: single-Particle frame

For a QD size < de Broglie wavelength: size quantization becomes relevant

Quantization energy in Cartesian coordinates:  $E_n = E_x + E_y + E_z$

QDs have often approximately equidistant energy levels  $\Rightarrow$  parabolic potential

1D parabolic potential:  $V = \frac{1}{2}m^*\omega_x^2x^2$ , with effective mass  $m^*$ , oscillator frequency  $\omega_x$

Eigenenergies of 1D harmonic oscillator:  $E_x = \hbar\omega_x \left(n_x + \frac{1}{2}\right)$ ,

with quantum number  $n_x = 0, 1, 2, 3, \dots$

Approximation: QD size  $\cong$  ground-state oscillator length  $L$ :

$$\text{For } x = \frac{L}{2}: V(x) = E_0 \text{ and } L^2 = \frac{4\hbar^2}{m^*\hbar\omega_x}$$

**Spherical QD shape** ( $\omega_x = \omega_y = \omega_z = \omega_0$ )

$$E_n = E_x + E_y + E_z = \hbar\omega_0 \left(n + \frac{3}{2}\right),$$

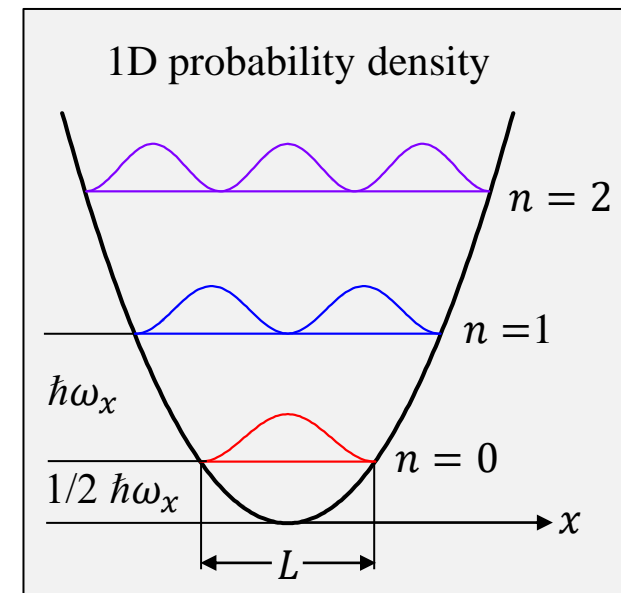
with  $n = n_{xyz} = n_x + n_y + n_z$

**Degeneracy** (without spin):

$n = 0$ : no degeneracy

$n = 1$ : deg. = 3 ( $n_{100}, n_{010}, n_{001}$ )

$n = 2$ : deg. = 6 ( $n_{110}, n_{011}, n_{101}, n_{200}, n_{020}, n_{002}$ )



# Harmonic Oscillator: Size Quantization

**Optical emission from QDs: radiative recombinations of excitons**

**QD emission energy:**  $E_n = E_g + E_{ne} + E_{nh} - E_C$ ,

with bandgap energy  $E_g$  of the QD material, electron and hole quantization energies  $E_{ne}$ ,  $E_{nh}$ , and exciton binding energy  $E_C$  (Coulomb interaction)

Approximations: 3D harmonic oscillator, spherical QD shape, no Coulomb interaction,  $n = 0$ :

$$E_{ne} = \left(n + \frac{3}{2}\right) \hbar\omega_e = \frac{3}{2} \hbar\omega_e, E_{nh} = \frac{3}{2} \hbar\omega_h$$

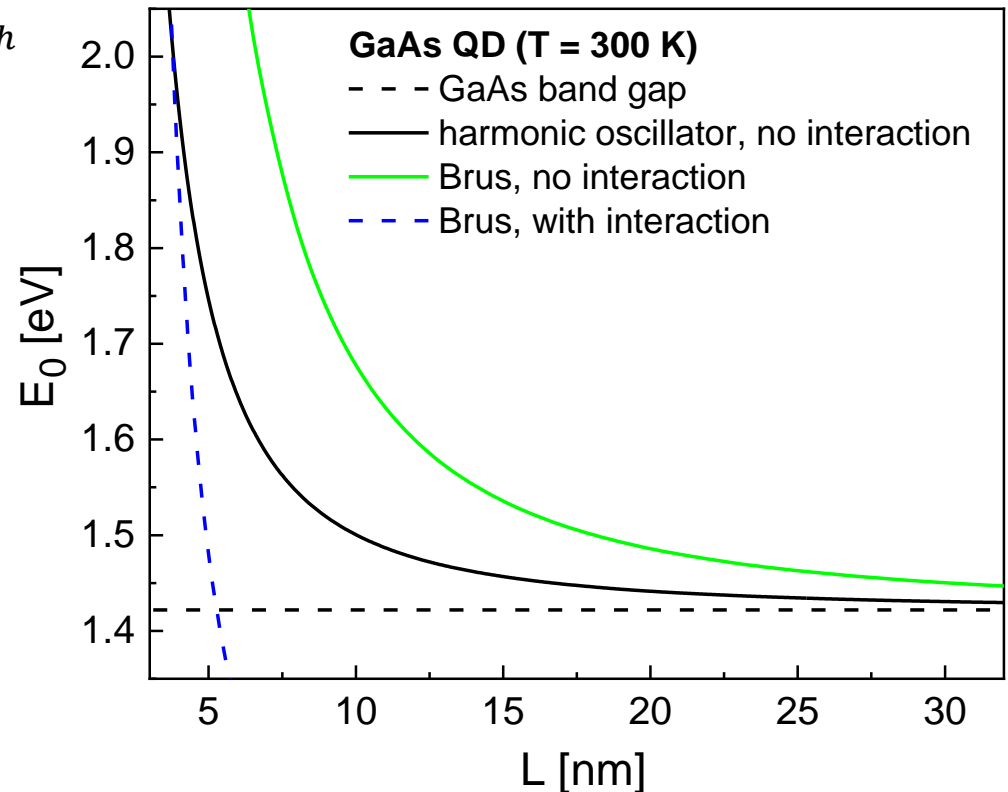
$$\text{With } \hbar\omega_e = \frac{4\hbar^2}{m_e^* L^2}, \hbar\omega_h = \frac{4\hbar^2}{m_h^* L^2} :$$

$$E_0 = E_g + \frac{6\hbar^2}{L^2} \left( \frac{1}{m_e^*} + \frac{1}{m_h^*} \right)$$

The well known Brus equation considers also an approximation for Coulomb interaction:

$$E_0 = E_g + \frac{2\pi^2 \hbar^2}{L^2} \left( \frac{1}{m_e^*} + \frac{1}{m_h^*} \right) - \frac{3.6e^2}{\epsilon_s L}$$

with the semiconductor permittivity  $\epsilon_s$   
[L. Brus, *J. Phys. Chem.* **90**, 2555 (1986)]



# Harmonic Oscillator: Example spherical GaAs QDs

## Example: PL spectrum of GaAs QDs in AlGaAs

- Bulk GaAs Peak at 1.469 eV ( $E_g$  at  $T = 192$  K)

- QDs: nearly equidistant peaks

$$E_1 - E_0 \cong E_2 - E_1, (E_n = E_g + E_{ne} + E_{nh} - E_C)$$

Harmonic oscillator approximation can be used:

$$E_{ne} = \left(n + \frac{3}{2}\right) \hbar \omega_e, E_{nh} = \left(n + \frac{3}{2}\right) \hbar \omega_h$$

- Electron, hole quantization (harmonic oscillator):

$$E_1 - E_0 = \hbar \omega_e + \hbar \omega_h = 57 \text{ meV}$$

- Oscillator length:  $L^2 = \frac{4\hbar^2}{m_e^* \hbar \omega_e} = \frac{4\hbar^2}{m_h^* \hbar \omega_h}$

$$\text{yields: } \frac{\omega_e}{\omega_h} = \frac{m_h^*}{m_e^*} \text{ and: } E_1 - E_0 = \hbar \omega_e \left(1 + \frac{m_e^*}{m_h^*}\right) \text{ or: } \hbar \omega_e = \frac{E_1 - E_0}{1 + \frac{m_e^*}{m_h^*}} \text{ and: } \hbar \omega_h = \frac{E_1 - E_0}{1 + \frac{m_h^*}{m_e^*}}$$

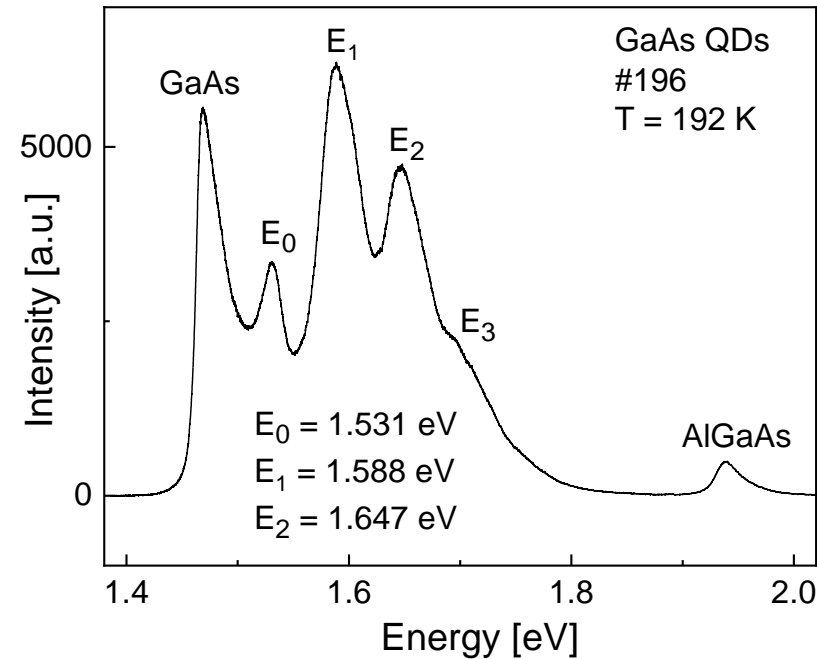
For GaAs ( $m_e^* = 0.066$ ,  $m_{hh}^* = 0.5$ ):  $\hbar \omega_e = 50.4 \text{ meV}$ ,  $\hbar \omega_h = 6.6 \text{ meV}$

Estimation of QD diameter:  $L = \left(\frac{4\hbar^2}{m_e^* \hbar \omega_e}\right)^{1/2} = 9.6 \text{ nm}$

- Coulomb interaction (approx.: spherical QD):

$$E_0 - E_g = \frac{3}{2}(\hbar \omega_e + \hbar \omega_h) - E_C \text{ and } E_1 - E_0 = \hbar \omega_e + \hbar \omega_h$$

$$\text{yields: } E_C = \frac{3}{2}(E_1 - E_0) - (E_0 - E_g) = 20.7 \text{ meV}$$

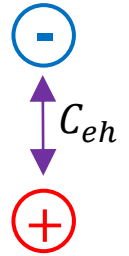




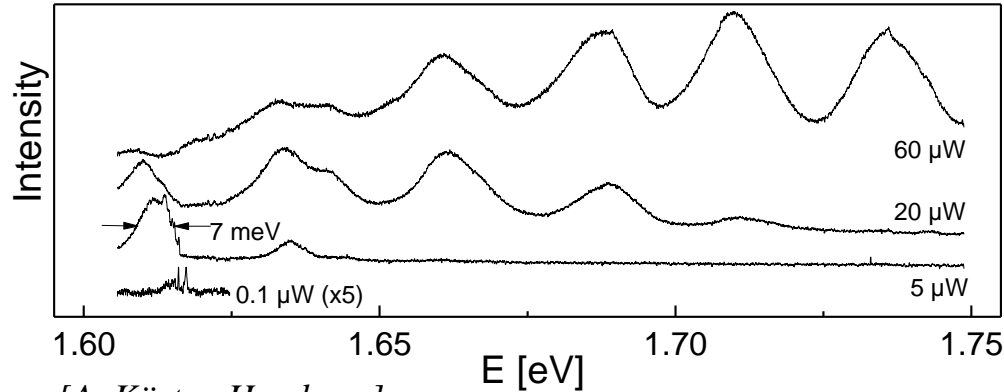
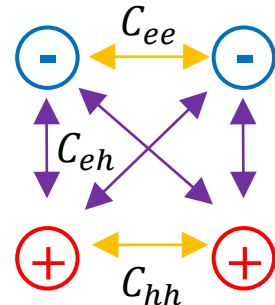
# Excitonic Complexes

Binding energy

Exciton



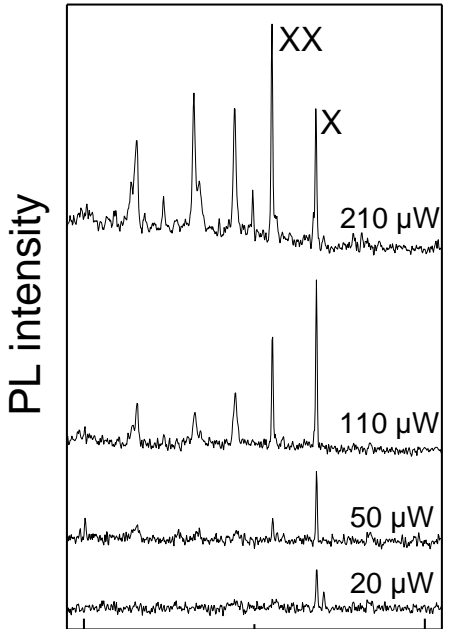
Biexciton



[A. Küster, Hamburg]

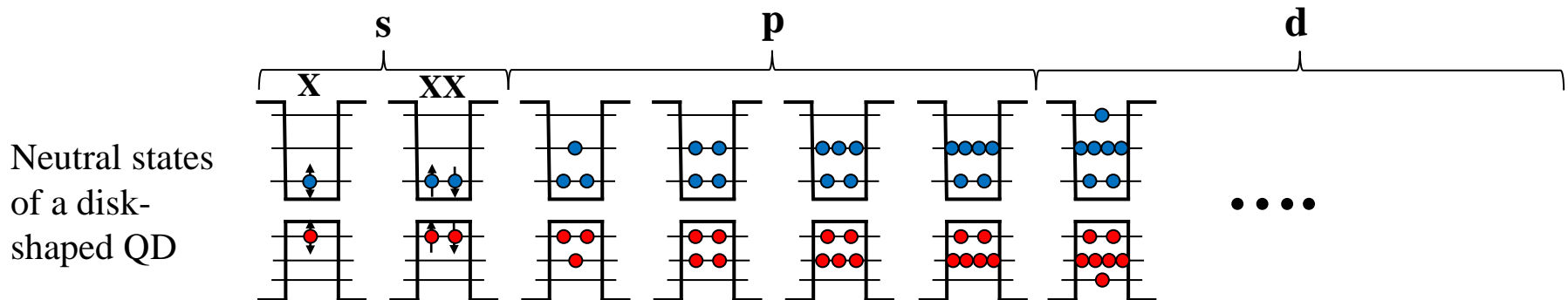
**Excitonic states:**

- s-level: up to 2 electrons and holes (spin-split): exciton X, biexciton XX
- Optical emission by radiative recombination of one exciton
- The presence of additional charge carriers shifts the emission energy due to Coulomb interactions ( $C_{eh}$ ,  $C_{ee}$ ,  $C_{hh}$ )



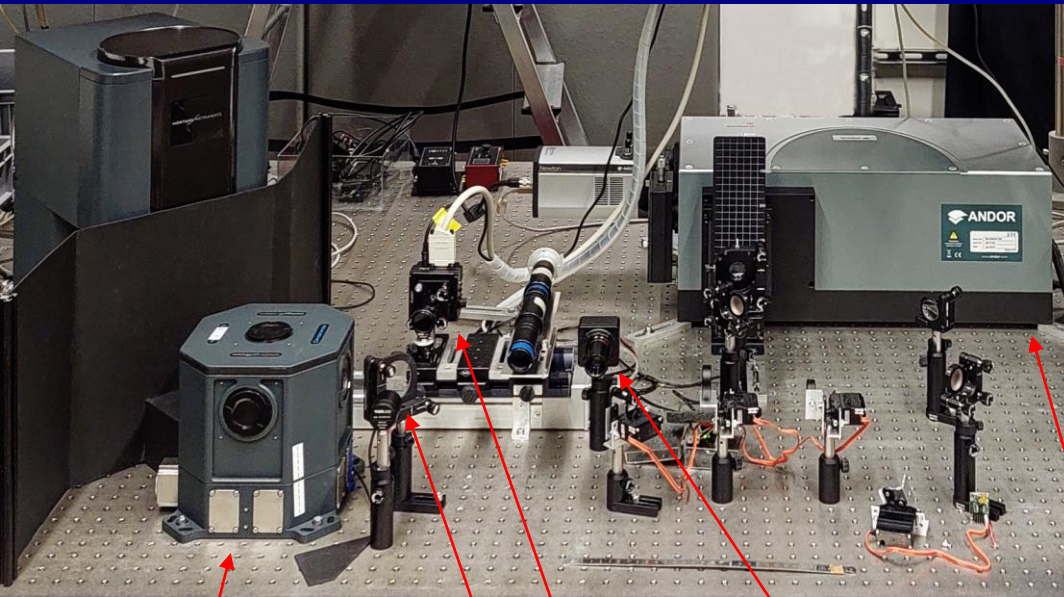
1.58 Energy [eV] 1.59

[Nanoscale Res. Lett. 5, 1633 (2010)]

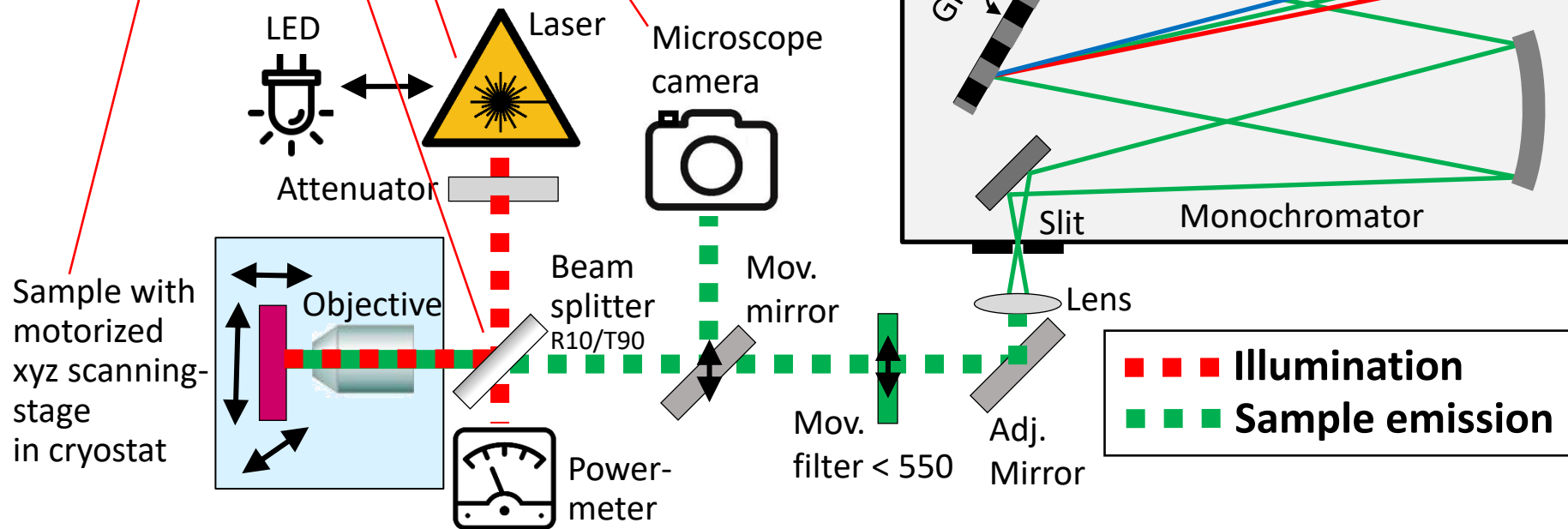


Neutral states  
of a disk-  
shaped QD

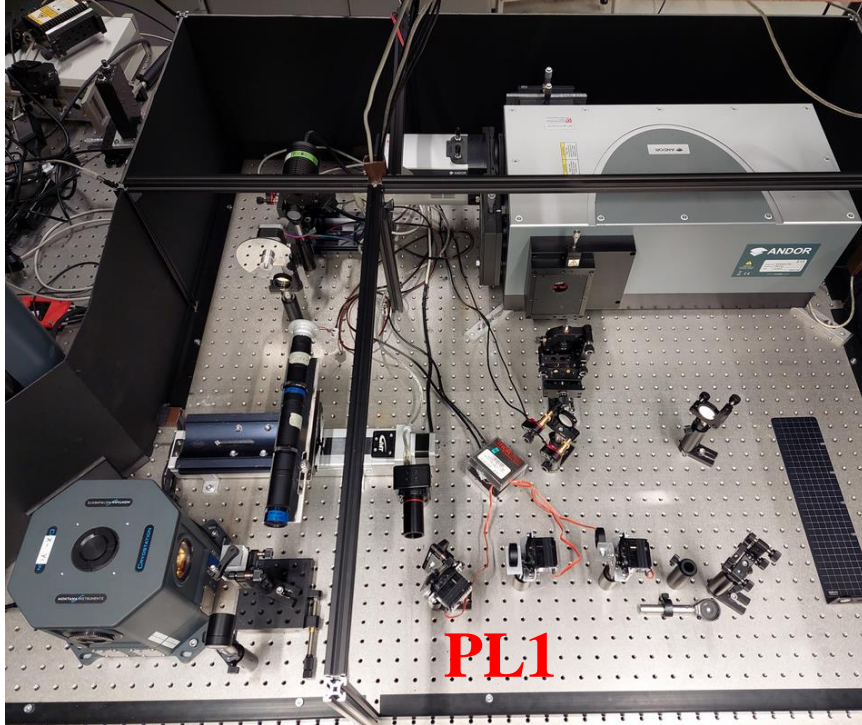
# Basic Micro-PL Spectrometer



- **Sample cooling (4 K)**
- **Micro-PL (confocal microscope)**
- **Extensions: ultra-high resolution, lifetime, polarization, correlation, ...**

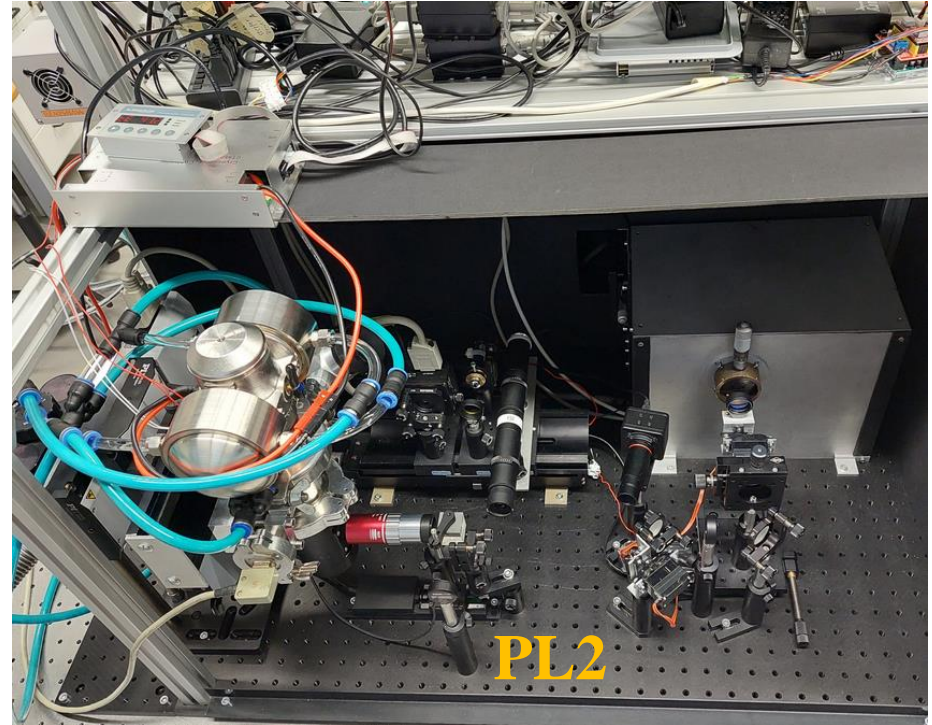


# PL-Setups



## PL1

- Sample cooling down to 3 K
- Ultra-low vibrations
- Extensions: high resolution, lifetime



## PL2

- Sample cooling down to 30 K

# PL-Setups: Software

SpecControl by Ch. Heyn (V. 17.09.2021), System: PortaLab, Camera: ZWO ASI1600MM Pro (4656 x 3520), Gratings: (1) 1200\_blaze750

-- Status --

Laser: 1.2 W

T-Camera: warm

-- Spectrometer --

Reset settings

WL: 700.0 nm

700 Go

Setup mono.

> Camera

Gain

139

0 100 200 300

Exposure

200

100-1000 ms

Camera cool.

Setup camera

> Capture

Capt. stripe

Adj.

Capture

time: 0.9 s

> Spectrum

Av.Y

1 15

Remove dark

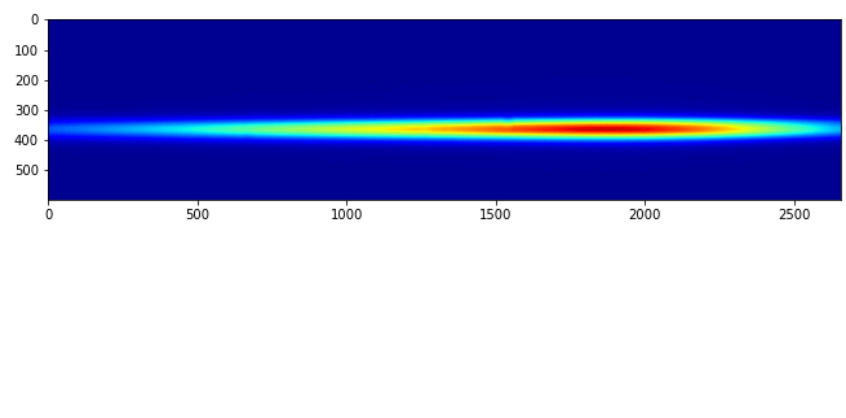
Auto line

> Save

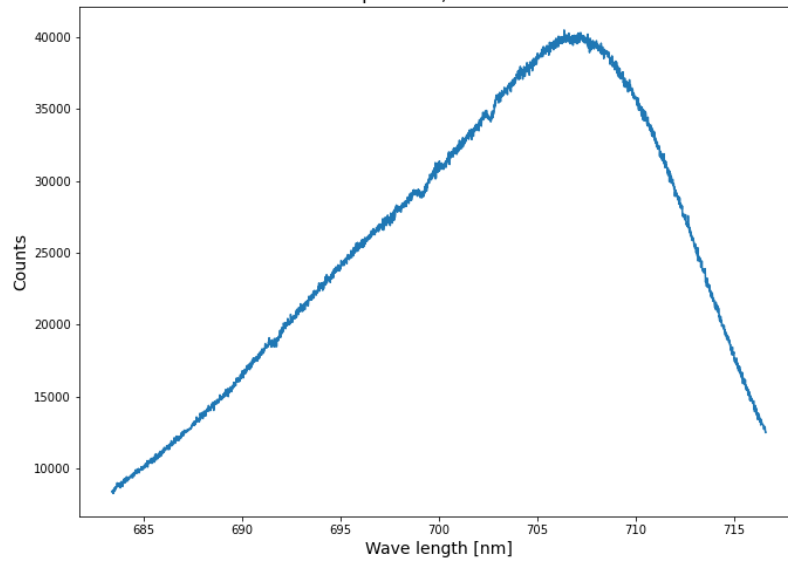
Save image

Save spectrum

Quit



Spectrum, line 361



-- Stage --

10  $\mu\text{m}$

x: 0.0  $\mu\text{m}$

-x +x 0

y: 0.0  $\mu\text{m}$

-y +y 0

z: 0.0  $\mu\text{m}$

-z +z 0

-- Microscope --

Camera -> ON

Show cross

Exposure

1

1 3 5 7 9

Brightness

0

-64 0 64

-- Laser --

Laser -> OFF

I [mA]: 0.5 Set

Laser: 3.01 V, 0.401 A, 1.2 W

-- Peltier --

Peltier -> ON

V [V]: 0 Set

Peltier: OFF

-- Spectrum --

Av.X

1

1 25 Set

Save spectrum

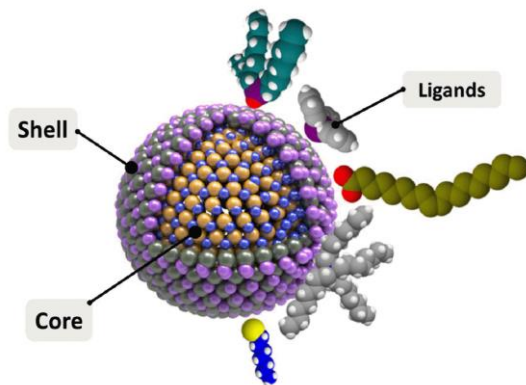
Load spectrum



# Fabrication of Semiconductor Quantum Dots

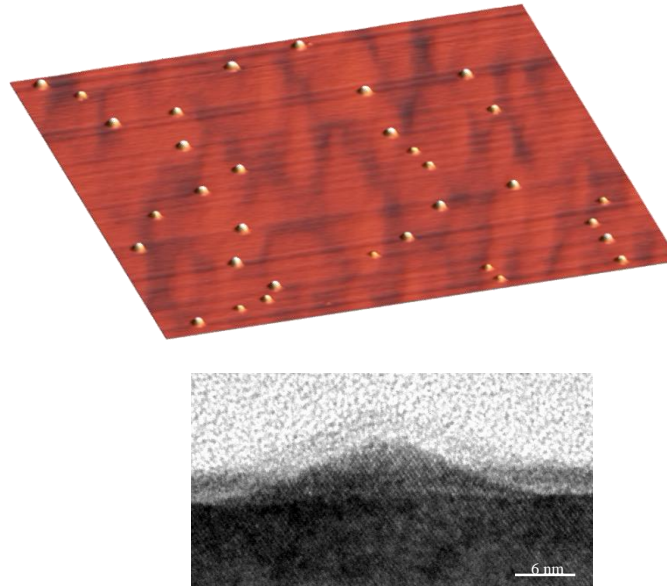
## Synthesis of colloidal QDs

- Powder / in a liquid
- + Mass production
- Contacts (ligands)
- Optical instability (blinking)



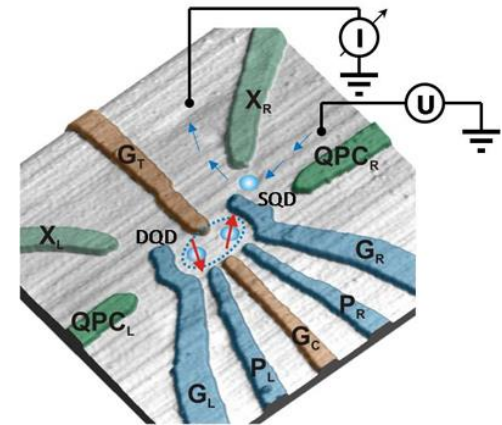
## Self-assembly of epitaxial QDs

- Wafer based
- + Tunable density
- + Contacts
- + Optically stable

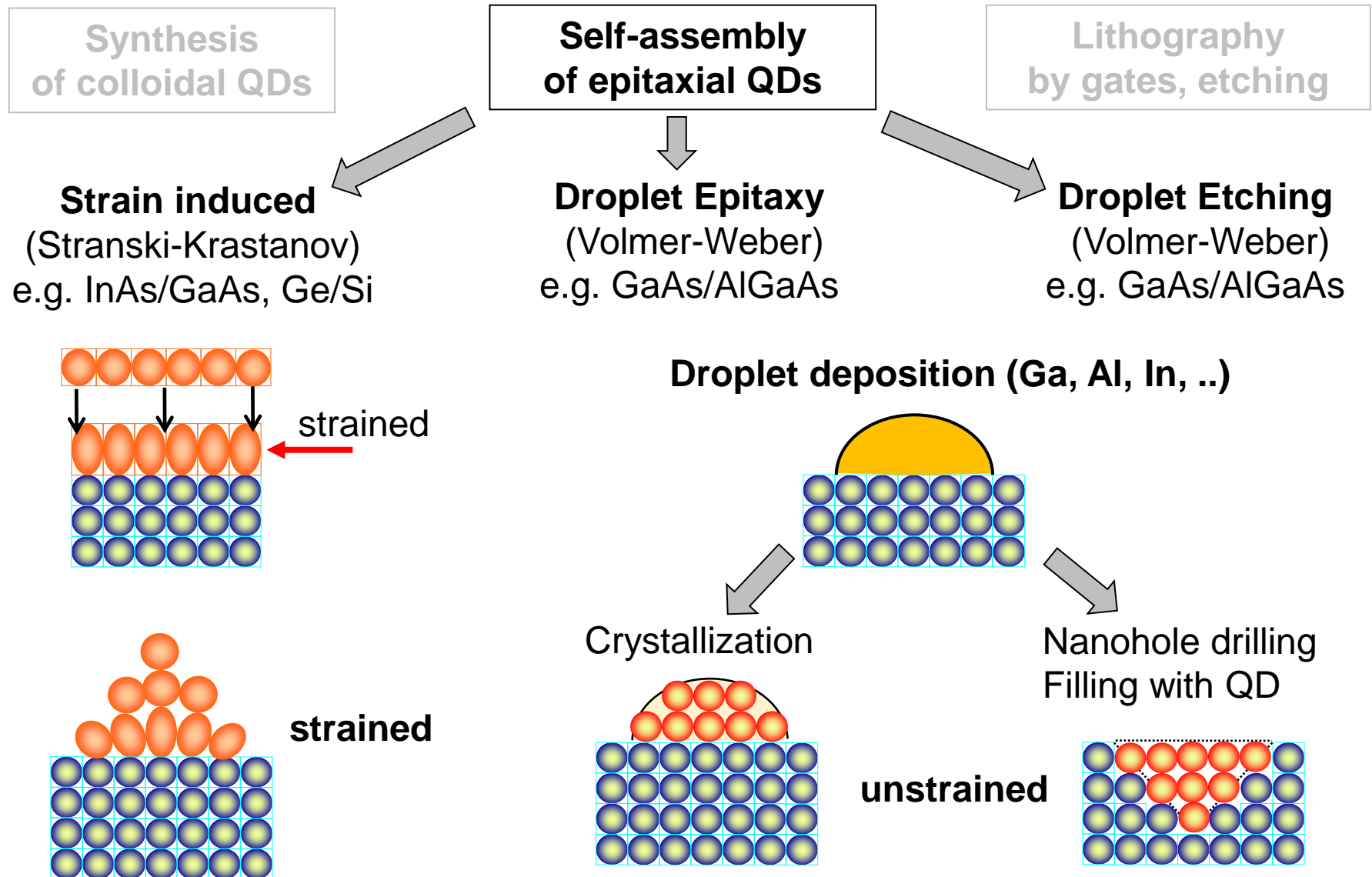


## Lithography by gates, etching

- Wafer based
- + Single QDs
- + Contacts
- Optical emission



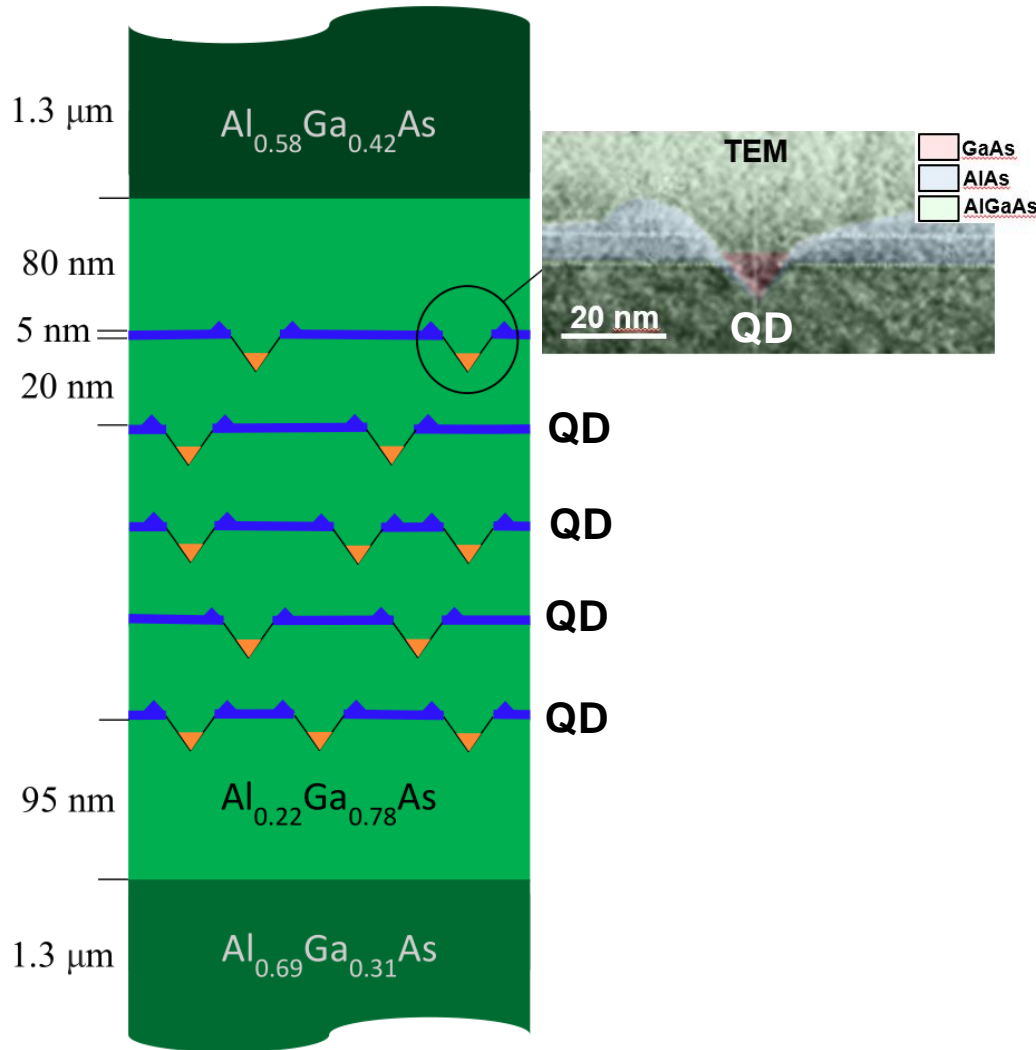
# Fabrication of Semiconductor Quantum Dots



# QD Samples

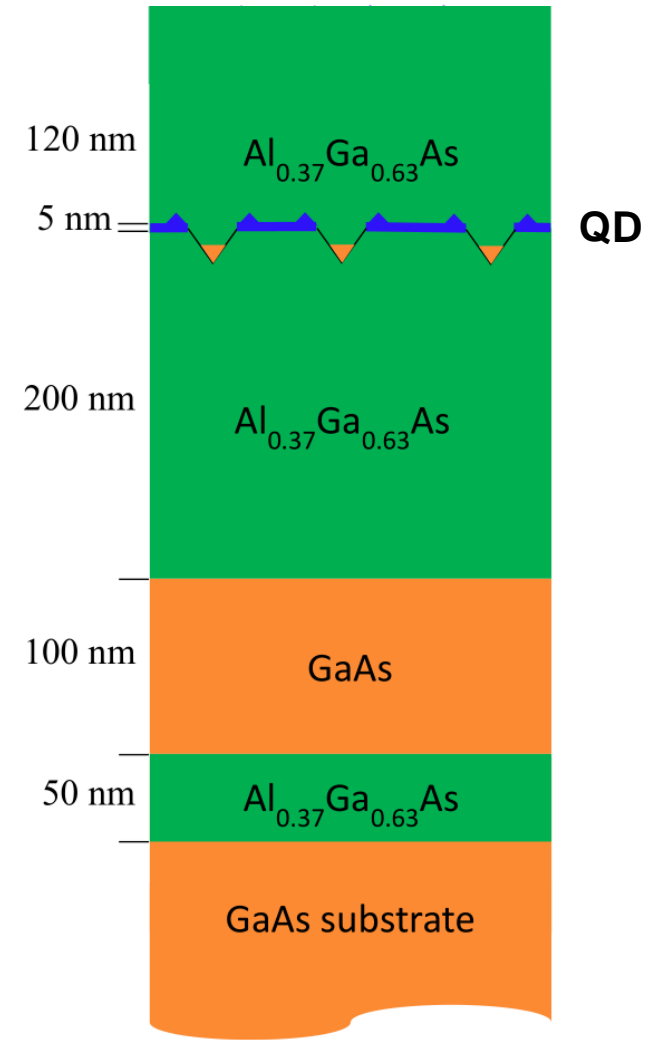
## QD-Probe A („Spezial“)

5 Lagen GaAs QD in dickem AlGaAs



## QD-Probe B („Standard“)

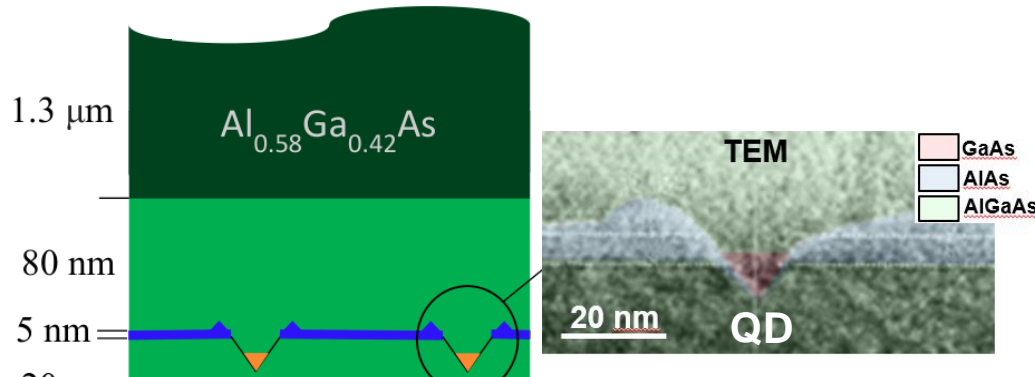
1 Lage GaAs QD in dünnem AlGaAs



# QD Samples

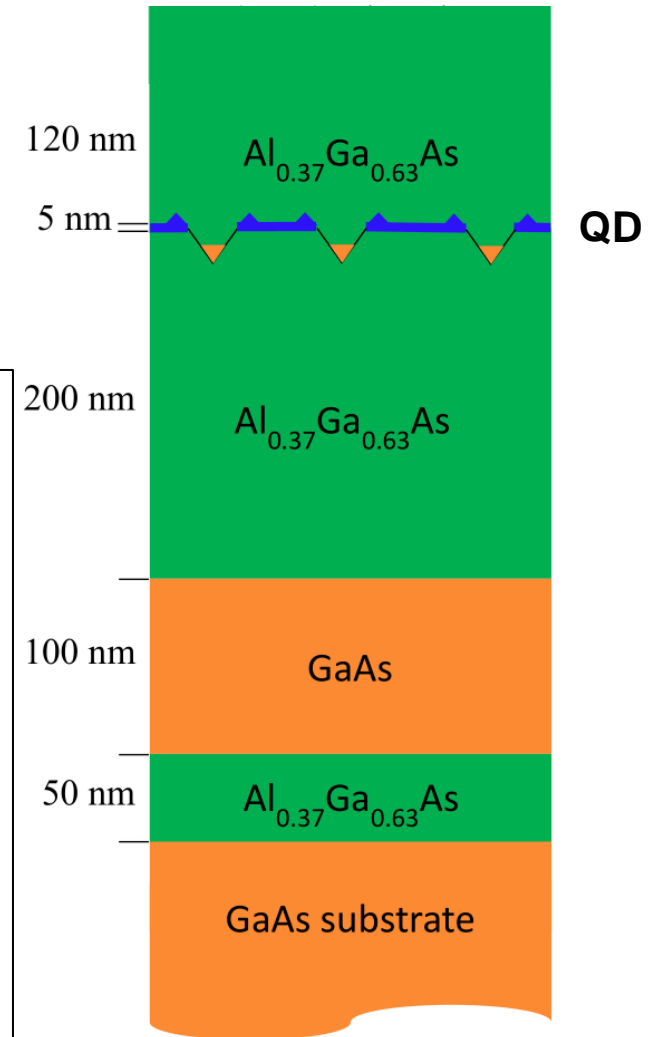
## QD-Probe A („Spezial“)

5 Lagen GaAs QD in dickem AlGaAs



## QD-Probe B („Standard“)

1 Lage GaAs QD in dünnem AlGaAs



Intensity

**GaAs substrate**

T dependent

left: bandgap

right: Fermi distribution

**$\text{Al}_x\text{Ga}_{1-x}\text{As}$  barrier**

x dependent

T dependent

**GaAs QDs**

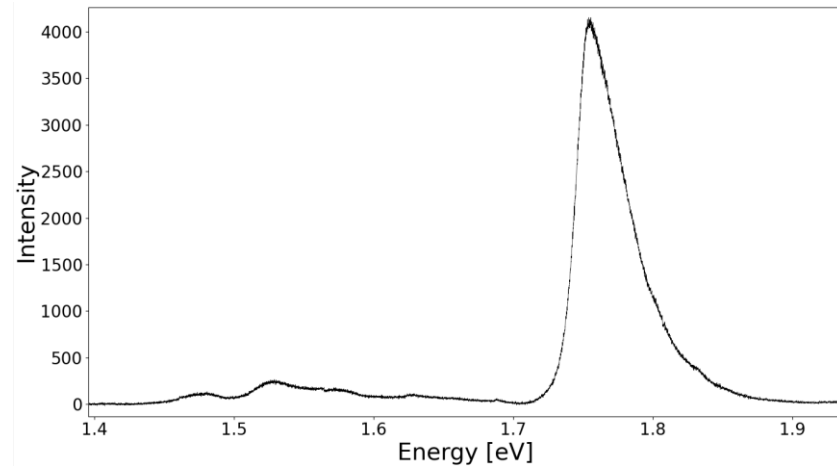
T dependent

$E_0, E_1, E_2, \dots$

**E**



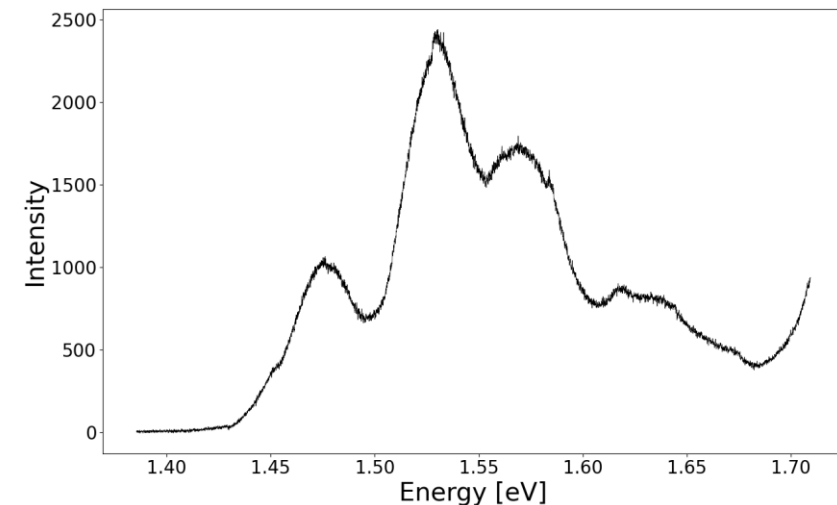
# QD Sample A



## Messung an QD-Probe A bei $T = 300$ K:

(Bereich 600-900 nm, zusammengesetzt aus Einzelspektren)

- Starker AlGaAs-Peak + schwache QD Peaks
- Zoom: QD-Peaks mit 4 Energieniveaus



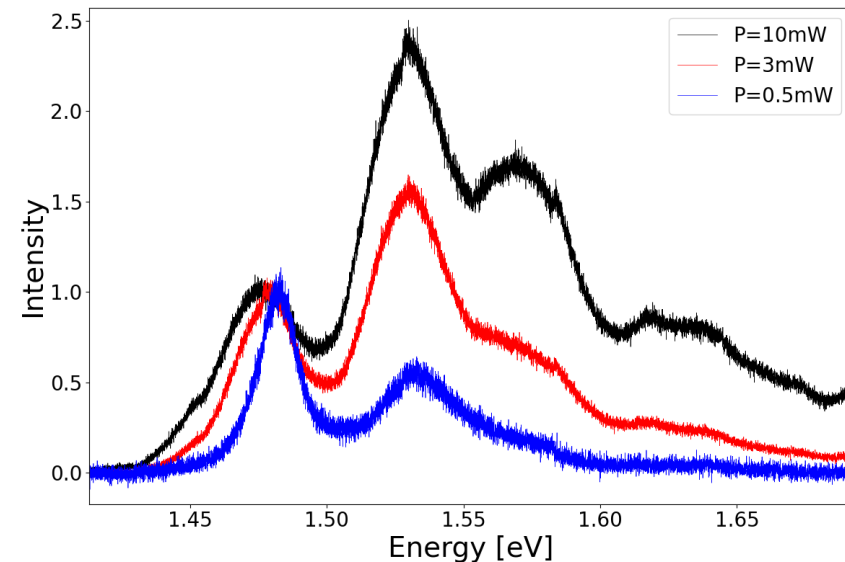
## Auswertungen:

- QD-Peaks sind (halbwegs) äquidistant:  
→ parabolisches Potenzial
- Bestimmung der Quantisierungsenergien
- Abschätzung der QD-Größe (Ausdehnung der Wellenfunktion)
- Abschätzung der Coulomb-Wechselwirkung zwischen Elektron und Loch

## QD-Probe A, Einfluss Laserleistung P

Bei reduzierter Laserleistung:

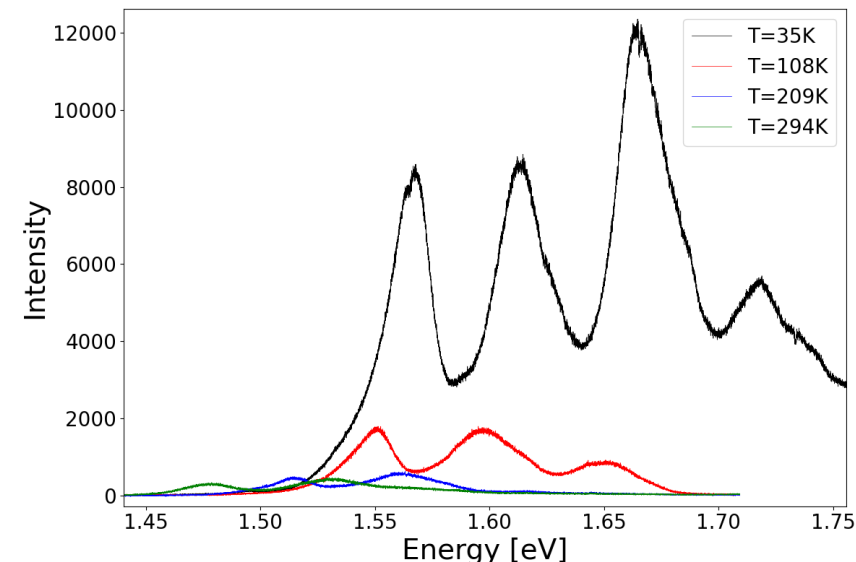
- Abnehmende Intensität
- Relative Abnahme höherer Schalen (Besetzungsstatistik)
- Blauverschiebung des Grundzustandes (Rotverschiebung durch höhere Schalen)



## QD-Probe A, Einfluss Probentemperatur T

Bei Kühlung:

- Intensitätserhöhung (Reduktion thermischer Emission aus den QD)
- Blauverschiebung der Energieniveaus (Analog GaAs-Bandlücke)
- Besetzung höherer Schalen



# Location

Meeting point:

Office  
Christian Heyn

Center for Hybrid  
Nanostructures  
(CHyN)  
Luruper Chaussee 149  
Building 600

Room: **2.46**

