Answers

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1 Task: 1

- What does it do?
  it prints two not sufficiently seeded "random" variables

- The difference between the methods is that rand() returns a random number and the other method

  - rand() returns a random integer between 0 and RANDMAX
  - gsl_rng_mt19937 is a generator that generates random numbers

  In the code the generator is passed to a (Distribution)function that uses this generator to evaluate a random number depending on the Distribution specified in the function.

- What happens if you remove the expression (double)?
  The division operation $\frac{rand()}{RANDMAX}$ does $\frac{intSmall}{intBig}$ and should result in a double, but with no cast it will be floored to 0.

- Is there a direct function to generate normally distributed random variables?
  double gsl_ran_gaussian_pdf(const gsl_rng * r, double sigma) command

2   Task: 3

The Plot should simulate the occurencedensity of points of our 1.000.000 samples which are normally distributed. But the picture shows that all points are over the exact Plot of the density function what ist nearly impossible with so many samples. Therefor we conclude that the plot was made with different parameters.
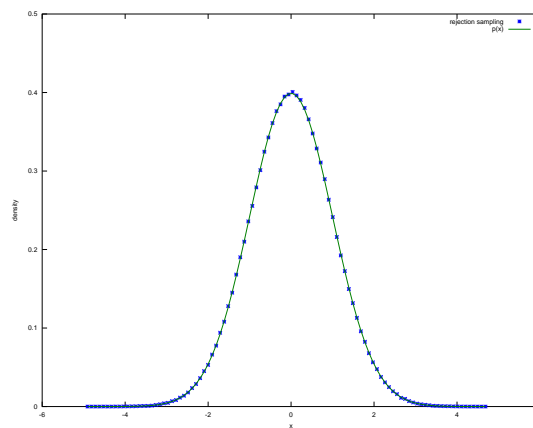
3   Task: 4

We can sample a uniformlly y in the intervall [0,1] and apply the inverse cdf to sample a normally distributed variable

4 Task: 5

The Algorithm uses a interpolation (see fig. 1) with maximal estimation error: $2 * 10^{-9}$ (see fig. 2) where the upper half of the Distributionfunction is devided into 2 sections in which interpolations where made. If x is in the lower halft of the Distributionfunction, than 1-NomralCDF(-x) will be used to use the symmetric property.
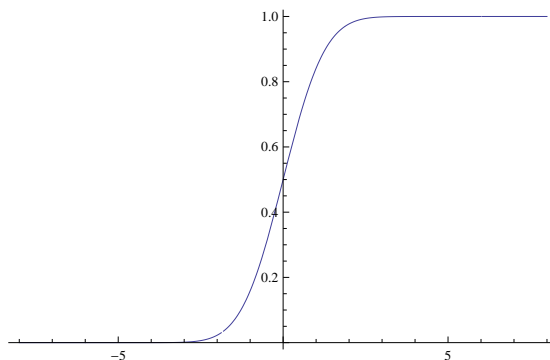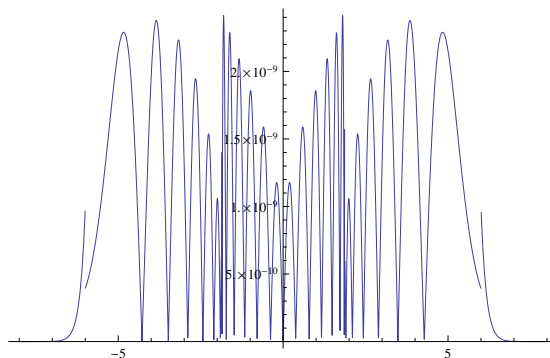

Figure 1: Plot of Approximation
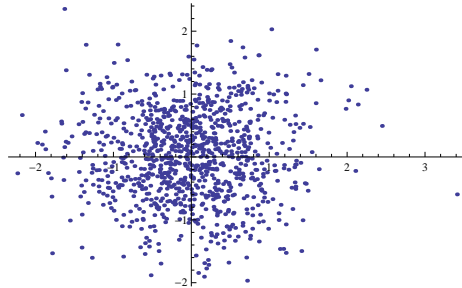

Figure 2: estimation error

5 Task 6

Figure 3: 2D Plot

6 Task 7

7 Task 8

The algorithm need only one summation instead of two. The algorithm interates new samples to the total solution of the last step, so it could work better if we constantly give new sampels to the old ones because there is no need to run the hole calculation again.
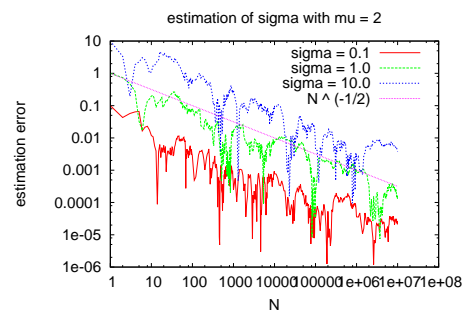
8 Task 9

We think that the error drops with the rate $\frac{1}{\sqrt{N}}$

Figure 4: estimation error