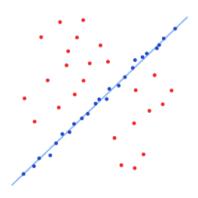
# Probabilistic Robotics Course

## **RANSAC**

### Giorgio Grisetti

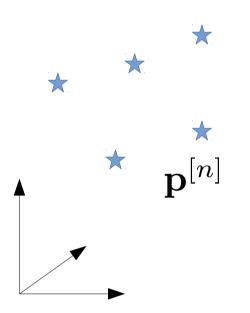
grisetti@diag.uniroma1.it

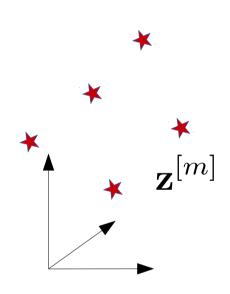
Department of Computer, Control, and Management Engineering Sapienza University of Rome



# **3D Point Registration**

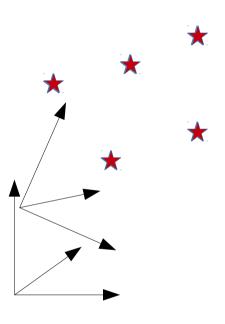
Unknown correspondences and initial guess!





# **3D Point Registration**

We want to find a transform that minimizes the distance between corresponding points

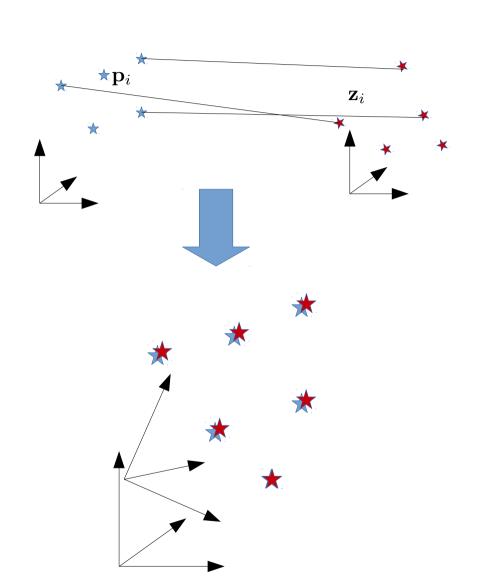


## What if...

we knew a minimal set of correct correspondences?

#### We could:

- find an initial guess of our system by using the tools we have learned so far
- with this initial guess, we could find more "good" correspondences
- we could determine the solution by considering all "good" correspondences, and dropping the bad ones

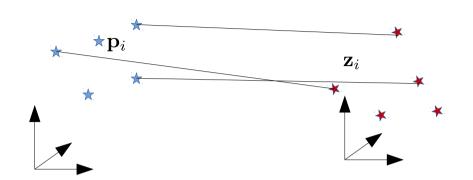


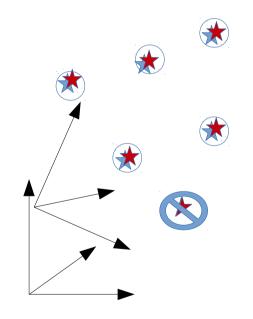
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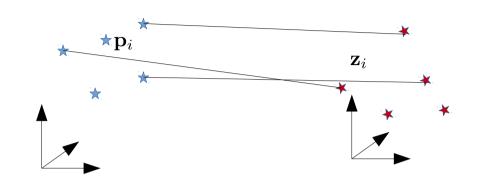


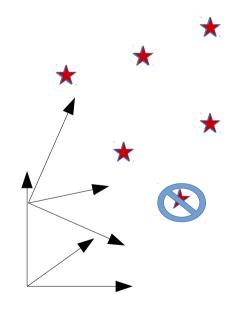
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## **RANSAC**

#### Random Sample Consensus

#### For N times:

- Sample (randomly) a minimal set of correspondences among the candidate ones
- With this minimal set compute an initial alignment
- Use this alignment to determine the number of good/bad correspondences
- Compute the "consensus" of the guess as a function of number of inliers and error
- Repeat the above steps N times, and at each time keep the "best" solution

When done, use only inliers to improve the final solution.

## RANSAC: What do we need

RANSAC is a schema to seek for a good solution, not a "closed" algorithm

To implement the schema we need:

- A procedure to seek for correspondences (the better the procedure, the less iterations N are needed)
- A procedure to smartly select a set of pseudorandom (worst case: uniform) set between candidate correspondences
- A procedure to compute a solution, immune to poor initial guesses
- A procedure to count the inliers

## Correspondences

The correspondence search is usually done exploiting the appearance of features.

- •This usually leads to few "good" correspondences.
- •The correspondence search is characterized by an "inlier ratio" w, that is the number of good matches divided the number of points in the model.

#### In this example:

- we assume "all" points match with all other points, so we have N\*N correspondences (worst case)
- •the inlier ratio is 1/N (pretty bad)

## **Determining a Solution**

In this case, the initial guess is poor.

 We prefer linear relaxation to compute the initial solution, as it is immune from the initial guess.

$$\mathbf{x}^{T} = (\mathbf{r}_{1}^{T} \ \mathbf{r}_{2}^{T} \ \mathbf{r}_{3}^{T} \ \mathbf{t}^{T})$$

$$\mathbf{h}^{[i]}(\mathbf{x}) = \mathbf{R}\mathbf{p}^{[i]} + \mathbf{t}$$

$$\mathbf{b} = \sum_{i} \mathbf{M}^{[i]T}(\mathbf{p}^{[i]} - \mathbf{z}^{[i]})$$

$$= \begin{pmatrix} \mathbf{r}_{1}^{T} \\ \mathbf{r}_{2}^{T} \\ \mathbf{r}_{3}^{T} \end{pmatrix} \mathbf{p}^{[i]} + \mathbf{t}$$

$$= \begin{pmatrix} \mathbf{p}^{[i]T} \\ \mathbf{p}^{[i]T} \\ \mathbf{p}^{[i]T} \end{pmatrix} \begin{pmatrix} \mathbf{r}_{1} \\ \mathbf{r}_{2} \\ \mathbf{r}_{3} \end{pmatrix} + \mathbf{t}$$

$$\mathbf{A} = \begin{pmatrix} \mathbf{r}_{1}^{T} \\ \mathbf{r}_{2}^{T} \\ \mathbf{r}_{2}^{T} \end{pmatrix} = \mathbf{U}\mathbf{\Sigma}\mathbf{V}^{T}$$

 $\mathbf{R} = \mathbf{U}\mathbf{V}^T$ 

## **Pruning Correspondences**

In absence of a reasonable appearance-based correspondence selection we can exploit some invariants: the distance in the space.

- We can select a triplet of points in the world that are reasonably distant from each other
- We can select a triplet of points in the measurement that have more or less the same distances

This is not part of RANSAC. It is just a simple optimization that might help us pruning wrong correspondences

Typical feature-based matching might have inlier ratios: w>0.2

## **Selecting Inliers**

Given three correspondences, we can "count" the inliers.

- We compute the error of each corresponding point under the solution
- We "count" the number of correspondences that are "good"
- More good points will correspond to a better solution

## How many rounds?

RANSAC is a random procedure, so we are never guaranteed that the solution found is correct.

We can however ask "what is the probability of having a correct solution"

To this extent we need to know

- •The inlier ratio w of the correspondences
- •The number of points n required to compute the initial solution

# How many rounds?

w: inlier ratio

n: min number of model points

p: desired probability of success