

Galois-Feld $\text{GF}(8)$ A4

Berechnen Sie $(x^2 + x + 1) \odot (x^2 + x)$ in $\text{GF}(8)$

$$(x^2 + x + 1) \cdot (x^2 + x) = x^4 + \cancel{x^3} + \cancel{x^2} + \cancel{x^3} + \cancel{x^2} + x$$
$$= x^4 + x$$

$$x^4 + x = x(x^3 + x^2 + 1) + x^3$$

$$x^3 = 1 \cdot (\overset{x^4}{x^3} + \overset{x^3}{x^2} + \overset{x}{1}) + x^2 + 1$$

$$\Rightarrow (x^2 + x + 1) \odot (x^2 + x) = x^2 + 1 \stackrel{!}{=} 101$$