

```
1  from __future__ import division
2  from math import sin,pi
3  from numpy import empty,array,arange
4  from pylab import plot,show
5
6  g = 9.81
7  l = 0.1
8  theta0 = 179*pi/180
9
10 a = 0.0
11 b = 10.0
12 N = 100          # Number of "big steps"
13 H = (b-a)/N      # Size of "big steps"
14 delta = 1e-8     # Required position accuracy per unit time
15
16 def f(r):
17     theta = r[0]
18     omega = r[1]
19     ftheta = omega
20     fomega = -(g/l)*sin(theta)
21     return array([ftheta,fomega],float)
22
23 tpoints = arange(a,b,H)
24 thetapoints = []
25 r = array([theta0,0.0],float)
26
27 # Do the "big steps" of size H
28 for t in tpoints:
29
30     thetapoints.append(r[0])
31
32     # Do one modified midpoint step to get things started
33     n = 1
34     r1 = r + 0.5*H*f(r)
35     r2 = r + H*f(r1)
36
37     # The array R1 stores the first row of the
38     # extrapolation table, which contains only the single
39     # modified midpoint estimate of the solution at the
40     # end of the interval
41     R1 = empty([1,2],float)
42     R1[0] = 0.5*(r1 + r2 + 0.5*H*f(r2))
43
44     # Now increase n until the required accuracy is reached
45     error = 2*H*delta
46     while error>H*delta:
47
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48         n += 1
49         h = H/n
50
51         # Modified midpoint method
52         r1 = r + 0.5*h*f(r)
53         r2 = r + h*f(r1)
54         for i in range(n-1):
55             r1 += h*f(r2)
56             r2 += h*f(r1)
57
58         # Calculate extrapolation estimates. Arrays R1 and R2
59         # hold the two most recent lines of the table
60         R2 = R1
61         R1 = empty([n,2],float)
62         R1[0] = 0.5*(r1 + r2 + 0.5*h*f(r2))
63         for m in range(1,n):
64             epsilon = (R1[m-1]-R2[m-1])/((n/(n-1))**(2*m)-1)
65             R1[m] = R1[m-1] + epsilon
66         error = abs(epsilon[0])
67
68         # Set r equal to the most accurate estimate we have,
69         # before moving on to the next big step
70         r = R1[n-1]
71
72     # Plot the results
73     plot(tpoints,thetapoints)
74     plot(tpoints,thetapoints,"b.")
75     show()
76
```