

Language and Speech Technology - Assignment 1

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Part I

File can be found attached to the e-mail.

Part II

Assignment 3

a.

$$\begin{aligned}x_1(t) &= \operatorname{Re}\{A_1 e^{i\phi_1} e^{i2\pi f_1 t}\} \\x_2(t) &= \operatorname{Re}\{A_2 e^{i\phi_2} e^{i2\pi f_2 t}\}\end{aligned}$$

b.

$$\begin{aligned}x_3(t) &= \operatorname{Re}\{A_1 e^{i(2\pi f_1 t + \phi_1)} + A_2 e^{i(2\pi f_2 t + \phi_2)}\} \\ \text{since } f_1 &= f_2 \\ x_3(t) &= \operatorname{Re}\{A_1 e^{i(2\pi f t)} + A_2 e^{i(2\pi f t + \phi_2)}\} \\ x_3(t) &= \operatorname{Re}\{e^{i(2\pi f t)}(A_1 e^{i\phi_1} + A_2 e^{i\phi_2})\}\end{aligned}$$

c.

$$\begin{aligned}A_1(\cos(\phi_1) + i\sin(\phi_1)) &= 1.3(\cos(0) + i\sin(0)) = 1.3 \\ A_2(\cos(\phi_2) + i\sin(\phi_2)) &= 1.2(\cos(0.9\pi) + i\sin(0.9\pi)) = 1.2(-0.95 + 0.31i) = \\ &= -1.14 + 0.37i\end{aligned}$$

d.

$$\begin{aligned}z_D &= 1.3 + 0i \\ z_E &= -1.14 + 0.37i \\ z_D + z_E &= 1.3 + (-1.14 + 0.37i) = 0.26 + 0.37i\end{aligned}$$

e.

$$0.26 + 0.37i = r(\cos(\theta) + i\sin(\theta))$$

$$r = 0.26^2 + 0.37^2 = 0.20$$

$$\tan^{-1}(0.37/0.26) = 0.96$$

$$0.20(\cos(0.96) + i\sin(0.96)) = 0.20e^{i0.96}$$

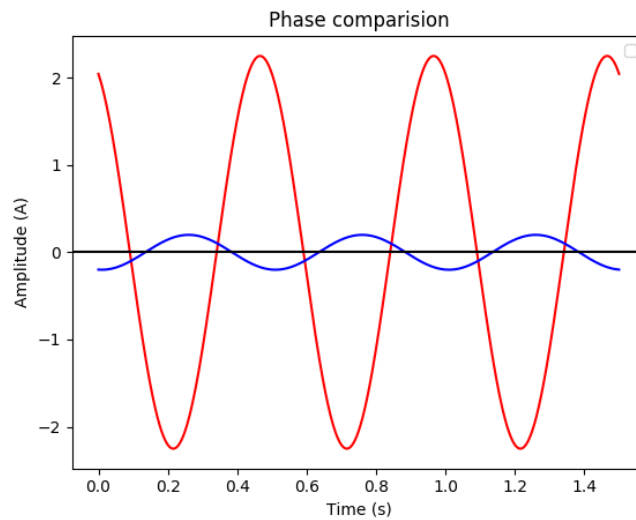
f.

$$x_3(t) = \text{Re}\{0.20e^{i0.96}e^{i(2\pi 20t)}\}$$

$$A_3 = 0.20$$

$$\phi_3 = 0.96$$

Assignment 4



Assignment 5

a

$$A_3 = (A_1\cos(\phi_1) + A_2\cos(\phi_2))^2 + (A_1\sin(\phi_1) + A_2\sin(\phi_2))^2$$

$$\phi_3 = \tan^{-1}\left(\frac{A_1\sin(\phi_1) + A_2\sin(\phi_2)}{A_1\cos(\phi_1) + A_2\cos(\phi_2)}\right)$$

b

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