PLEASE ATTACH THIS SINGLE SHEET FACING OUT ON THE BACK OF YOUR HW. We are attempting to reduce bias in grading by keeping the names off of the front of the HW. Studies show that we can easily be unintentionally biased by names, even when we are trying to be fair (search names and bias if you want to learn more). Thanks!

Reminder: Please familiarize yourself with the HW expectations policy on Sakai as well as the information about collaboration in the class syllabus. Graders are aware of these policies and may take points off. The purpose of the guidelines is for you to practice good communication and to make things do-able for your dear graders.

Name: _____

Section (Circle one)   1: MW 1:15   2: MW 2:45   3: TTH 1:15

Due date: Friday, January 27 at noon in the Engineering lounge.

Outside sources and how I used them: _____

_____

Collaborators: _____ .

I spent about _____ **hours on this assignment.**

I still need to better understand: _____

_____

POINTS (graders can fill for # problems on this HW)

1		6	
2		7	
3		8	
4		9	
5		Σ	

1, 2, 3, 4, 5

1 The deflection δ of the tip of a cantilever beam depends on the applied force P, the beam length L, the elastic modulus (a material property that characterizes stiffness and has dimensions force/length^2) E, and a property of the cross section called the second moment of area, which is represented with the symbol I and has dimensions of length^4. Experience with analysis of beams would tell us that it is always the product of E and I that determines deflection, so we may work with the grouped quantity EI from the outset.

(a) Choose force (and not mass) as one of the fundamental dimensions. Develop a set of dimensionless parameters for this problem. Choose parameters such that δ appears in only one of them.

(b) Show that if you were to have used mass as one of the fundamental dimensions you would get the same number of dimensionless groups.

(c) The theoretical tip deflection is

$$\delta = \frac{PL^3}{3EI}.$$

If you were to do a set of experiments by varying problem parameters and measuring values for δ you could determine the functional relationship connecting your dimensionless parameters. Assuming that this relationship is a power law, sketch a plot that shows the regression line (indicating its intercept and slope) that you would expect if your data corresponded to the theoretical deflection.

2 In 1945, the United States conducted the Trinity nuclear test in New Mexico as part of the Manhattan Project. This photo was published in Life magazine. Much to the chagrin of the US government, fluid dynamics professor Geoffrey Taylor used the photo below and other unclassified ones like it (all had scale bars) and the Buckingham Pi theorem to estimate the yield of the blast (in kilotons of TNT)—which was definitely classified information!

(a) Determine a dimensionless parameter that relates the blast energy E, radius of the shock wave R at time t and air density ρ.

(b) Taylor did experiments with smaller explosives and determined that the value of his version of this parameter was approximately 1. That is convenient, because yours is 1 too, even if your parameter is his to some power. Here is some of the data from his paper (which is in Resources on Sakai if you are interested). What is your estimate of the blast energy in Joules? In kilotons of TNT? The true (then classified) answer is about 21 kilotons. How good is your estimate?

t (ms)	R (m)
0.24	19.9
0.94	36.3
1.93	48.7
3.26	59.0
4.61	67.3
15.0	106.5
62.0	185.0

(c) In general, if a physical problem is described by one dimensionless parameter, what can we say about that parameter?

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3 A thermistor is a temperature-dependent resistor. This problem is about the kind of thermistor that has a higher resistance as it gets hotter, so it can be used as a fuse. If the current surges, the resulting Joule heating (due to Power $= I^2R$) increases the resistance and so cuts the current. This is nice because when the current surge goes away and the thermistor cools down and normal operation can resume without the replacement of a fuse. This is how hairdryers switch themselves off for awhile when they get too hot. Our goal is to understand how characteristics of a thermistor and its operating conditions are related to its resistance.

The resistance across a disk like a thermistor can be written as $\rho d / A$, where ρ is the resistivity of the material (this is what changes with temperature; typical units are $\Omega \cdot$m), d is the thickness of the disk and A is the circular cross sectional area. Other material properties that are significant are the heat transfer coefficient $h \left(\frac{W}{m^2 K} \right)$ and the thermal conductivity $k \left(\frac{W}{mK} \right)$. The operating conditions are specified by V, the voltage across the thermistor, and ΔT, the change in temperature from the reference temperature.

Develop a set of dimensionless parameters that relate ρ, d, A, h, k, V and ΔT. There is not a unique choice of fundamental dimensions. Be sure you have an independent set.

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4 In 2012, the Curiosity rover (mass m = 900 kg) landed on Mars. It approached the planet at 20000 km/hour. Atmospheric drag slowed it to about 1600 km/hour, then a parachute opened, which slowed to 320 km/hr (90 m/s). Rockets then completed the deceleration so it could make a gentle landing. How did NASA engineers design a parachute that they knew would work on Mars? How could they predict the minimum diameter d of the parachute that they should use on Mars by doing tests on Earth?

(a) Relevant physical parameters include the acceleration due to gravity g and the atmospheric density ρ (considered constant on each planet: $\rho_{\text{Earth}} = 1.2 \text{ kg/m}^3$, $\rho_{\text{Mars}} = 0.02 \text{ kg/m}^3$). The atmospheric viscosity is not important for this rough analysis because it is low on both planets. Develop a set of dimensionless parameters for this problem. Remember that this set of parameters is not unique, and so to answer the next parts of the question you might want to consider a different set.

(b) Using a model rover on Earth, what set of experiments and analysis would you do to solve the design problem of finding the correct minimum diameter? Explain clearly for full credit.

(c) The parachute used for the rover on Mars actually had a diameter of 20 m. What single test (one diameter parachute) on Earth with a 10 kg model rover could prove this to be correct for a 90 m/s Mars terminal velocity? What velocity would be measured in the Earth experiment?

5 Find the 95% confidence interval for the mean terminal velocity calculated during the first class for the steel ball (with d = 15.88 mm and w = 0.1603 N) falling in oil (with ρ = 920kg/m^3 and μ = 0.067 Pa·s). Find the 95% prediction interval for the terminal velocity of a ball dropped in one trial under the same conditions.