Symmetries Tutorial

GamesCrafters 2006



2006-11-15 Yanpei Chen

Symmetries Tutorial

Agenda

What are symmetries

Why are they needed

Common symmetries

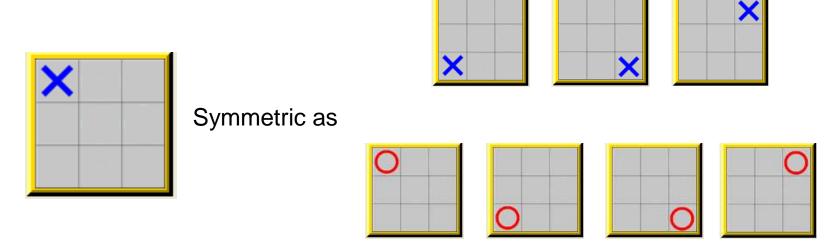
How to implement symmetries

What are symmetries

Symmetric positions are

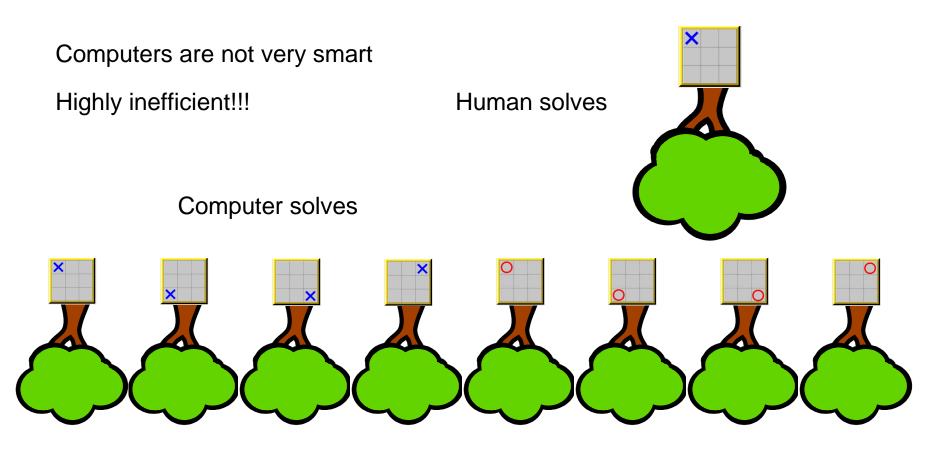
Any class of positions that are the "equivalent" for humans

But "different" for computers



The position at left is the representative "canonical position" of all eight positions Symmetries depend on game rules

Why do we need symmetries



Symmetries lead to huge space and time savings

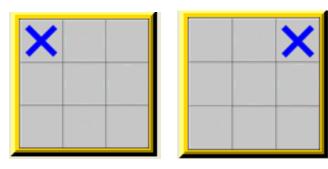
Space savings – we could store only the canonical in the database

Time savings – we could solve only the canonical positions

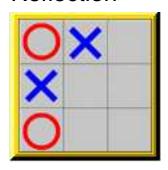
Common symmetries

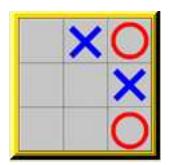
Geometric symmetries

Rotation



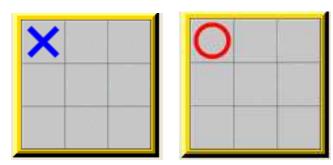
Reflection





Symmetries in pieces

Switching

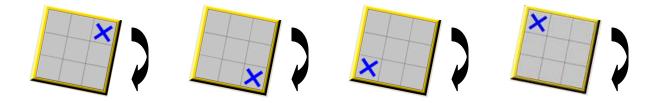


Other equivalences in pieces

Other game specific stuff

Spinning – Finding the Canonical Position

Often the canonical position is the position with the smallest hash value For Gamesman, POSITION is the hash value So canonical position = smallest POSITION in the equivalent class Given a POSITION, we find all its equivalent, symmetric "brothers" This is done by simulating spinning the board around and rehashing Then we designate board with the smallest hash value as the canonical



Thus finding the canonical position is often referred to as "spinning"

How to Implement Symmetries

Game modules need to implement only one function

POSITION gCanonicalPosition (POSITION p); Must adhere to interface Takes in any position Performs spinning Returns the canonical position

Freedom in implementing game specific symmetries

How to Turn on Symmetries

```
---- Main (Pre-Solved) Menu for Ouarto ----
       s)
               (S)TART THE GAME
       w)
               START THE GAME (W)ITHOUT SOLVING
       Evaluation Options:
       0)
               (0) bjective toggle from STANDARD to REVERSE
       d)
               (D) ebug Module BEFORE Evaluation
       g)
               (G)ame-specific options for Quarto
       2)
               Toggle (2)-bit solving (currently OFF)
       p)
               Toggle Global (P)osition solving (currently OFF)
       1)
               Toggle (L)ow Mem solving (currently OFF)
               Toggle Sy(M)metries (currently OFF)
       m)
       h)
               (H)elp
               (Q)uit
       q)
```

Examples

```
Symmetries implemented in
```

Tic-Tac-Toe – Simple; mttt.c

Bagh Chal – Simple; mbaghchal.c

Quarto! – Not so simple; mquarto.c

Others?

Add to this list!!!

Summary

Symmetries = positions that are the "same" to humans

Need because wasteful to solve many symmetrical positions

Common symmetries – geometric, pieces

Implement using POSITION gCanonicalPosition (POSITION p);