Is the Curry boiling?

A model checker for Inquisitive Semantics

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Introduction

- Inquisitive semantics is a framework for analysing information exchange.
- We will make a model checker for the most basic version of this framework (InqB).

Inquisitive Semantics

- Classical formal semantics are suitable for analysing declarative sentences.
- However, they are not equipped to analyse questions such as:
 - "Is the Curry boiling?"
- Inquisitive semantics was developed at the ILLC to overcome these issues.

Models

- A first order inquisitive model $M = \langle W, D, I \rangle$ where
 - W is a set of possible worlds;
 - *D* is a non-empty set of individuals;
 - *I* is an interpretation function.

```
type World = Int
type Universe = [World]
type Individual = String

type Domain = [Individual]
type UnRelation = [(World, [Individual])]
type BiRelation = [(World, [(Individual, Individual)])]
```

Models in Haskell

Information States

- The semantics of InqB are given in terms of sets of worlds rather than in worlds.
- We call these sets of worlds information states.

```
type InfState = [World]
```

Propositions

- Propositions are non-empty, downward-closed sets of sets of worlds
- Intuition: A proposition consists of the information states that resolve the issues raised by that proposition.
- We represent a propositions by its maximal elements, called alternatives.
- A proposition has informative content and inquisitive content

Propositions in Haskell

```
type Prop = [[World]]

alt :: Model -> Form -> [InfState]

alt m f = sort [x | x <- p, not (any (strictSubset x) p)]
    where p = toProp m f

info :: Model -> Form -> InfState
info m f = sort . nub . concat $ toProp m f
```

Support of Propositions

- We say that an information state supports a propositions if its an element of it.
- In other words, s supports P iff $s \in P$.

```
supportsProp :: InfState -> Prop -> Bool
supportsProp s p = s `elem` p
```

Formulas

The language of InqB is that of first order logic:

```
type Var
                  = String
data Term
                = Indv Individual | Var Var
        deriving (Eq. Ord, Show)
data Form = UnR UnRelation Term
            Bink Bikelation Term Term
           TertR TertRelation Term Term Term
          | Neg Form | Con Form Form | Dis Form Form
          | Impl Form Form
            Forall Var Form | Exists Var Form
          deriving (Eq, Ord, Show)
```

Special Operators

- Furthermore, there are two special operators: ! and ?.
- The operators ! and ? make a formula non-inquisitive and non-informative, respectively.
- As they are abbreviations, we implemented them as functions:

```
nonInq :: Form -> Form
nonInq = Neg . Neg
nonInf :: Form -> Form
nonInf f = Dis f $ Neg f
```

Semantics

Formulas can be interpreted in a model as propositions.

 In the other clauses of this function we use more complicated helper functions. We will not go into those clauses.

Model checker

 An information state supports a formula if it is an element of the corresponding proposition.

```
supportsForm :: Model -> InfState -> Form -> Bool
supportsForm m s f = supportsProp s $ toProp m f
```

 Given a model, an information state and a formula, our model checker should check if that information state supports the formula.

Useful functions

```
isInquisitive :: Model -> Form -> Bool
isInquisitive m f
      = sort (toProp m f) /=
            (sort . powerset) (info m f)
isInformative :: Model -> Form -> Bool
isInformative m f
      = (sort . universe) m /= sort (info m f)
entails :: Model -> Form -> Form -> Bool
entails m f1 f2 = all ('elem' p2) p1 where
            p1 = toProp m f1
            p2 = toProp m f2
```

To do

- Implement QuickCheck;
- Check several well-known theorems of InqB using QuickCheck.