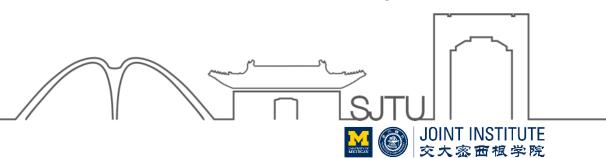


## ECE215 Final RC Part 3

**Chapter 13 Magnetically Coupled Circuits** 

Chen Yijia



## **Magnetically Coupled Circuits**

Inductance comes from magnetic flux.

$$v = N \frac{d\phi}{dt} = N \frac{d\phi}{di} \frac{di}{dt} = L \frac{di}{dt}$$

 $L = N \frac{d\phi}{DI}$  the self inductance of the coil

If two inductors are coupled, they will be affected by mutual inductance M.

The inducted voltage  $v=M\frac{di}{dt}$ 

Remember the unit of M (H) henrys

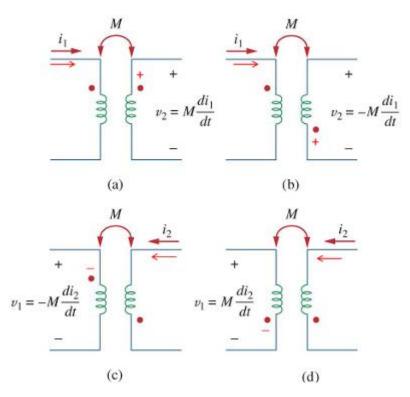
#### **Dot Convention**

We use dot convention to reduce the need of using Lens' law.

The dot convention is stated as follows:

If a current enters the dotted terminal of one coil, the reference polarity of the mutual voltage of the second coil is positive at the dotted terminal of the second coil.

Understand or copy to your CTPP

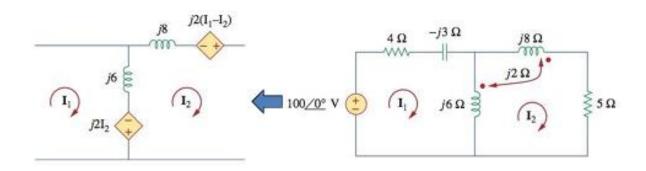


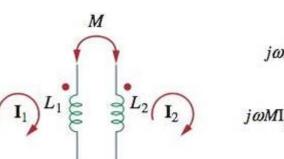


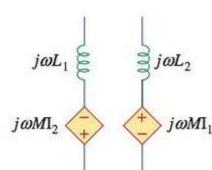
#### **Dot Convention**

For simplicity on analyzing, we assign a dependent voltage source

Pay attention to the current value







Phasor representation



## **Energy in Magnetically Coupled Circuits**

How to prove  $M_{12} = M_{21} = M$ 

refers to slide #28

$$w = \frac{1}{2}L_1i_1^2 + \frac{1}{2}L_2i_2^2 \pm Mi_1i_2$$

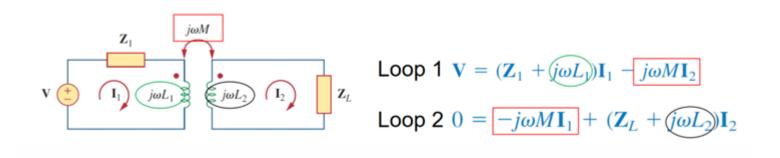
Positive if both entering the dot/ leaving the dot, otherwise negative.

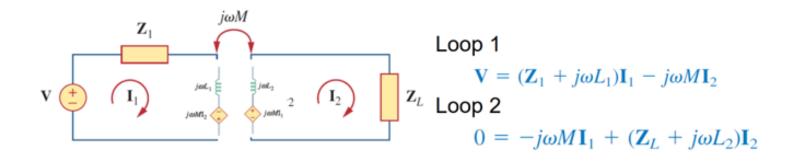
 $M \leq \sqrt{L_1 L_2}$  due to the power shouldn't be negative

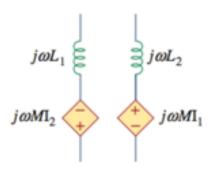
$$k = \frac{M}{\sqrt{L_1 L_2}}$$
 defines how two coils are coupled.  
k>0.5 tightly, k<0.5 loosely.

### **KVL** analysis

#### Pay attention to the dot convention

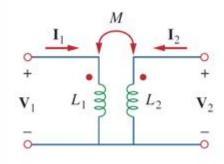


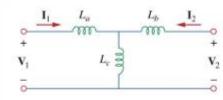




## **Equivalent circuit**

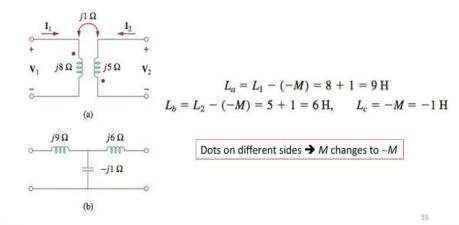
Equivalent T circuit



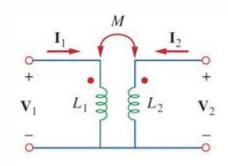


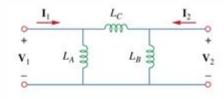
$$L_a = L_1 - M$$
,  $L_b = L_2 - M$ ,  $L_c = M$ 

Dot conventions!
Should be -M if not both entering at dots



Equivalent  $\pi$  circuit





$$L_{A} = \frac{L_{1}L_{2} - M^{2}}{L_{2} - M}, L_{B} = \frac{L_{1}L_{2} - M^{2}}{L_{1} - M} L_{C} = \frac{L_{1}L_{2} - M^{2}}{M}$$

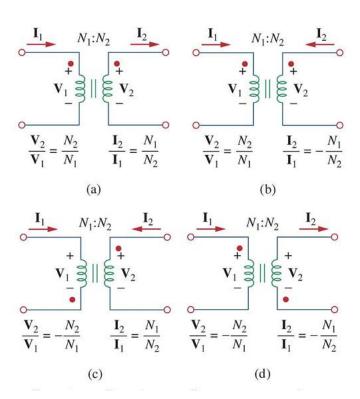


#### **Ideal transformers**

K=1,  $L=\infty$ , indicated by vertical lines Dot conventions!

Determine the sign of ration

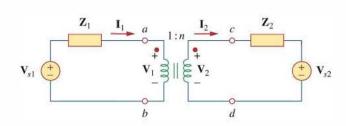
- (a) Voltages: both positive at the dotted terminals → +n Currents: I₁ enters whereas I₂ leaves the dotted terminal → +n
- (b) Voltages: both positive at the dotted terminals → +n Currents: Both enter the dotted terminals → -n

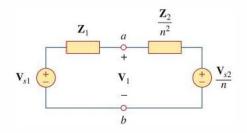


## Thevenin equivalent circuit

Use to simplify the circuit

Only apply when there are no external connections





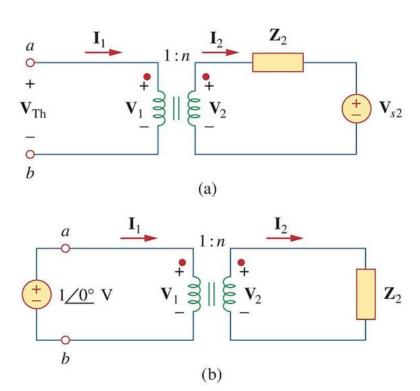
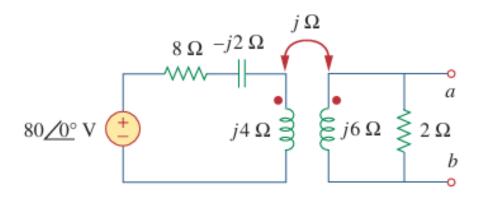


Figure 13.34 Obtaining the Thevenin equivalent for the circuit in Fig. 13.33.

### **Exercise**

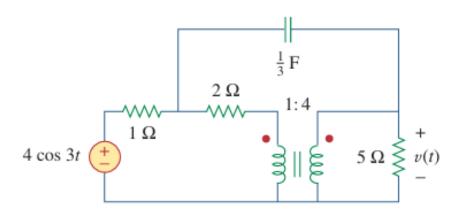
Obtain the Norton equivalent at the terminals a-b





### **Exercise**

Find v(t) for the circuit



### **Tips**

Review Homework and previous final exam

Understand the principle

If you can't, copy to CTPP

Good Luck!



### Reference

- 1. 2024 Fall VE215 slides, Sung-Liang Chen
- 2. 2023 Fall Final RC, Hengyi Cai
- 3. 2024 Fall RC 6, Yutin Cao



# **THANK YOU!**

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