

# **Formal Verification and Synthesis**

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**Date: 12.05.24**

<https://github.com/BoazGur/SokobanVerficiation>

## Part 1:

1. The FDS is the group:  $D = \{V, \theta, \rho, J, C\}$

$V = \{board, x, y, turn, possible\_up, possible\_down, possible\_right, possible\_left\}$

When the variables are defined as:

board: array representation of the map,  $n \times m$  matrix (XSB format) **\*in the nuXmv it's defined as a set of  $n*m$  variables ( $v_{ij}$ ) which represent  $board[i][j]$ , the nuXmv didn't work for us with a 2D array, also in the nuXmv we translated the XSB format to words:**

**$\{@, +, \$, *, \#, ., -\} \rightarrow \{shtrudel, plus, dollar, star, solamit, dot, minus\}$**

x: int, x-position of the keeper on board  $s.t 0 \leq x < m$

y: int, y-position of the keeper on board  $s.t 0 \leq y < n$

possible\_u: boolean, true if the keeper can go up

possible\_d: boolean, true if the keeper can go down

possible\_r: boolean, true if the keeper can go right

possible\_l: boolean, true if the keeper can go left

turn: enum, representation of action taken,  $\{u, d, l, r, none\}$

**\*in the nuXmv we also defined 3 constants, n: # of rows, m: # of columns, done: boolean, true if there are no dollars (boxes).**

$\theta(\text{starting board}) = (turn = None) \wedge (board = input) \wedge (x = input.findcol(@ \vee +)) \wedge$   
 $\wedge (y = input.findrow(@ \vee +)) \wedge (possible\_u = up(x, y, board)) \wedge$   
 $\wedge (possible\_d = down(x, y, board)) \wedge (possible\_r = right(x, y, board)) \wedge$   
 $\wedge (possible\_l = left(x, y, board))$

Notice the board is given as an input to the nuXmv. The turn starts as None.

x and y are determined by the input where the keeper was found.

Let's define the functions up, down, right, and left. Which determine the behavior of possible\_u, possible\_d, possible\_r, and possible\_l respectively.

$possible\_u = !((y = 0) \vee ((y > 1) \wedge (input[y - 1][x] = \#)) \vee$   
 $\vee ((y > 1) \wedge (input[y - 1][x] \in \{\$, *\}) \wedge (input[y - 2][x] \in \{\$, *, \#\})))$

$possible\_d = !((y = n - 1) \vee ((y < n - 1) \wedge (input[y + 1][x] = \#)) \vee$   
 $\vee ((y < n - 2) \wedge (input[y + 1][x] \in \{\$, *\}) \wedge (input[y + 2][x] \in \{\$, *, \#\})))$

$possible\_l = !((x = 0) \vee ((x > 1) \wedge (input[y][x - 1] = \#)) \vee$   
 $\vee ((x > 1) \wedge (input[y][x - 2] \in \{\$, *\}) \wedge (input[y][x - 2] \in \{\$, *, \#\})))$

$possible\_r = !((x = m - 1) \vee ((x < m - 1) \wedge (input[y][x + 1] = \#)) \vee$   
 $\vee ((x < m - 2) \wedge (input[y][x + 1] \in \{\$, *\}) \wedge (input[y][x + 2] \in \{\$, *, \#\})))$

$\rho$  consist of the transition of all the variables so we will defined each one here:

$$\begin{aligned} possible\_u' &= !((y = 0) \vee ((y > 1) \wedge (input[y - 1][x] = \#)) \vee \\ &\vee ((y > 1) \wedge (input[y - 1][x] \in \{\$, *\}) \wedge (input[y - 2][x] \in \{\$, *, \#\}))) \end{aligned}$$

$$\begin{aligned} possible\_d' &= !((y = n - 1) \vee ((y < n - 1) \wedge (input[y + 1][x] = \#)) \vee \\ &\vee ((y < n - 2) \wedge (input[y + 1][x] \in \{\$, *\}) \wedge (input[y + 2][x] \in \{\$, *, \#\}))) \end{aligned}$$

$$\begin{aligned} possible\_l' &= !((x = 0) \vee ((x > 1) \wedge (input[y][x - 1] = \#)) \vee \\ &\vee ((x > 1) \wedge (input[y][x - 2] \in \{\$, *\}) \wedge (input[y][x - 2] \in \{\$, *, \#\}))) \end{aligned}$$

$$\begin{aligned} possible\_r' &= !((x = m - 1) \vee ((x < m - 1) \wedge (input[y][x + 1] = \#)) \vee \\ &\vee ((x < m - 2) \wedge (input[y][x + 1] \in \{\$, *\}) \wedge (input[y][x + 2] \in \{\$, *, \#\}))) \end{aligned}$$

$$\begin{aligned} \rho_{turn} &= ((done = true) \wedge (turn' = None)) \vee \\ &\vee ((possible\_u' = true) \wedge (possible\_d' = true) \wedge (possible\_r' = true) \wedge (possible\_l' = true) \wedge \\ &\vee (turn = \{none, u, d, r, l\})) \vee \\ &\vee ((possible\_u' = true) \wedge (possible\_d' = true) \wedge (possible\_l' = true) \wedge (turn' = \{none, u, d, l\})) \vee \\ &\vee ((possible\_u' = true) \wedge (possible\_d' = true) \wedge (possible\_r' = true) \wedge (turn' = \{none, u, d, r\})) \vee \\ &\vee ((possible\_u' = true) \wedge (possible\_r' = true) \wedge (possible\_l' = true) \wedge (turn' = \{none, u, r, l\})) \vee \\ &\vee ((possible\_d' = true) \wedge (possible\_r' = true) \wedge (possible\_l' = true) \wedge (turn' = \{none, d, r, l\})) \vee \\ &\vee ((possible\_d' = true) \wedge (possible\_r' = true) \wedge (turn' = \{none, d, r\})) \vee \\ &\vee ((possible\_d' = true) \wedge (possible\_l' = true) \wedge (turn' = \{none, d, l\})) \vee \\ &\vee ((possible\_u' = true) \wedge (possible\_r' = true) \wedge (turn' = \{none, u, r\})) \vee \\ &\vee ((possible\_u' = true) \wedge (possible\_l' = true) \wedge (turn' = \{none, u, l\})) \vee \\ &\vee ((possible\_d' = true) \wedge (possible\_u' = true) \wedge (turn' = \{none, d, u\})) \vee \\ &\vee ((possible\_l' = true) \wedge (possible\_r' = true) \wedge (turn' = \{none, l, r\})) \vee \\ &\vee ((possible\_u' = true) \wedge (turn' = \{none, u\})) \vee \\ &\vee ((possible\_d' = true) \wedge (turn' = \{none, d\})) \vee \\ &\vee ((possible\_r' = true) \wedge (turn' = \{none, r\})) \vee \\ &\vee ((possible\_l' = true) \wedge (turn' = \{none, l\})) \vee \\ &\vee ((possible\_u' = false) \wedge (possible\_d' = false) \wedge (possible\_l' = false) \wedge (turn' = none)) \end{aligned}$$

The idea of turn transition is that if done so turn is None, but if not done then we check cases:

If  $possible\_u' = true$  then  $u \in turn'$ , If  $possible\_d' = true$  then  $d \in turn'$

If  $possible\_r' = true$  then  $r \in turn'$ , If  $possible\_l' = true$  then  $l \in turn'$

And always  $None \in turn'$

$$\rho_x = ((turn' = r) \wedge (x < m - 1) \wedge (x' = x + 1)) \vee ((turn' = l) \wedge (x > 0) \wedge (x' = x - 1))$$

$$\rho_y = ((turn' = d) \wedge (y < n - 1) \wedge (y' = y + 1)) \vee ((turn' = u) \wedge (y > 0) \wedge (y' = y - 1))$$

$$\begin{aligned} \rho_{board[i][j]} = & ((y = i) \wedge (x = j) \wedge (board[i][j] = @) \wedge (turn' \neq None) \wedge (board[i][j]' = -)) \vee \\ & ((y = i) \wedge (x = j) \wedge (board[i][j] = +) \wedge (turn' \neq None) \wedge (board[i][j]' = .)) \vee \\ & \vee ((y = i) \wedge (x = j - 1 > -1) \wedge (board[i][j] \in \{-, \$\}) \wedge (turn' = r) \wedge (board[i][j]' = @)) \vee \\ & \vee ((y = i) \wedge (x = j - 1 > -1) \wedge (board[i][j] \in \{., *\}) \wedge (turn' = r) \wedge (board[i][j]' = +)) \vee \\ & \vee ((y = i) \wedge (x = j - 2 > -2) \wedge (board[i][j - 1] \in \{*, \$\}) \wedge (turn' = r) \wedge (board[i][j] = -) \wedge \\ & \wedge (board[i][j]' = \$)) \vee \\ & \vee ((y = i) \wedge (x = j - 2 > -2) \wedge (board[i][j - 1] \in \{*, \$\}) \wedge (turn' = r) \wedge (board[i][j] = .) \wedge \\ & \wedge (board[i][j]' = *)) \vee \\ & \vee ((y = i) \wedge (x = j + 1 < m) \wedge (board[i][j] \in \{-, \$\}) \wedge (turn' = l) \wedge (board[i][j]' = @)) \vee \\ & \vee ((y = i) \wedge (x = j + 1 < m) \wedge (board[i][j] \in \{., *\}) \wedge (turn' = l) \wedge (board[i][j]' = +)) \vee \\ & \vee ((y = i) \wedge (x = j + 2 > m) \wedge (board[i][j + 1] \in \{*, \$\}) \wedge (turn' = l) \wedge (board[i][j] = -) \wedge \\ & \wedge (board[i][j]' = \$)) \vee \\ & \vee ((y = i) \wedge (x = j + 2 > m) \wedge (board[i][j + 1] \in \{*, \$\}) \wedge (turn' = l) \wedge (board[i][j] = .) \wedge \\ & \wedge (board[i][j]' = *)) \vee \\ & \vee ((y = i - 1 > -1) \wedge (x = j) \wedge (board[i][j] \in \{-, \$\}) \wedge (turn' = d) \wedge (board[i][j]' = @)) \vee \\ & \vee ((y = i - 1 > -1) \wedge (x = j) \wedge (board[i][j] \in \{., *\}) \wedge (turn' = d) \wedge (board[i][j]' = +)) \vee \\ & \vee ((y = i - 2 > -2) \wedge (x = j) \wedge (board[i - 1][j] \in \{*, \$\}) \wedge (turn' = d) \wedge (board[i][j] = -) \wedge \\ & \wedge (board[i][j]' = \$)) \vee \\ & \vee ((y = i - 2 > -2) \wedge (x = j) \wedge (board[i - 1][j] \in \{*, \$\}) \wedge (turn' = d) \wedge (board[i][j] = .) \wedge \\ & \wedge (board[i][j]' = *)) \vee \\ & \vee ((y = i + 1 < n) \wedge (x = j) \wedge (board[i][j] \in \{-, \$\}) \wedge (turn' = u) \wedge (board[i][j]' = @)) \vee \\ & \vee ((y = i + 1 < n) \wedge (x = j) \wedge (board[i][j] \in \{., *\}) \wedge (turn' = u) \wedge (board[i][j]' = +)) \vee \\ & \vee ((y = i + 2 < n) \wedge (x = j) \wedge (board[i + 1][j] \in \{*, \$\}) \wedge (turn' = u) \wedge (board[i][j] = -) \wedge \\ & \wedge (board[i][j]' = \$)) \vee \\ & \vee ((y = i + 2 < n) \wedge (x = j) \wedge (board[i + 1][j] \in \{*, \$\}) \wedge (turn' = u) \wedge (board[i][j] = .) \wedge \\ & \wedge (board[i][j]' = *)) \end{aligned}$$

$J$  are state that need to repeat infinite amount of times, in our problem we want that ?

$C$  are pair of states that if one repeat infinite amount of times the other also, so in our problem we want that ?

### Part 1:

2. The LTLSPEC we defined for our problem is this:  $F(done)$ , which means that for a win eventually done will be true.

## Part 2:

1. The code and the nuXmv's and the output files can be found in this GitHub repo:  
<https://github.com/BoazGur/SokobanVerification>.
2. We converted all the board examples that was provided in the last page of the exercise to XSB format and run the python script on them.  
Most of them worked great with just the command "nuXmv <file name>".  
Just the last board (board7) took to long so we run it with BMC manually with the commands "nuXmv -int <file name>" and then "go\_bmc" and then "check\_ltlspec\_bmc -k 15"

Board1.out:

```
27 -- specification !( F done) is false
28 -- as demonstrated by the following execution sequence
29 Trace Description: LTL Counterexample
30 Trace Type: Counterexample
31 -> State: 1.1 <-
32   turn = none
33   possible_up = FALSE
34   possible_down = FALSE
35   possible_right = TRUE
36   possible_left = FALSE
37   y = 1
38   x = 1
39   v_00 = solamit
40   v_01 = solamit
41   v_02 = solamit
42   v_03 = solamit
43   v_04 = solamit
44   v_10 = solamit
45   v_11 = shtrudel
46   v_12 = dollar
47   v_13 = dot
48   v_14 = solamit
49   v_20 = solamit
50   v_21 = solamit
51   v_22 = solamit
52   v_23 = solamit
53   v_24 = solamit
54   done = FALSE
55   m = 5
56   n = 3
57 -> State: 1.2 <-
58   turn = r
59   x = 2
60   v_11 = minus
61   v_12 = shtrudel
62   v_13 = star
63   done = TRUE
64 -- Loop starts here
65 -> State: 1.3 <-
66   turn = none
67   possible_right = FALSE
68   possible_left = TRUE
69 -> State: 1.4 <-
70
```



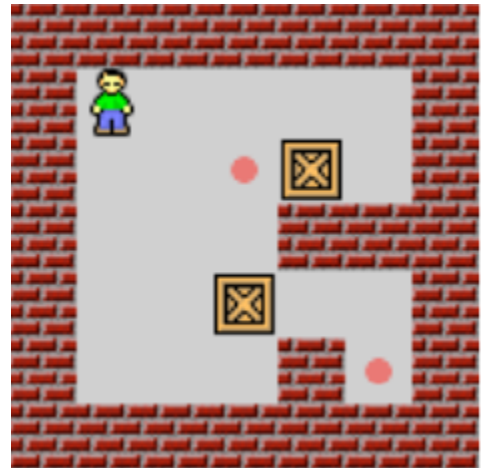
Board2.out:

```
27 -- specification !( F done) is true
28
```



Board3.out:

```
27 -- specification !( F done) is true
28
```



Board4.out:

```

27 -- specification !( F done) is false 80
28 -- as demonstrated by the following ex 81
29 Trace Description: LTL Counterexample 82
30 Trace Type: Counterexample 83
31 -> State: 1.1 <- 84
32   turn = none 85
33   possible_up = TRUE 86
34   possible_down = TRUE 87
35   possible_right = TRUE 88
36   possible_left = TRUE 89
37   y = 3 90
38   x = 3 91
39   v_00 = solamit 92
40   v_01 = solamit 93
41   v_02 = solamit 94
42   v_03 = solamit 95
43   v_04 = solamit 96
44   v_05 = solamit 97
45   v_06 = solamit 98
46   v_10 = solamit 99
47   v_11 = solamit 100
48   v_12 = solamit 101
49   v_13 = dot 102
50   v_14 = solamit 103
51   v_15 = solamit 104
52   v_16 = solamit 105
53   v_20 = solamit 106
54   v_21 = solamit 107
55   v_22 = solamit 108
56   v_23 = dollar 109
57   v_24 = solamit 110
58   v_25 = solamit 111
59   v_26 = solamit 112
60   v_30 = solamit 113
61   v_31 = dot 114
62   v_32 = dollar 115
63   v_33 = shtrudel 116
64   v_34 = dollar 117
65   v_35 = dot 118
66   v_36 = solamit 119
67   v_40 = solamit 120
68   v_41 = solamit 121
69   v_42 = solamit 122
70   v_43 = dollar 123
71   v_44 = solamit 124
72   v_45 = solamit 125
73   v_46 = solamit 126
74   v_50 = solamit 127
75   v_51 = solamit 128
76   v_52 = solamit 129
77   v_53 = dot
78   v_54 = solamit
79   v_55 = solamit

v_56 = solamit
v_60 = solamit
v_61 = solamit
v_62 = solamit
v_63 = solamit
v_64 = solamit
v_65 = solamit
v_66 = solamit
done = FALSE
m = 7
n = 7

-> State: 1.2 <-
  turn = d
  y = 4
  v_33 = minus
  v_43 = shtrudel
  v_53 = star

-> State: 1.3 <-
  turn = u
  possible_down = FALSE
  possible_right = FALSE
  possible_left = FALSE
  y = 3
  v_33 = shtrudel
  v_43 = minus

-> State: 1.4 <-
  possible_down = TRUE
  possible_right = TRUE
  possible_left = TRUE
  y = 2
  v_13 = star
  v_23 = shtrudel
  v_33 = minus

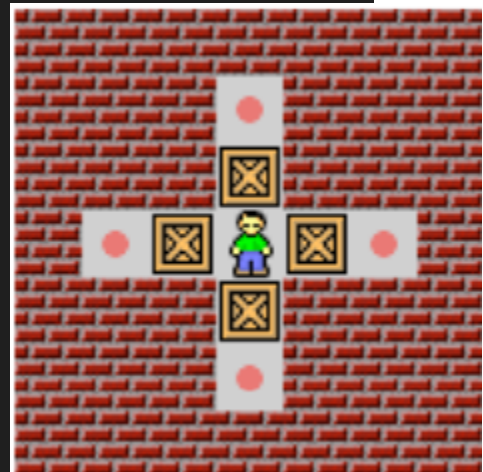
-> State: 1.5 <-
  turn = d
  possible_up = FALSE
  possible_right = FALSE
  possible_left = FALSE
  y = 3
  v_23 = minus
  v_33 = shtrudel

-> State: 1.6 <-
  turn = r
  possible_up = TRUE
  possible_right = TRUE
  possible_left = TRUE
  x = 4
  v_33 = minus
  v_34 = shtrudel
  v_35 = star

-> State: 1.7 <-
  turn = 1
  possible_up = FALSE
  possible_down = FALSE
  possible_right = FALSE
  x = 3
  v_33 = shtrudel
  v_34 = minus

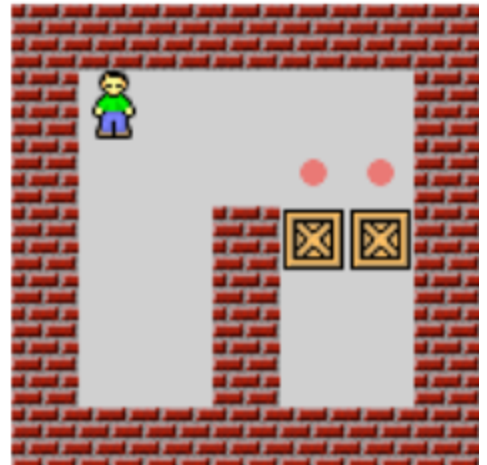
-> State: 1.8 <-
  possible_up = TRUE
  possible_down = TRUE
  possible_right = TRUE
  x = 2
  v_31 = star
  v_32 = shtrudel
  v_33 = minus
  done = TRUE
-- Loop starts here
-> State: 1.9 <-
  turn = none
  possible_up = FALSE
  possible_down = FALSE
  possible_left = FALSE
-> State: 1.10 <-

```



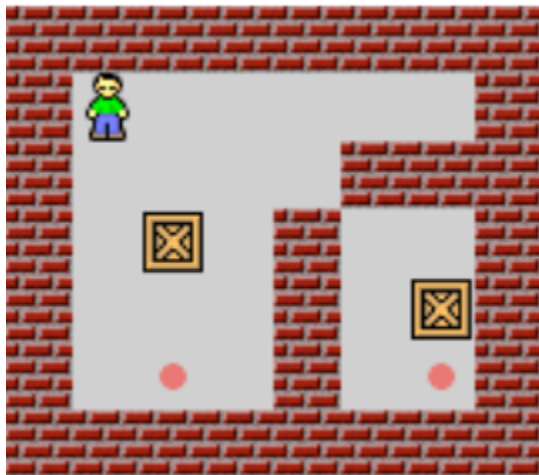
Board5.out:

```
27  -- specification !( F done)  is true
28
```



Board6.out:

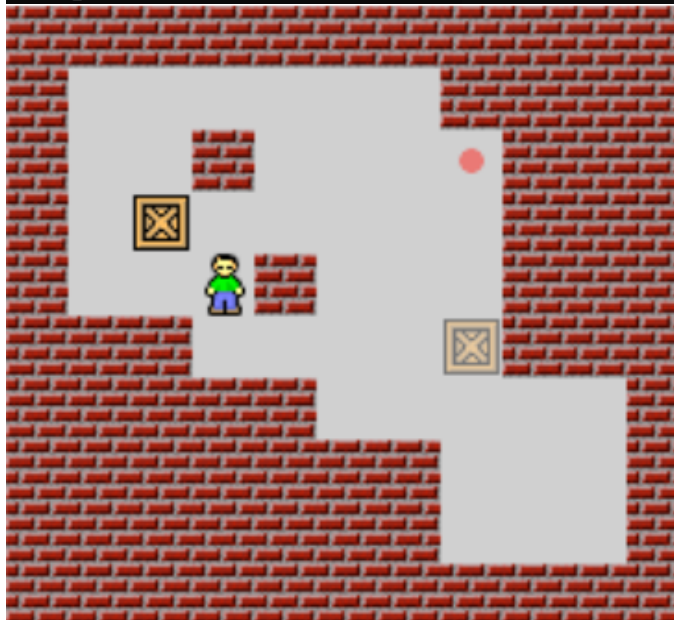
```
27  -- specification !( F done)  is true
28
```





Board7.out:

```
nuXmv > check_ltlspec_bmc -k 15
-- no counterexample found with bound 0
-- no counterexample found with bound 1
-- no counterexample found with bound 2
-- no counterexample found with bound 3
-- no counterexample found with bound 4
-- no counterexample found with bound 5
-- no counterexample found with bound 6
-- no counterexample found with bound 7
-- no counterexample found with bound 8
-- no counterexample found with bound 9
-- no counterexample found with bound 10
-- specification ! ( F done ) is false
-- as demonstrated by the following execu
Trace Description: BMC Counterexample
Trace Type: Counterexample
-> State: 1.1 <-
  turn = none
  possible_up = TRUE
  possible_down = TRUE
  possible_right = FALSE
  possible_left = TRUE
  y = 4
  x = 3
  v_00 = solamit
  v_01 = solamit
  v_02 = solamit
  v_03 = solamit
  v_04 = solamit
  v_05 = solamit
  v_06 = solamit
  v_07 = solamit
  v_08 = solamit
  v_09 = solamit
  v_10 = solamit
  v_11 = minus
  v_12 = minus
  v_13 = minus
  v_14 = minus
  v_15 = minus
  v_16 = minus
  v_17 = solamit
  v_18 = solamit
  v_19 = solamit
  v_110 = solamit
  v_20 = solamit
  v_21 = minus
  v_22 = minus
  v_23 = solamit
  v_24 = minus
  v_25 = minus
  v_26 = minus
  v_27 = dot
  v_28 = solamit
  v_29 = solamit
  v_210 = solamit
  v_30 = solamit
  v_31 = minus
  v_32 = dollar
  v_33 = minus
  v_34 = minus
  v_35 = minus
  v_36 = minus
  v_37 = minus
  v_38 = solamit
  v_39 = solamit
  v_310 = solamit
  v_40 = solamit
  v_41 = minus
  v_42 = minus
  v_43 = shtrudel
  v_44 = solamit
  v_45 = minus
  v_46 = minus
  v_47 = minus
  v_48 = solamit
  v_49 = solamit
  v_410 = solamit
  v_50 = solamit
  v_51 = solamit
  v_52 = solamit
  v_53 = minus
  v_54 = minus
  v_55 = minus
  v_56 = minus
  v_57 = star
  v_58 = solamit
  v_59 = solamit
  v_510 = solamit
  v_60 = solamit
  v_61 = solamit
  v_62 = solamit
  v_63 = solamit
  v_64 = solamit
  v_65 = minus
  v_66 = minus
  v_67 = minus
  v_68 = minus
  v_69 = minus
  v_610 = solamit
  v_70 = solamit
  v_71 = solamit
  v_72 = solamit
  v_73 = solamit
  v_74 = solamit
  v_75 = solamit
  v_76 = solamit
  v_77 = minus
  v_78 = minus
  v_79 = minus
  v_710 = solamit
  v_80 = solamit
  v_81 = solamit
  v_82 = solamit
  v_83 = solamit
  v_84 = solamit
  v_85 = solamit
  v_86 = solamit
  v_87 = minus
  v_88 = minus
  v_89 = minus
  v_810 = solamit
  v_90 = solamit
  v_91 = solamit
  v_92 = solamit
  v_93 = solamit
  v_94 = solamit
  v_95 = solamit
  v_96 = solamit
  v_97 = solamit
  v_98 = solamit
  v_99 = solamit
  v_910 = solamit
  done = FALSE
  m = 11
  n = 10
-> State: 1.2 <-
  turn = l
  x = 2
  v_42 = shtrudel
  v_43 = minus
-> State: 1.3 <-
  possible_down = FALSE
  possible_right = TRUE
  x = 1
  v_41 = shtrudel
  v_42 = minus
-> State: 1.4 <-
  turn = u
  possible_left = FALSE
  y = 3
  v_31 = shtrudel
  v_41 = minus
-> State: 1.5 <-
  turn = r
  possible_down = TRUE
  x = 2
  v_31 = minus
  v_32 = shtrudel
  v_33 = dollar
-> State: 1.6 <-
  possible_left = TRUE
  x = 3
  v_32 = minus
  v_33 = shtrudel
  v_34 = dollar
-> State: 1.7 <-
  possible_up = FALSE
  x = 4
  v_33 = minus
  v_34 = shtrudel
  v_35 = dollar
-> State: 1.8 <-
  possible_up = TRUE
  possible_down = FALSE
  x = 5
  v_34 = minus
  v_35 = shtrudel
  v_36 = dollar
-> State: 1.9 <-
  possible_down = TRUE
  x = 6
  v_35 = minus
  v_36 = shtrudel
  v_37 = dollar
-> State: 1.10 <-
  turn = d
  possible_right = FALSE
  y = 4
  v_36 = minus
  v_46 = shtrudel
-> State: 1.11 <-
  turn = r
  possible_right = TRUE
  x = 7
  v_46 = minus
  v_47 = shtrudel
-> State: 1.12 <-
  turn = u
  possible_right = FALSE
  y = 3
  v_27 = star
  v_37 = shtrudel
  v_47 = minus
  done = TRUE
nuXmv > |
```



## Part 2:

3. For each board we found was solvable we'll define the winning moves:

Board1: r

Board4: d, u, u, d, r, l, l

Board7: l, l, u, r, r, r, r, d, r, u

## Part 3:

| Board  | SAT[sec] | BDD[sec] |
|--------|----------|----------|
| board1 | 0.12     | 0.13     |
| board2 | 1.23     | 0.14     |
| board3 | 15.28    | 6.7      |
| board4 | 1.4      | 6.52     |
| board5 | 10.49    | 2.13     |
| board6 | 7.05     | 1.58     |
| board7 | 21.89    | 1758.48  |

When running the SVM's we used interactive mode and different commands for BDD and SAT:

BDD: commands = go -> check\_ltlspec -> quit

SAT: commands = go\_bmc -> check\_ltlspec\_bmc -k 15 -> quit

From those tests, we can understand that BDD solved faster for boards which isn't solvable probably because we forced the SAT to continue and stop after 15 moves. But we noticed that for solvable boards (1, 4, 7) the SAT solved them faster, and for board7 that is bigger than the others the SAT solved it much faster than the BDD.

To conclude, in our opinion the SAT is better than BDD, especially in solvable boards.

#### Part 4:

For this part, we added some new functionality to the SMVWriter class using the SMVWriterIterative class which inherits from SMVwriter. In this class, we also follow the position of one specific box in each iteration. For that we had modified 'done' to check if the chosen box had reached a target. At the end of each iteration we try to get our new board state. To do that, first of all, we check if our specification is true. If so, we know our board is unsolvable and we return None. otherwise, we inspect all the last changes of each place of the board (aka. the board state) and then return the board after the iteration.

For each iteration, we run the nuXmv in SAT mode, using these commands:

SAT: `commands = go_bmc -> check_Itlspec_bmc -k 15 -> quit`

For each board, we saved the total time that took the nuXmv to run, and these are the results:

| Board  | ITERATIVE_SAT[sec] | ITERATIONS |
|--------|--------------------|------------|
| board1 | 0.16               | 1          |
| board2 | 1.26               | 1          |
| board3 | 2.53               | 2          |
| board4 | 1.52               | 4          |
| board5 | 9.28               | 2          |
| board6 | 7.77               | 2          |
| board7 | 24.39              | 1          |

As for the times of the iterative algorithm, we got pretty similar results to the regular SAT mode. We can see a dramatic change in runtime in the board3 solution which is caused by the error we will explain in the next paragraph.

In some cases, two boxes can satisfy the specification although the board isn't solved. What's happening is that the new box pushed the first from the target and now the box that was on the target is not solved. This makes the program run another iteration as there is now 'another' box (which we solved in previous iterations). To solve that we found the number of boxes in the beginning and then we checked if our iteration number surpassed the number of boxes in the beginning. This solution doesn't really solve the problem, it just indicates that if our algorithm can get in a loop then it will stop it and define the board as unsolvable, which of course isn't always the true assumption.

Another problem we encountered when we tried to solve bigger, more complex boards, was the fact that when we solved for a specific box we could accidentally push another box to a corner or someplace it couldn't reach a target, to solve this problem we just avoided it:)

We created a new bigger solvable board, especially for this part which in XSB format looks like this:

```
#####  
#--$--.####  
##-#---.###  
#--$----###  
#--@#---###  
###----$###  
#####----#  
#####---#  
#####.---#  
#####
```

Which is like board7, but with more boxes to make it harder to solve. We checked the times in the SAT model, and our iterative\_SAT, and got these results:

Regular SAT: 175.75 sec, and solved in 23 moves (The full output file can be seen in the GitHub repo under outputSAT/board8.out).

Iterative\_SAT: 18.78 sec, and 3 iterations (The full output file can be seen in the GitHub repo under outputIterative/board8\_time.out,board8\_box\_iteration1-3.out).

As we can see, using our Iterative solution on big and complex boards yields way better results in time, as expected.