

1466-8858 Volume 10 Preprint 32 21 April 2007 CORROSION INHIBITION EFFICIENCY OF NONIONIC SCHIFF BASE

AMPHIPHILES OF p-AMINOBENZOIC ACID FOR ALUMINUM IN 4N-HCL

Nabel A. Negm* and Mohamed F. Zaki

Applied surfactant laboratory, Petrochemicals department

Egyptian Petroleum Research Institute (EPRI), Nasr city, Cairo, Egypt

ABSTRACT

A novel series of self-assembled nonionic Schiff base amphiphiles were synthesized and their chemical structures were confirmed using elemental analysis, FTIR spectroscopy and 1H-NMR spectra. The surface activities of these amphiphiles were determined based on the data of surface and interfacial tension, critical micelle concentration, effectiveness, efficiency, maximum surface excess and minimum surface area. Thermodynamics of adsorption and micellization processes of these amphiphiles in their solutions were also calculated. The surface and thermodynamic data showed their higher tendency towards adsorption at the interfaces. The synthesized amphiphiles were evaluated as corrosion inhibitors for aluminum (3SR) at different doses (400-10 ppm) in acidic medium (4N HCl) using weight loss and hydrogen evolution techniques. The corrosion measurements showed that the synthesized nonionic schiff bases could serve as effective corrosion inhibitors. The surface and corrosion inhibition activities were correlated to the chemical structures of the inhibitors

KEYWORDS

Nonionic surfactant, Schiff base, adsorption, surface tension, corrosion inhibition, corrosion rate, inhibition efficiency.

INTRODUCTION

Ferrous, nonferrous metals and their alloys are extensively used in industry. To remove unwanted scale and salt deposits or mill scales formed during manufacture, metals are immersed in acid solutions, which are known as an acid pickling bath. After the scale is removed, the metal may be subjected to attack by the acids. In order to reduce the degree of metal attack and rate of consumption of the acid, corrosion inhibitors are added to the pickling solutions. Hydrochloric and sulphuric acids are the most commonly used acids in the pickling bath ^(1, 2). Most commercial inhibitor formulations include aldehydes and amines in their structure ⁽³⁾. The choice of the inhibitors is based on two considerations: first, they could be synthesized conventionally from relatively cheap raw materials; secondly, they contain the electron clouds on the aromatic rings or, the electronegative atoms such as benzene ring containing Schiff bases ⁽⁶⁾. Schiff base inhibitors have been reported as effectively corrosion inhibitors for steel, copper and aluminum ⁽⁷⁻⁹⁾. These substances generally become effective by adsorption on the metal surface. Adsorption depends on the nature and charge of the metal



and also, on the chemical structures of the inhibitors. Self-assembled monolayer can provide a convenient method for corrosion inhibition, since the process of self-assembling is simple, and the chemical composition and thickness of self-assembled monolayers can be tailored by design and synthesis of the adsorption agent. The practical applications of self-assembled monolayers as corrosion inhibitors were explored by several investigators (11-14). It was found that densely packed self-assembled monolayers heteroatom containing compounds were effective for blocking certain electrochemical processes, thus effectively act as corrosion inhibitors. In this study, different self-assembled inhibitors containing polyethylene glycol chains with different molecular weights and schiff base terminal group were synthesized. The corrosion inhibition efficiencies of these compounds towards aluminum alloy were examined using weight loss and hydrogen evolution techniques. The surface activities of these schiff base amphiphiles and the surface activity-corrosion inhibition-chemical structure relationships were also discussed.

EXPERIMENTAL PROCEDURES

Synthesis of Schiff bases

0.5 mole of aldehydes (anisaldehyde and/or furfuraldehyde, respectively) was condensed with 0.5 mole of p-aminobenzoic acid in presence of 250 mL of ethyl alcohol as a solvent. The reaction mixture was refluxed for 6 hours and then left overnight until the product was precipitated. The product was washed by petroleum ether and recrystallized from ethanol. The final product was dried under vacuum at 40° C $^{(15)}$. The produced Schiff bases were denoted as ASB-p-ABA and FSB-p-ABA and their chemical structures were represented in *Scheme 1*.

$$CH_3O$$
— $C=N$ — $COOH$ ASB- p -ABA

Scheme 1. Chemical structures of the synthesized Schiff bases.

Synthesis of ASA-p-ABA polyethylene glycol palmitate

Polyethylene glycol monopalmitate of different molecular weights (400, 1000, 2000, 3000 and/or 6000) were esterified by the synthesized Schiff base ASA-p-ABA in equimolar ratio in xylene as a solvent and p-toluene sulfonic acid (0.01 wt%) as a dehydrating agent ⁽¹⁶⁾. The reaction was continued until complete removal of the water of the reaction. Vacuum distillation was performed to remove the unreacted materials and the solvent, *Scheme* 2.

n = 9, 14, 23 and 68 ethylene oxide units

Scheme 2. Chemical structure of the synthesized ASA-p-ABA polyethylene glycol palmitate

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ASA-p-ABA Schiff base (0.1 mole) was esterified with 0.1 mole of polyethylene glycol-2000-monoalkanoic acid namely: decanoate, dodecanoate, tetradecanoate, hexadecanoate, octadecanoate and oleate in presence of xylene as a solvent and p-toluene sulfonic acid as dehydrating agent. The reaction mixture was completed by removal 1.8 mL of water. Then the reaction mixture was distilled under vacuum to complete removal of the unreacted materials and solvent, *Scheme 3*.

R = decanoate, palmitate, stearate and oleate moieties

$Scheme \ 3. \ Chemical \ structure \ of \ the \ synthesized \ ASA-p-ABA \ polyethylene \ glycol-2000-alkanoate \\ Structural \ analysis$

The elemental analyses were performed for the synthesized surfactants using Vario Elementar instrument for elemental analysis, Fourier-transfer infrared spectrophotometer for FTIR spectra and Bruker model DRX-300 NMR spectrometer with TMS as an internal standard for ¹H-NMR spectra. The results were represented in *Table 1*.

Surface and interfacial tension measurements

Surface tension measurements were made for freshly prepared inhibitors solutions in a concentration range of 0.1 to 0.0001 M/L at 25°C using a Du-Nuoy Tensiometer-Kruss-K100. Also, interfacial tension measurements were made for inhibitors-oil systems ⁽¹⁷⁾.

Weight loss determination

Aluminum coupons of 10cm^2 were used for weight loss measurement. Different concentrations of the inhibitors (400-10 ppm) in 4N HCl solution were used at 25° C. Coupons were placed in the corrodent-inhibitor systems and removed at 1 hour interval for 4 hours. The tested specimens were washed with distilled water and ethanol then dried and weighted. The difference in the weight was taken as the weight loss in mg. The percentage inhibitor efficiency was calculated as $^{(18)}$:

% Efficiency =
$$\frac{W_b - W}{W_b} X100$$

where W_b and W are the weight loss of aluminum specimens without and with inhibitors, respectively.

The corrosion rates were calculated according to the following formula:

$$Cr (mpy) = (KW)/(ATD)$$

where; K = constant, A = area, T = time, W = weight loss in mg and <math>D = density.

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Hydrogen gas evolution technique

In the gas evolution measurement, the corrosion rates of aluminum were investigated by the hydrogen evolution rate with the inhibitors concentrations of 400, 200, 100, 50, 25 and 10 ppm and 4N HCl solution without inhibitors. The hydrogen evolved is a function of the corrosion reaction and it displaced the fluid in the gasometeric setup, which is read directly. Experiments performed without inhibitors recorded the highest volume of hydrogen gas evolved ⁽¹⁹⁾. The percentage efficiency was calculated as:

% Efficiency =
$$\frac{V_b - V}{V_b} X 100$$

where V_b and V are the volumes of hydrogen evolved without and with inhibitors respectively.

RESULTS AND DISCUSSION

The Surface Activity

Effect of hydrophobic chain length

Figure 1 represents the relation between the surface tension and *-log* concentration of the synthesized nonionic Schiff base amphiphiles containing similar polyethylene glycol content (n = 46 EO units) at 25°C. It is clear that the surface tension profile has the characteristics of the nonionic surfactants. That appeared in the relatively higher surface tension values. Also, it could be observed that increasing the number of methylene groups along the hydrophobic chains from 10 to 18 units decreases the critical micelle concentrations gradually ⁽¹⁷⁾. That effect was explained in a previous work ⁽²⁰⁻²¹⁾ due to the repulsion occurred between the hydrophobic chains (nonpolar phase) and the water phase (polar phase), which forced the molecules to adsorb at the air-water interface and to micellize in the bulk of their solutions in order to decrease that repulsion. While, the lowest CMC values was observed for SBG-2000-oleate at 0.0009 M/L at 25°C, which referred to the above reasons and also to the unsaturation in oleate chain which increase the repulsion extent.

The effectiveness (π_{cmc}) values showed gradual decrease by increasing the hydrophobic chain length indicating the increasing of accumulated surfactant molecules at the interface. The maximum accumulation was indicated by the lowest surface tension depression at the critical micelle concentration and was recorded for SBG-2000-oleate molecules at 44 mN/m. The effectiveness values as well as the maximum surface excess considered as a clear description for the accumulation extent of amphiphiles molecules at the air-water interface.

The calculated values of the maximum surface excess showed increasing trend from SBG-2000-decanoate to SBG-2000-oleate as represented from the slope of pre-CMC region of surface tension profile (*Figure 1*). The maximum surface excess values were increased from



N 1466-8858 Volume 10 Preprint 32 21 April 2007 decanoate to oleate derivatives indicating higher surface concentration and increasing number of surfactant molecules at the interface.

Values of the minimum surface area occupied by the nonionic Schiff base amphiphiles at the interface (A_{min}) were calculated according to the equation:

$$A_{\min} = 10^{16} / (N_{AV} \cdot \Gamma_{\max})$$

where, Γ_{max} and N_{AV} are the maximum surface excess and Avogadro's number, respectively. Increasing the maximum surface excess values indicates the increasing of adsorbed molecules at the interface, hence the area available for each molecule will decrease. That causes the compacting of surfactant molecules at the interface to form denser layer. The values of critical micelle concentration, effectiveness, maximum surface excess and minimum surface area of the Schiff base nonionic amphiphiles were listed in *Table* (2).

Effect of polyethylene oxide content

Figure 2 represents the effect of ethylene oxide content on the surface activity of the synthesized nonionic schiff base amphiphiles. It is clear that increasing the number of ethylene oxide units within the nonionic moiety increases the hydrophilic characters of these molecules, which increases their critical micelle concentrations and also their surface tension values. The increasing of CMC values can be referred to the formation of hydrogen bonds (HBs) between amphiphiles-water molecules. HBs increase the adsorption of these amphiphiles at the air-water interface, which increases the CMC values gradually. On the other hand, the effectiveness (π_{CMC}) values of the synthesized Schiff base nonionic amphiphiles. SBG-n-16 were increased gradually by increasing the length (n) of the nonionic moiety (where n = 9, 14, 23 and 68) $^{(22-23)}$. The effectiveness (π_{CMC}) and the efficiency (pC₂₀) values were showed an increasing trend by increasing the hydrophobic chain length. The maximum lowering in the surface tension values was corresponded to the SBG-2000-oleate.

The maximum surface excess (Γ_{max}) values indicate lower surface concentration for lower ethylene oxide containing amphiphiles. On contrarily, the minimum surface area (A_{min}) values increased by increasing the nonionic chain lengths, (Table 2).

Thermodynamics of Adsorption and Micellization

The micellization and adsorption processes of the amphiphile molecules are occurred instantly. But, in common, one process may be predominating than the other one. The predominance of any of the two processes is governed by the thermodynamic variables of this process. In the investigated amphiphiles, both adsorption and micellization thermodynamic functions were calculated based on the methodology of Rosen, et al (24) and using the surface activity data in Table (2). The free energy changes of micellization and adsorption showed



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negative sign indicating the spontaneously of the two processes at 25° C. Also, ΔG_{mic} decreased gradually by increasing the hydrophobic chain lengths. But, ΔG_{ads} has slight increase in negativity than ΔG_{mic} . The maximum depression in ΔG_{mic} and ΔG_{ads} was observed at -12.04 and 12.11 Kj/Mole for SBG-2000-oleate, respectively. That showed the higher tendency of these amphiphiles towards adsorption rather than micellization. The tendency towards adsorption is refereed to the interaction between the aqueous phase and the hydrophobic chains which pumps the amphiphile molecules to the interface. The presence of these amphiphiles at the interface decreases the different in phases interactions.

Corrosion Inhibition Efficiency

Effect of alkyl chain length

Figure 3 represents the variation of corrosion inhibition efficiency of the synthesized nonionic schiff bases amphiphiles containing constant ethylene oxide content (n = 45 EO units). It is clear that the inhibition efficiency increased by increasing the number of repeated methylene groups in the hydrophobic chains. Schiff base polyethylene glycol ABA-2000 showed the maximum corrosion inhibition efficiency at 55.28%. Comparison between the corrosion rate of the different hydrophobic chains (Figure 3) showed the following trend: oleate > stearate > palmitate > decanoate. That behavior could be referred for two factors. First, the surface activity of these inhibitors at the interfaces. Second, the longer hydrophobic chains neighbored to each other can easily overlapped. That forms a condensed nonpolar layer faced the polar aggressive medium. Hence, good isolation occurred and the corrosion process stopped. The presence of coiling in these chains or unsaturation sites enhances their overlapping. That effect appears obviously in case of stearate and oleate derivatives. Increasing the adsorption tendency is directing them towards the metal/corrosive medium interface where the inhibitor molecules act as a barrier; hence corrosion process steadily decreased (25). Table (2) also showed that Amin values of the inhibitor molecules at the interface increased by increasing the number of methylene groups in their chains. That enforcing the molecular visualize to act as a blanket aligned with the aggressive medium and fade away its destructive action as shown in case of SBG-2000-oleate, $(A_{min} = 110.01 \text{ A}^2)$. Since, the hydrogen evolution and weight loss techniques were used to assure the accuracy and the reproducibility of the results. Hence, Figures (3, 4) showed that the inhibition efficiency of the two techniques are highly comparable having very close values. The invariability confirms the accuracy of the inhibitors efficiency values.

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Figure (5) represents the variation of corrosion inhibition efficiencies of nonionic schiff base derivatives bearing different ethylene oxide contents (400, 1000, 2000 and 3000) at constant hydrophobic chain (palmitate). The corrosion inhibition efficiency was increasingly varied by decreasing the PEO content. Higher PEO content increases the hydrophilicity of these compounds. Hence, molecules tend to locate in the aqueous medium, which decreases their adsorption tendency at the interfaces. Consequently, their accumulation at the metal surface decreased. That explains their low efficiency as corrosion inhibitors. On contrarily, lower PEO containing derivatives had higher surface activity due to their high hydrophobicity. That directs these molecules towards accumulation at the interfaces. Hence, their corrosion inhibition efficiencies increased (18).

Effect of inhibitor doses

Figure (6) represents the effect of the synthesized corrosion inhibitor doses on their corrosion inhibition efficiency for aluminum alloy in acidic medium at 25°C. It is clear that, at higher doses (400 ppm), η appears in the lowest values. Decreasing the doses to 200 ppm and 100 ppm increases the inhibition efficiencies to higher extent, till reaches the maximum around 100 ppm. Meanwhile, further decrease in the inhibitor concentrations (50, 25 and 10 ppm) turns the efficiencies to lower values, but remains higher than those belonged to 400 ppm. That behavior could be rationalized to the micellization and micelle formation of these inhibitors (amphiphiles). At lower inhibitor doses (10, 25 and 50 ppm), the molecules are pumped to the interfaces and participated in the formation of isolating layer at the metal surface, hence the corrosion efficiency increased. The 150 ppm dose is considered a critical dose, that is due to the metal surface is completely covered by inhibitor molecules, which appears the highest corrosion inhibition efficiency. That is due to micelle formation neat that concentration. The lowering in corrosion inhibition efficiencies upon increasing the inhibitor concentrations implements the idea that the inhibition occurred through a molecular mechanism and not the micellar one.

Corrosion inhibition mechanism

The mechanism of inhibition processes of the corrosion inhibitors is mainly the adsorption one. The process of adsorption is governed by different parameters depend almost on the chemical structure of the inhibitors. The adsorption process is occurred either physically or chemically. Figure (6) indicates that the inhibition efficiency increased by increasing the doses of the used inhibitors until the maximum η values at 100 ppm. Then, the efficiency decreased gradually by increasing the inhibitor concentration. That indicates the formation of



ISSN 1466-8858 Volume 10 Preprint 32 21 April 2007 adsorbed layer of inhibitors at lower concentrations, which increased by increasing the dose to

100 ppm. The decrease in η at higher doses indicates that the adsorption is not in successive layers due to the formation of the micelles at higher concentrations ⁽¹⁹⁾. That conclusion can be interpreted from *Figure (7)*, which indicates the formation of only one S-shape proves the formation of one layer of the inhibitor molecules at the metal surface.

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Table 1: Elemental analysis of the synthesized Schiff bases nonionic surfactants

Compound	Mol.	Carbon		Hydrogen		Nitrogen	
Compound	Wt.	Calc.	Found	Calc.	Found	Calc.	Found
Parent Schiff	255.27	70.58	70.31	5.13	5.02	5.49	5.24
base							
SBG-400-16	874.13	67.32	67.12	9.11	9.02	1.6	1.52
SBG-1000-16	1490.86	62.03	61.84	9.13	9.04	0.94	0.91
SBG-2000-16	2476.00	58.69	58.51	9.08	8.99	0.57	0.54
SBG-3000-16	2783.65	52.21	52.04	6.48	6.42	0.50	0.46
SBG-2000-10	2391.85	57.74	57.57	8.89	8.80	0.59	0.57
SBG-2000-18	2504.06	58.99	58.81	9.14	9.05	0.56	0.53
SBG-2000-Oleate	2502.04	58.04	58.86	9.02	8.93	0.56	0.51

All of the above compounds show satisfactory IR spectra: 850-890 cm⁻¹ (benzene ring), 1200 cm⁻¹ (ether linkage), 1340 cm⁻¹ (C=N), 1718 cm⁻¹ (C=O ester group), 2833 cm⁻¹ (CH₂) and, 2942 cm⁻¹ (CH₃). Also, ¹H-NMR spectra: 0.9 ppm (S, 6H, CH₃); 1.3 ppm (m, nH, CH₂) (where n=16H decanoate, 28H hexadecanoate, 32H octadecanoate) and 3.6 ppm (t, nH, OCH₂) (where n=36H PEG-400, 96H PEG-1000, 196H PEG-2000 and 292H PEG-3000).

Table 2: Surface Parameters of the synthesized Schiff base amphiphiles

Compound	CMC	$\pi_{ m cmc}$	Pc ₂₀	Γ_{max} X $10^{\text{-}10}$	A _{min} , A ²	ΔG _{mic}	ΔG_{ads}
SBG-2000-10	0.00173	23.0	3.00	2.03	81.83	-8.72	-8.83
SBG-2000-16	0.00124	24.0	3.25	1.85	89.79	-9.20	-9.28
SBG-2000-18	0.000167	26.0	3.49	1.78	93.32	-11.95	-12.02
SBG-2000-oleate	0.000156	28.5	3.74	1.51	110.01	-12.04	-12.11

 $\Gamma_{\text{max}} = (-d\gamma/d\log C) / (8.3 \times 10^7 \times RT)$

 $\Delta G_{mic} = [2.303RTlog(CMC)] - [log(55.5)]$

 ΔG_{ads} = $\Delta G_{mic} - (0.6023~\textrm{X}~10^{\text{-2}}~\textrm{X}~\textrm{pi}~\textrm{cmc}~\textrm{X}~\textrm{Amin})$

















