

Teaching F#

From numerical expressions to 3D graphics

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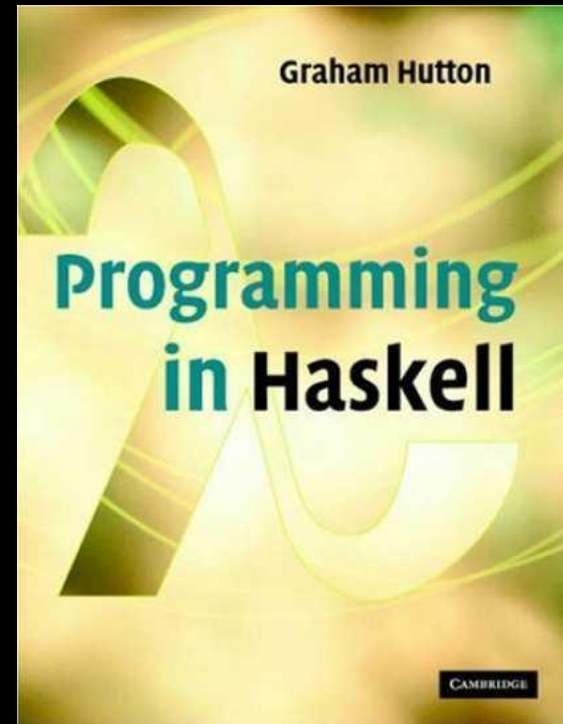
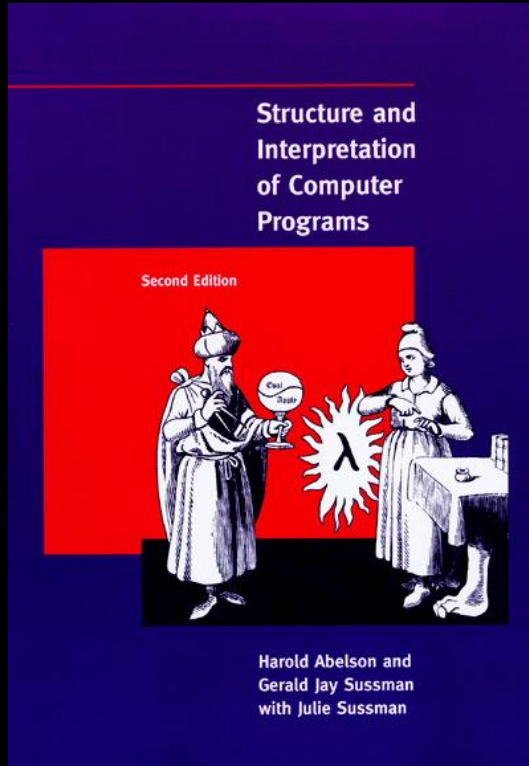
F# enthusiast and F# book author

PhD student at University of Cambridge

Target audience

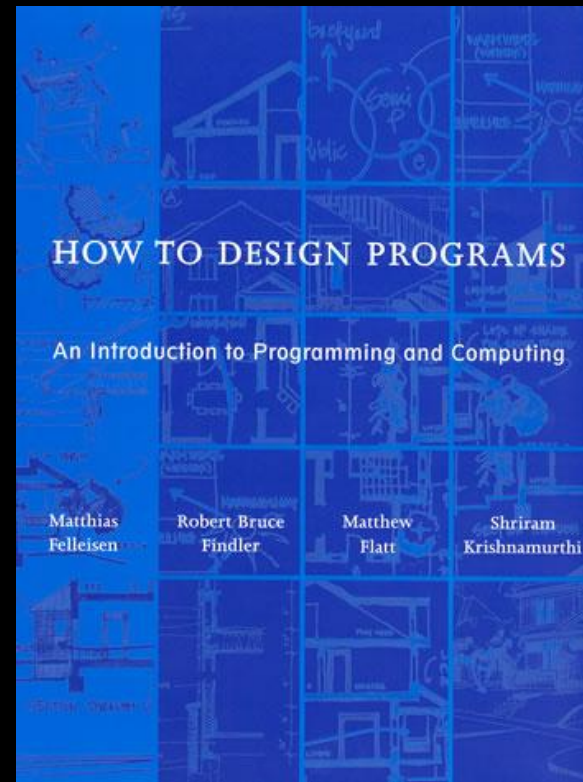
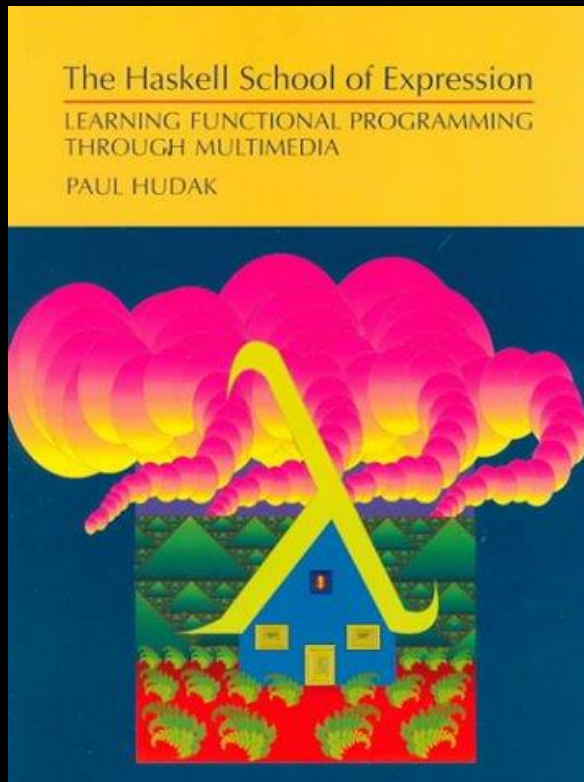
- Freshman students
 - Basic knowledge of **math** principles
(Not too much – they may not like it)
 - Earlier in **high-school** or later at **university** should be fine too
- Possibly first programming course
 - **Controversial** topic, but F# has many benefits

Related functional textbooks #1



- Emphasize theory and abstract thinking

Related functional textbooks #2



- Functional programming with fun demos

Why F# as a first language?

- Mathematically oriented language
 - Supplements **math and theory** courses
 - **Eliminates differences** between students
- Open-source with cross-platform support
 - **F# for MonoDevelop** on Linux/Mac
- Practical language with some market
 - .NET/Mono skills are valued by industry
 - Very easy **transition to C#** and other languages

First functional programming steps

Expressions in F#

What F# shares with math?

- **Language is exact** – we need to precisely say what we want to get
- **Composition does not break things** – we can mix various correct facts
- **Things do not change** – theorems will always be true, π will not change

Pythagorean theorem

- Math has equations and expressions

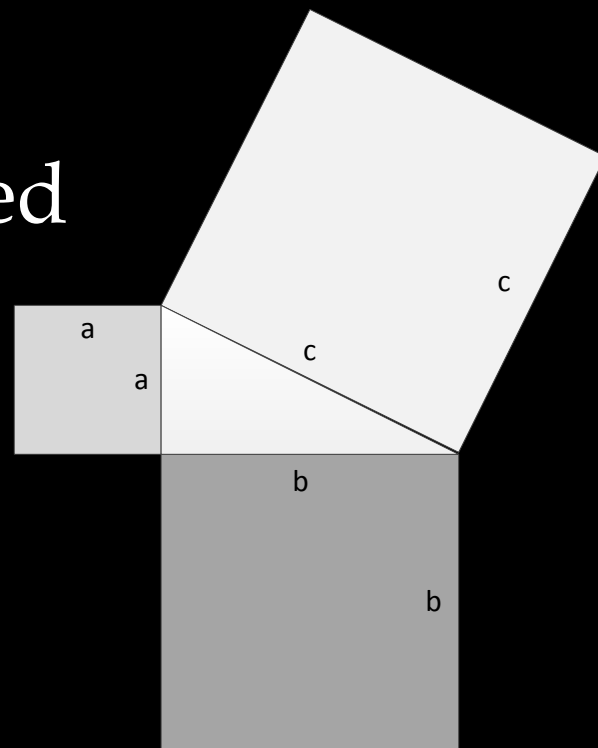
$$c^2 = a^2 + b^2 \qquad \sqrt{a^2 + b^2}$$

- Expressions can be evaluated

$$\sqrt{3^2 + 4^2} = \sqrt{9 + 16} = \sqrt{25} = 5$$

- Using F# Interactive

```
> sqrt((pown 3.0 2) + (pown 4.0 2));;  
val it : float = 5.0
```



Introducing let declarations and if

■ Solving quadratic equations

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad \frac{-b \pm \sqrt{D}}{2a} \quad \text{where } D = b^2 - 4ac$$

■ Script for solving written in F#

```
let d = pown b 2 - 4.0 * a * c;;

if d < 0.0 then "No real solution"
elif d > 0.0 then "Two solutions"
else "One solution";;

let x1 = (-b + sqrt d) / 2.0 * a
let x2 = (-b - sqrt d) / 2.0 * a;;
```

Working with F# expressions

DEMO

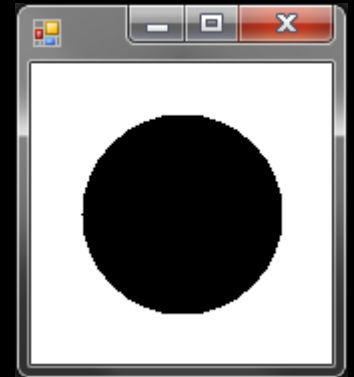
Fun examples for students to play with
Composing graphics in F#

Composing graphics

- Expressions that have *drawing* as the result
 - Same concepts as mathematical expressions

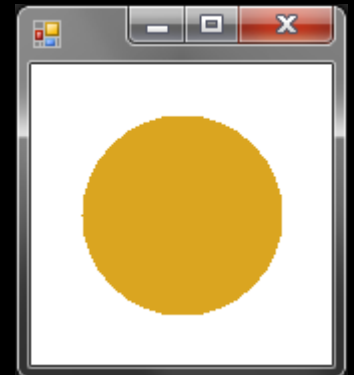
- Basic shapes

```
> Fun.circle 100.0f;;  
val it : Drawing = (Drawing 100x100)
```



- Functions for creating new shapes

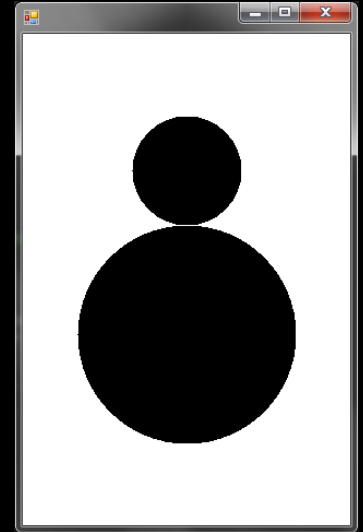
```
> Fun.fillColor Color.Goldenrod  
  (Fun.circle 100.0f);;  
val it : Drawing = (Drawing 100x100)
```



Working with shapes

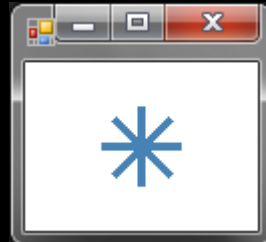
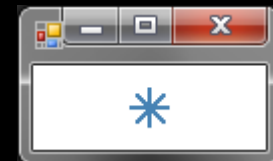
- Composing drawings using custom operator (\$)

```
Fun.circle 200.0f $  
  Fun.move 0.0f 150.0f (Fun.circle 100.0f)
```



- Let declarations to reuse drawings

```
let plus =  
  Fun.lineStyle 2.0f Color.SteelBlue  
    ( Fun.line -10.0f 0.0f 10.0f 0.0f $  
      Fun.line 0.0f -10.0f 0.0f 10.0f )  
  
let star = plus $ (Fun.rotate 45.0f plus)  
let bigStar = Fun.scale 2.0f 2.0f star
```



Creating drawings using F# expressions

DEMO

Difficult concepts explained using graphics

Introducing recursion and 3D

Explaining recursion

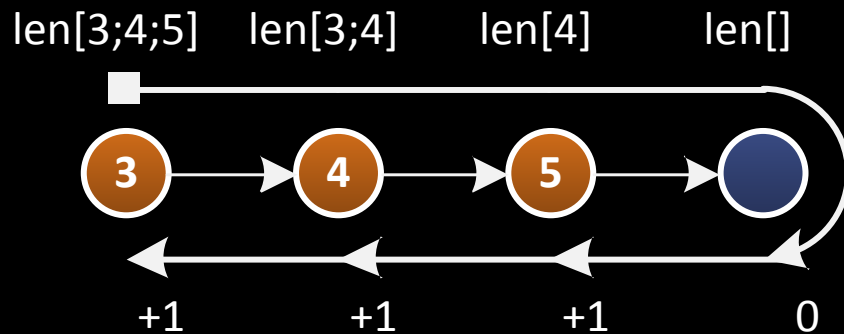
- Recursion is tricky concept
- Two types of recursions (from HTDP)
 - **Structural** – follows recursive data structure
For example lists, trees, expressions etc.
Such functions must terminate in F#
 - **General** – arbitrary recursive calls
May not terminate (if it is not well written)
For example generating fractals

General recursion for lists

■ Not tail-recursive list length

```
let rec length list =  
  match list with  
  | [] -> 0  
  | head::tail -> (length tail) + 1
```

■ Easy visualization of execution



■ Not tail-recursive – work done on the “way back”

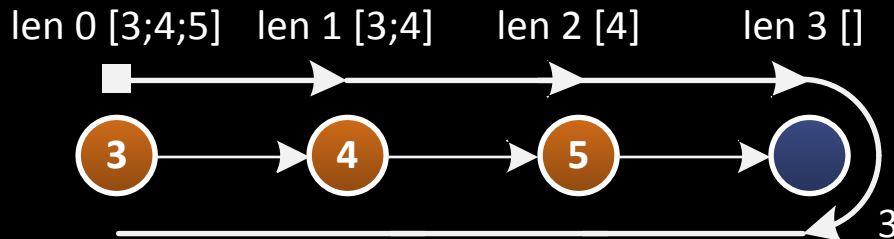
General recursion for lists

■ Tail-recursive list length

```
let rec length acc list =  
  match list with  
  | head::tail ->  
    let newacc = acc + 1 in length newacc tail  
  | [] -> acc;;
```

■ All work done on the way “forward”

■ This is what *tail-recursive* means!



Generating drawings from lists

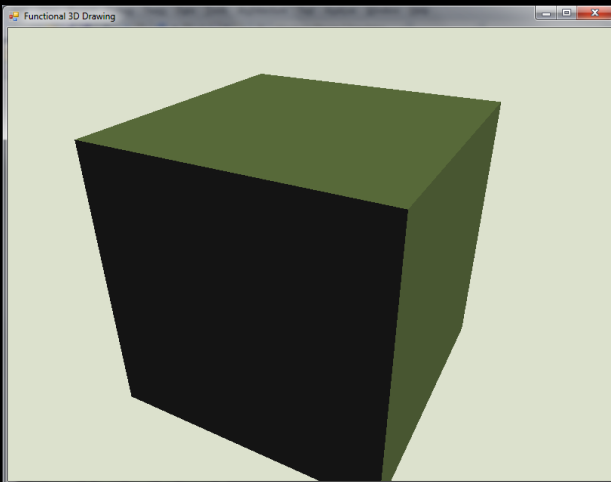
DEMO

Adding new dimension to drawings

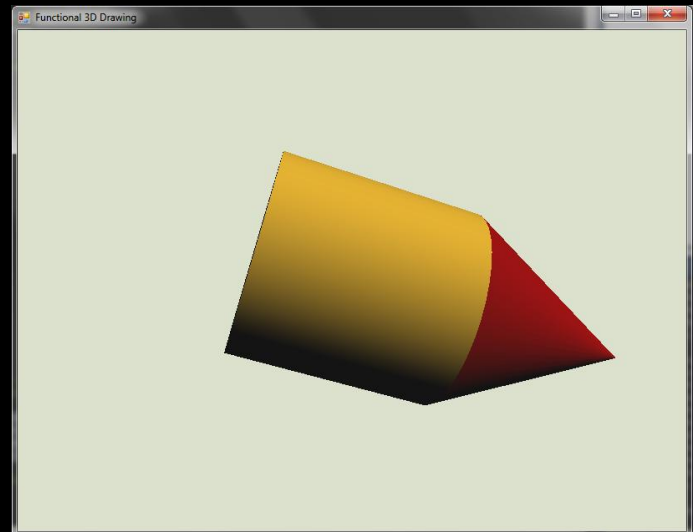
- Expressions that define **3D objects**

- Just like math
and 2D graphics

```
> Fun.cube;;  
val it : Drawing3D = (...)
```



```
Fun.color Color.DarkRed Fun.cone $  
( Fun.color Color.Goldenrod  
  (Fun.translate (0.0, 0.0, 1.0)  
    Fun.cylinder) );;  
val it : Drawing3D = (...)
```



Introducing general recursion using 3D objects

DEMO

Links and Q & A

■ Functional variations Web Site

Cross-platform F# support
Teaching materials for F#, etc...

■ <http://functional-variations.net>

■ If you're interested in more, get in touch!

■ <http://tomasp.net> | tomas@tomasp.net

■ <http://twitter.com/tomaspetricek>