

# CSE2301

# Digital Logic Design

Department of Computer Science and Engineering  
University of Connecticut

CSE2301: Digital Logic Design

**Why is this course  
important?**



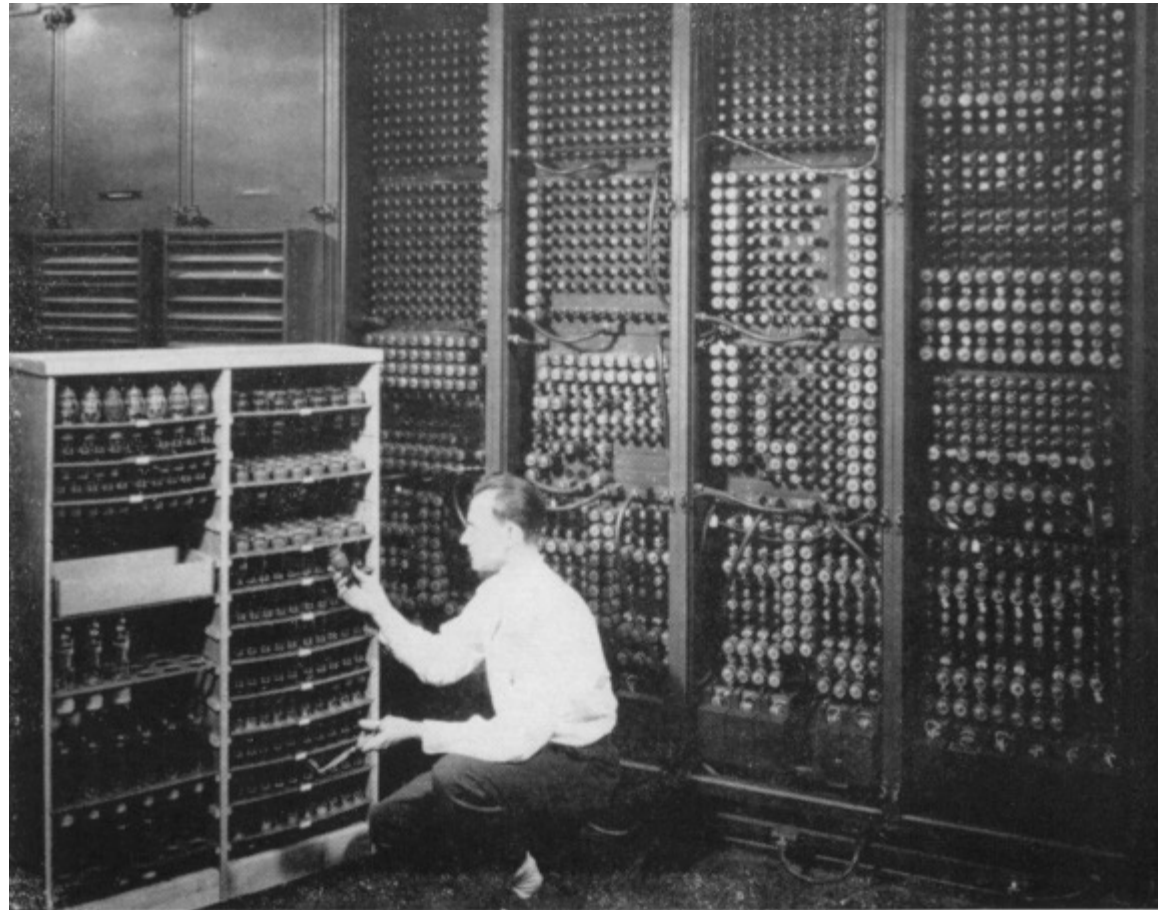
If you want to ....

- Design processor/motherboard/ Nintendo Wii
  - Write operating system, device drivers
  - Write software for embedded systems
- Understand how software interacts with hardware
  - Do hardware security
  - .....

**This class is really important for you!**



# Digital   Logic   Design



Replacing a bad tube meant checking among ENIAC's 19,000 possibilities.

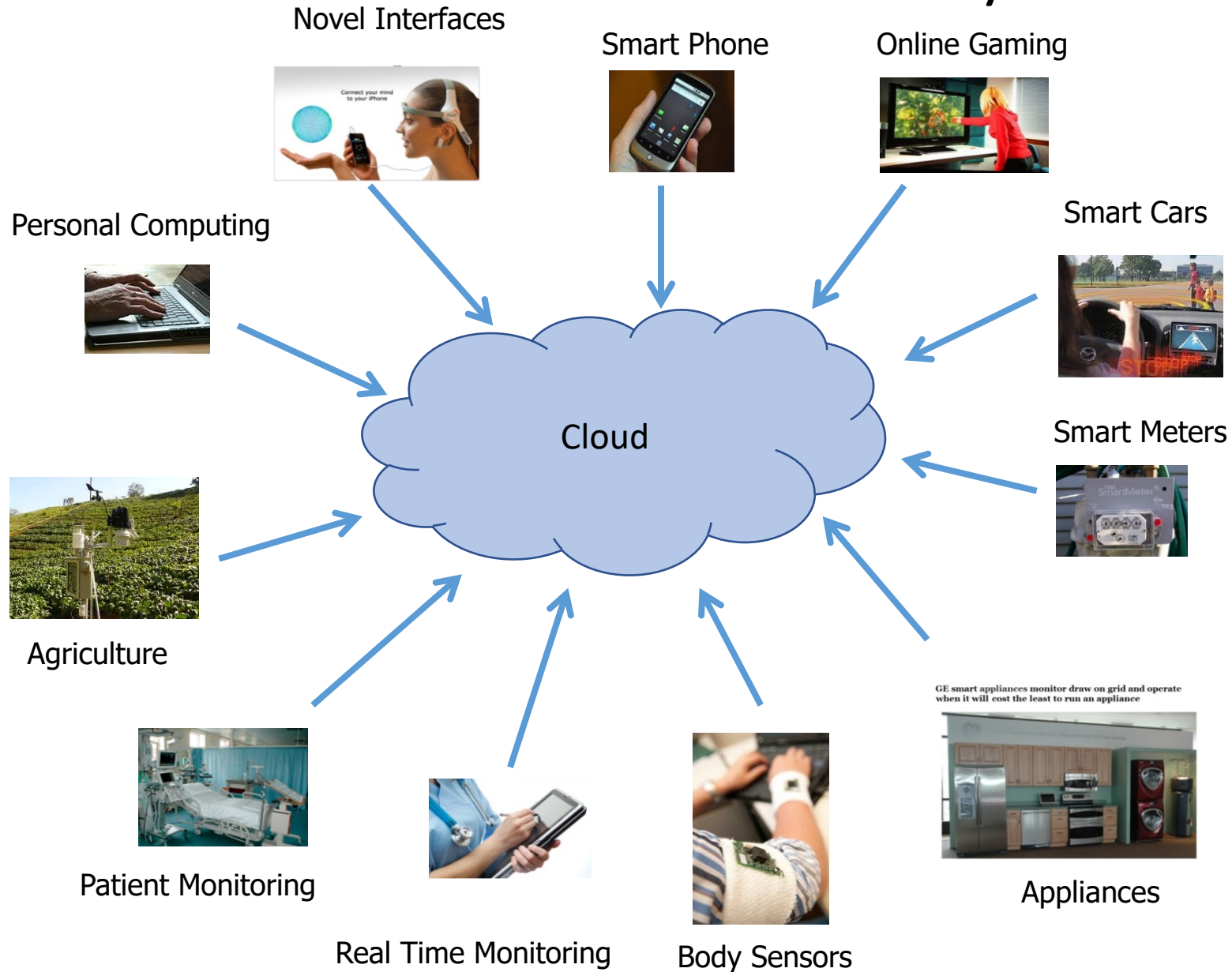
Source:

<http://www.computersciencelab.com/ComputerHistory/HistoryPt4.htm>



John Bardeen, William Shockley and Walter Brattain at  
Bell Labs, 1948.

# Miniaturization was the key .....



# Now, what are the main ideas?

- In our everyday world, we have many symbols
  - A,B,C,....0,1,2,3,.....\$,@,.....
- In digital world, there are only two symbols in our system
  - 0 and 1 (Welcome to the Binary system!)
  - You can only communicate using these two symbols!
  - You can use multiple of these symbols!



# Now, wait a second ....

- How do you represent 0 or 1? There is no such thing in physical world!

# Now, wait a second ....

- How do you represent 0 or 1? There is no such thing in physical world!
- You are right! These are just two numbers!
- In physical world, voltage and current are real!
- In digital world, we use 5V to represent 1 and 0v to represent 0 (Different voltage level may be used as well!)

# American Standard Code for Information

Table 1.7

American Standard Code for Information Interchange (ASCII)

(II)

$b_4b_3b_2b_1$	$b_7b_6b_5$							
	000	001	010	011	100	101	110	111
0000	NUL	DLE	SP	0	@	P	`	p
0001	SOH	DC1	!	1	A	Q	a	q
0010	STX	DC2	“	2	B	R	b	r
0011	ETX	DC3	#	3	C	S	c	s
0100	EOT	DC4	\$	4	D	T	d	t
0101	ENQ	NAK	%	5	E	U	e	u
0110	ACK	SYN	&	6	F	V	f	v
0111	BEL	ETB	‘	7	G	W	g	w
1000	BS	CAN	(	8	H	X	h	x
1001	HT	EM	)	9	I	Y	i	y
1010	LF	SUB	*	:	J	Z	j	z
1011	VT	ESC	+	;	K	[	k	{
1100	FF	FS	,	<	L	\	l	
1101	CR	GS	—	=	M	]	m	}
1110	SO	RS	.	>	N	^	n	~
1111	SI	US	/	?	O	—	o	DEL

# Some Example Problems

- Design a circuit with the following specification-
  - Takes two one-bit input from two users
  - (a) If either of the input is 1, output 1
  - (b) If both input are 1, output 1
  - (c) If both input are same, output 1

# Some Example Problems

- Assume that you are designing a circuit that beeps if any of the door in your car is not properly locked. Assume that each door is equipped with a sensor that outputs 1 if the door is not properly locked. You have 4 doors in your car.

- It is all about playing with voltage and switches!
- We just need to come up with the logic behind this switching.

Hence, the term “Digital Logic” Design

# Some Example Problems

- Design a digital clock.
- How is this problem different than the first two examples?

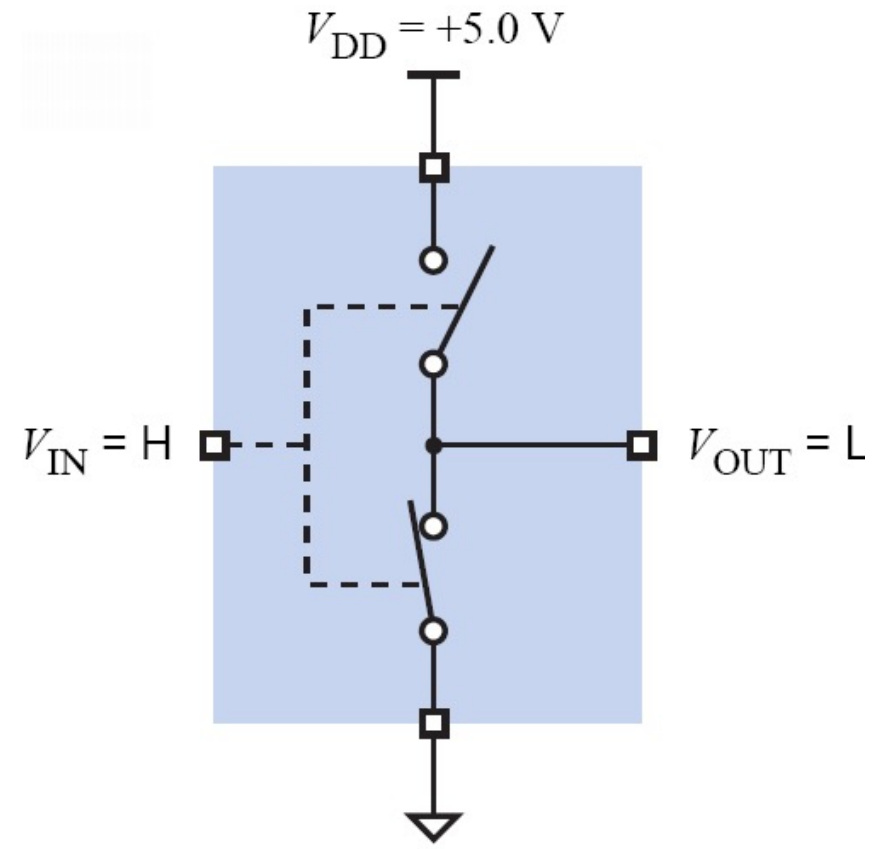
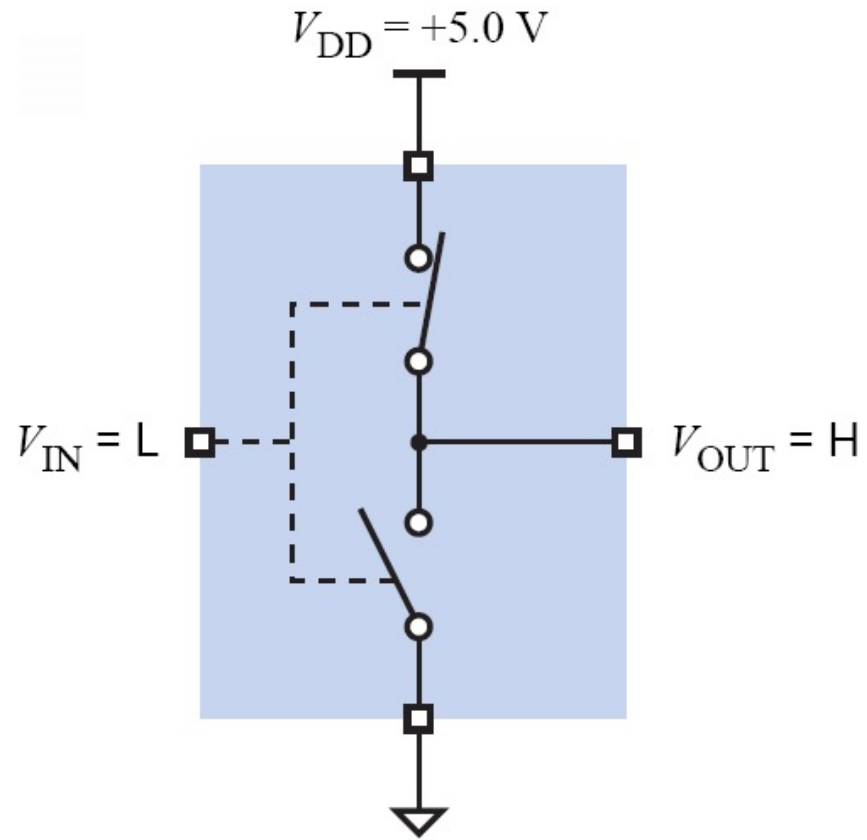
- It is all about playing with voltage and **switches**!
- We just need to come up with the logic behind this **switching**.

Hence, the term “Digital Logic” Design

**What do I mean by “switches”?**



# Inverter



# That Car Example...

- Let us assume that we have only two doors in our car. If one of the two doors are open, set the alarm signal to 1.

# That Car Example...

- 2 doors

Door	Open	Close
X	1	0
Y	1	0

**How would you express the logic?**

# That Car Example...

- If ( $X = 1$  **or**  $Y = 1$ ) then **alarm** = 1

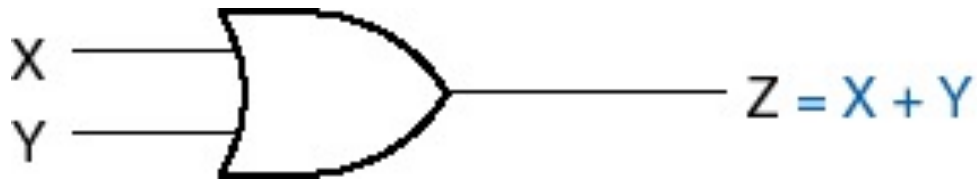
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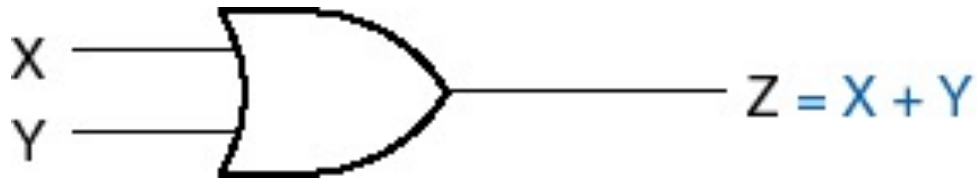


**OR Gate**

X	Y	X OR Y
0	0	0
0	1	1
1	0	1
1	1	1

# That Car Example...

- If ( $X = 1$  **or**  $Y = 1$ ) then **alarm** = 1



**OR Gate**

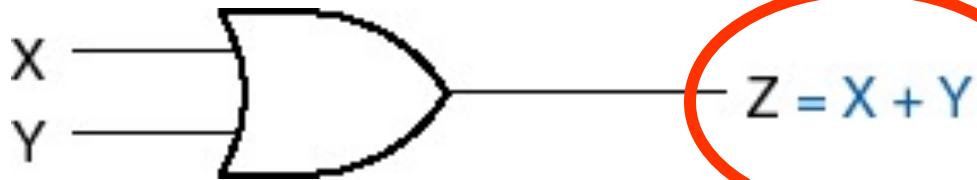
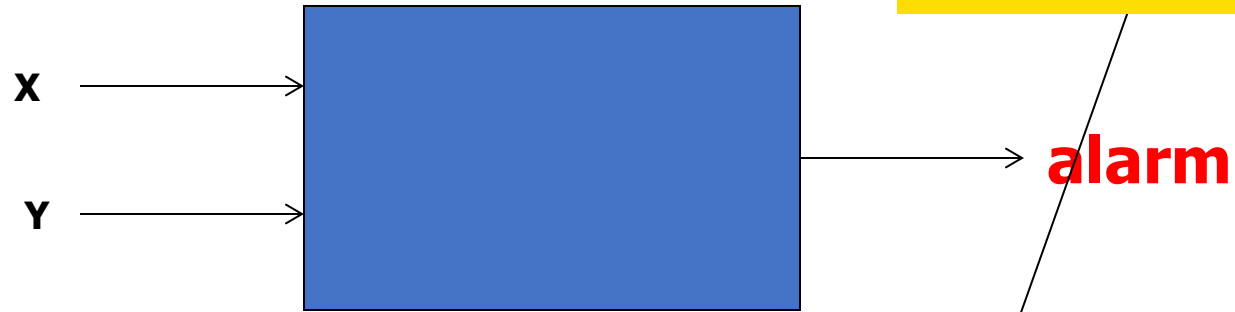
Truth Table

X	Y	X OR Y
0	0	0
0	1	1
1	0	1
1	1	1

# That Car Example...

- If ( $X = 1$  **or**  $Y = 1$ ) then **alarm** = 1

## Truth Table



**OR Gate**

**OR is denoted using the "+" symbol**

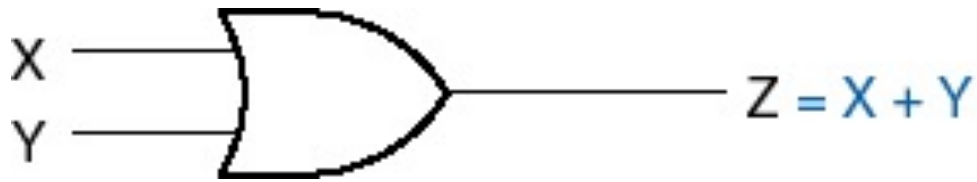
X	Y	X OR Y
0	0	0
0	1	1
1	0	1
1	1	1



# That Car Example...

- If ( $X = 1$  **or**  $Y = 1$ ) then **alarm** = 1

**Congratulations!**  
**I just introduced you to your first logic gate!**



**OR Gate**

X	Y	X OR Y
0	0	0
0	1	1
1	0	1
1	1	1

# Now, a **changed** Car Example...

- **If and only if** both of the two doors are open, set the alarm signal to 1.

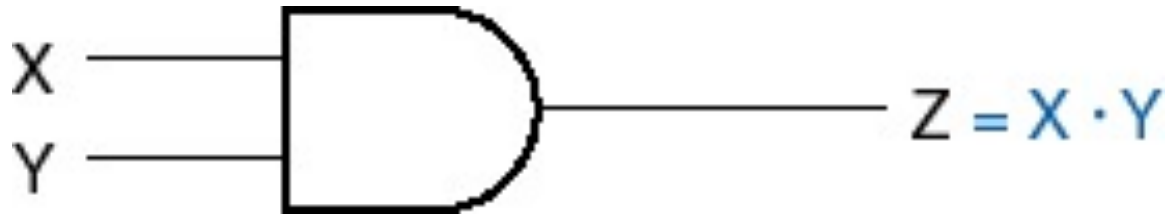
**How would you express the logic?**

# That Car Example...

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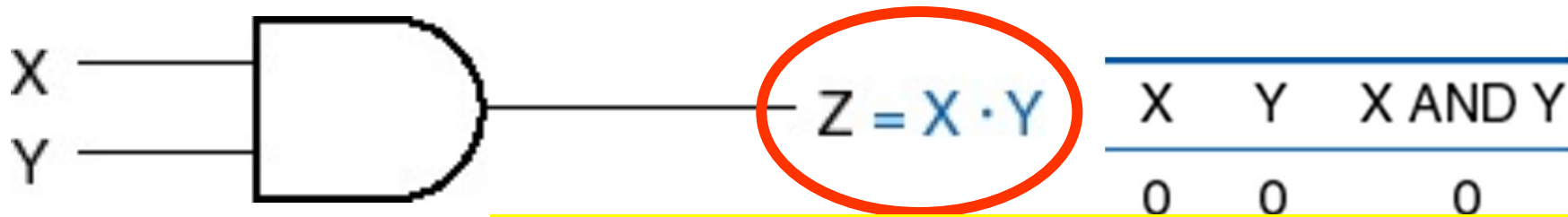


**AND Gate**

X	Y	X AND Y
0	0	0
0	1	0
1	0	0
1	1	1

# That Car Example...

- If ( $X = 1$  **and**  $Y = 1$ ) then **alarm** = 1



**AND Gate**

AND is denoted using the "." symbol

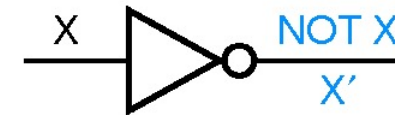
# Gates

- Gates are basic digital devices
- A gate takes one or more inputs and produces an output
  - Can be considered as a function
  - Inputs are either 0 or 1



X	Y	X AND Y
0	0	0
0	1	0
1	0	0
1	1	1

X	Y	X OR Y
0	0	0
0	1	1
1	0	1
1	1	1



X	NOT X
0	1
1	0

# Boolean operators

- Complement:  $X'$  (opposite of  $X$ )
- AND:  $X \cdot Y$
- OR:  $X + Y$

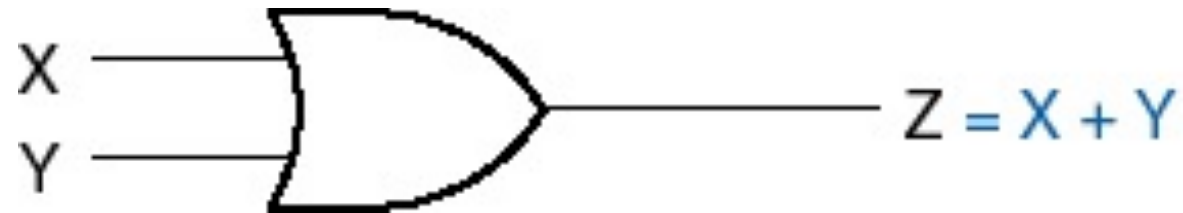
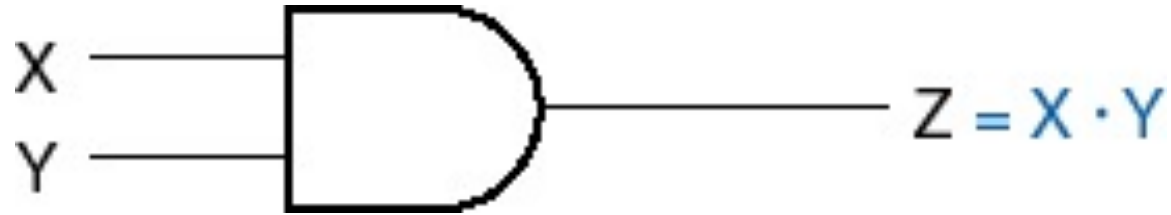
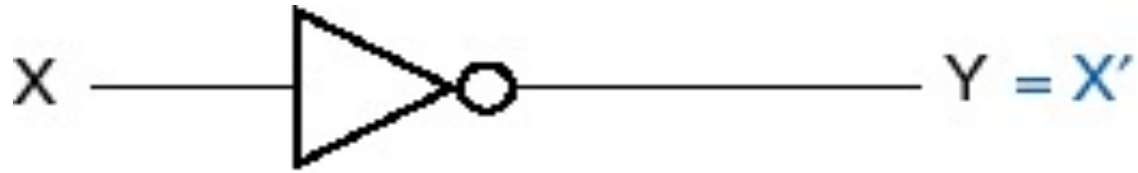
Function described  
with [truth table](#).

X	Y	X AND Y
0	0	0
0	1	0
1	0	0
1	1	1

X	Y	X OR Y
0	0	0
0	1	1
1	0	1
1	1	1

X	NOT X
0	1
1	0

# Logic symbols of NOT, AND, and OR





# Now, another **changed** Car Example...

- **If and only if** both of the two doors are open (or close), set the alarm signal to 1.

**How would you express the logic?**

# That Car Example...

If ((X = 1 **and** Y = 1) **or** (X = 0 **and** Y = 0))  
then **alarm** = 1

**Can you generate the truth table for this?**

# That Car Example...

If  $((X = 1 \text{ and } Y = 1) \text{ or } (X = 0 \text{ and } Y = 0))$

then **alarm** = 1

<i>X</i>	<i>Y</i>	Alarm
0	0	1
0	1	0
1	0	0
1	1	1

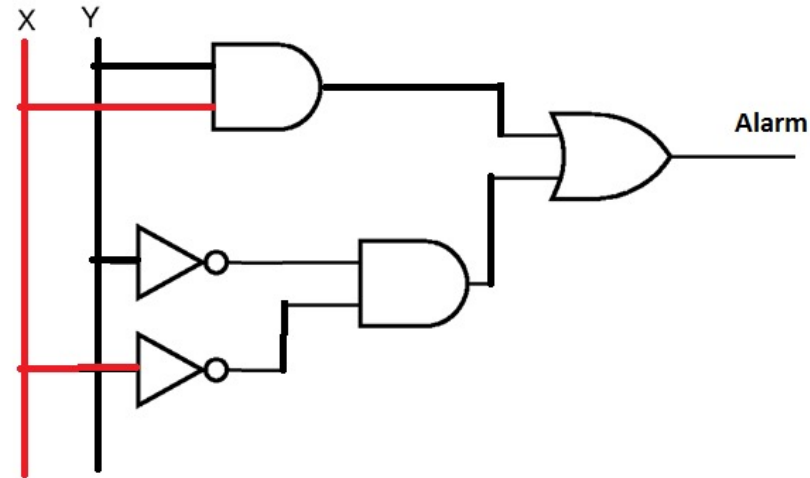
**Can you implement this logic using the gates we have seen so far?**

# That Car Example...

If  $((X = 1 \text{ and } Y = 1) \text{ or } (X = 0 \text{ and } Y = 0))$

then **alarm** = 1

X	Y	Alarm
0	0	1
0	1	0
1	0	0
1	1	1



**Can you implement this logic using the gates we have seen so far?**

- So, the idea is to –
  - First, express the circuit design problem in terms of input binary variables
  - Second, identify the output binary variables
  - Third, build a truth table where you need to assign a value to the output variable for each combination of input variables
  - Finally, express the output variable(s) in terms of input variables
  - **We will see how to do the last step soon!**