**To nest or not to nest, that is the question.** An argument that NCList is unnecessary. BH 2019.08.09 rev.

**Just for discussion**; based on *Nested Containment List (NCList): a new algorithm for accelerating interval query of genome alignment and interval databases*, Alexander V. Alekseyenko and Christopher J. Lee, Vol. 23 no. 11 **2007**, pages 1386–1393. doi:10.1093/bioinformatics/btl647

These authors present a nested approach to finding overlapping intervals within a potentially very large set of intervals. They argue that in a situation such as given in their Fig. 2 (Figure 1), it is better to nest interval *y* into *x* than to leave it in the initially searched list.

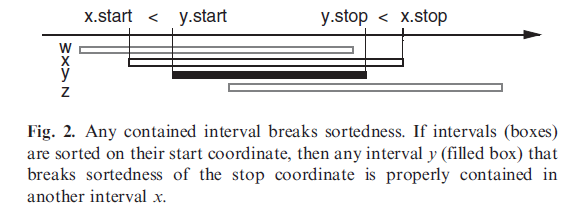


Figure 1. The original issue leading to the development of NCList.

The authors state the problem in this way (bold mine):

*Interval query can be slow because the overlapping intervals for any given query may not be contiguous in standard indexing.* ***Therefore, the database query cannot stop at the first non-overlapping interval, but must scan the rest of the database.***

And their solution:

*We can easily solve this problem by realizing that it is caused solely by the intervals that are contained within other intervals, i.e. x. start < y. start y.stop < x.stop. (see Fig. 2). If a sorted list of intervals has both start and stop coordinates in ascending order, then the overlapping intervals for any query are guaranteed to be contiguous in the list.*

The solution is clever. Create a list that is *monotonic* in both start and end for all intervals by packaging any nonconforming intervals (*y* in this case) into one of those conforming intervals (i.e., *x*). NCList’s findOverlap(from,to) method involves a series of binary searches that are of sets potentially smaller than *N*, each followed by a linear contiguous scan. For example, consider using NCList, for all overlaps of interval *I,* as shown in (my) Figure 2. Intervals *w*, *x*, and *z* are monotonically increasing in both start and end positions, but *y* is not. We package *y* into *x*. A binary search for “the first end point after the start of interval *I*“ finds *w*. A linear forward scan finds *x,* and *z*. A second binary search and linear scan through the subintervals of *x* finds *y*.



Figure 2: NCList looking for overlaps with *I* finds *w* first using a binary search for the closest end point after the start of *I* (1), then scans forward for intervals that have a starting point before the end of *I* (2), finding *x* and *z*. Interval *y* is found within *x* using a second binary search (3), followed again by a second forward search (not shown, because in this case *y* is the only subinterval of *x*).

**Jalview’s NCList implementation – IntervalStore**

The implementation of NCList in Jalview, IntervalStore<SequenceFeature> is identical to the original specification, with the added efficiency that during initialization all intervals that have no subintervals are set aside in a separate list. While this adds complications when adding or removing intervals from the set, it is more efficient in terms of storage (just a simple ArrayList<SequenceFeature>). The Jalview implementation is further optimized by separating different *types* of features (plaf, variant, etc.) into separate FeatureStore objects, each with their own IntervalStore. This substantially reduces the number of levels of nesting as well as the number of intervals in any single binary search.

**But do we have to nest?**

There is another, considerably simpler, solution involving a linked list with similarly scalable performance. The problem addressed by NCList is that once the first binary search is over, we still don’t know which intervals that start ahead of our specified interval overlap with it. Consider the situation in Figure 3. A set of eight intervals, a-h, are not ordered by start but not monotonic in end. NCList creates a set of subsets that are internally monotonic in both start and end: Set a contains b, g, and h; Set b contains c, d, and e; and Set e contains f. The key point here is that we are removing c, d, e, and f from the initial binary search.



Figure 3. (a) Eight intervals a-h, in order of increasing start position is not monotonic in end position. The indicated query must return the set {a, b, e, f, g}. (b) NCList nests intervals that are not monotonically increasing in both start and end points, creating subset {b, g, h} within a, subset {c, d, e} within b, and subset {f} within e. Within each subset the intervals are monotonic in both start and end point.

NCList processing finds the “first interval having an end point not before the query interval.” In this case, it finds a. Then, within a’s subsets it finds b, within b it finds e, and within e it finds f. Interval g is found by scanning the subset {b, g, h} in sequential order until the start of an interval (h in this case) is past the end of the query interval. This works, but might it be overly complicated?

Now consider the simple alternative shown in Figure 4, where we allow for a linked list of pointers from an interval to the *nearest prior interval that contains its starting point*.



Figure 4. An alternative to NCList that utilizes a reference for each interval pointing to the nearest prior interval that contains its starting point. Note that intervals f and h flank this interval but are not included in it.

A *dual binary search* for the *two nearest starting points flanking this query* gives us f and h. The set of all intervals starting between these ({g} in this case) is added to the results. Interval f along with all intervals that are linked from it (f -> e -> b -> a), are added only if their end is not before the start of the query interval. Note that intervals c and d are never checked, since they are not in the linked list starting from f.

The implementation at <https://github.com/BobHanson/IntervalStoreJ> uses a simple int[] array to manage the linked list, where the elements of the array are relative index offsets rather than actual object references. Thus, for the set {a b c d e f g h} the offsets would be [\*, 1, 1, 2, 3, 1, 2, 1], where \* is a reserved number (Integer.MIN\_VALUE, as implemented) meaning “not contained”, which stops all link processing when it is found.

As described, the algorithm is not scalable for sets where there is substantial overlap. The problem is that this sort of set produces long strings of pointers. An improvement involves indicating an offset with a negative number when the pointer is to an interval that has a higher end point than any that comes before it (Figure 5). If that interval is checked and found to have an end point prior to the start of the query interval, it is guaranteed that no further checking along the chain will lead to a result. We can stop scanning.



Figure 5: Offsets indicated with negative numbers to indicate a link to the interval with the highest end point of any previous intervals. The process (f -> e -> b -> a -> etc.) can be terminated after checking interval a, since its offset from b is -1, meaning that we know that no interval before Interval a extends beyond Interval a (into query *I*).

**Accelerating the loading of intervals**  
  
A major difficulty is trying to scale loading time, particularly if checking for duplicates. The problem is that every time a new interval is added, one has to check to see if it is a duplicate of any other in the set. As shown in Figure 6, this is a problem for both of the NCList Java implementations.

Figure 6. Comparison of loading time in ms vs. N log N for the loading of N intervals and not allowing duplicates. NCList does not scale, at least in these two implementations (top two data sets). Lower traces is for IntervalStore using a linked list.

Two major improvements give a huge advantage to the linked list approach. First, in this version of intervalstore.nonc.IntervalStore, all private storage of array data is handled by a simple IntervalI[ ] array. ArrayList is not used at all. This allows substantially more control over array capacity and accelerates all array processing. For example, Java’s ArrayList will expand its back-end array buffer *one element at a time* as elements are added. In this implementation, we double the capacity of the array whenever we need to, leading to a log N dependence on array enlargement.

One might think this would lead to a waste of space, but actually not. We use the extra capacity to temporarily handle out-of-sequence additions, saving hugely in incremental sorting time. Thus, we grow the array *from both ends*, as shown in Figure 7, using the front end of the array to hold the growing trunk of ordered intervals and the tail end of the array to hold a binary linked list of ordered branches off this main trunk



Figure 7. Double-ended array holding a growing binary tree of intervals with main trunk growing from the left that is searchable using a binary search. Dotted lines are links indicating branching points.

Periodically, when it is time to enlarge the array, we simply scan the main trunk from right to left, shifting blocks of intervals right, inserting the linked branches in a single pass, and discarding the branches. Array shifting uses highly efficient native System.arrayCopy calls. The array is fully trimmed after the incremental loading is completed.

**Deletion of intervals**

Figure 8 shows preliminary results for deletion timing. The test deletes 1000 intervals from a collection of N intervals. No effort has been made to optimize this for linked lists. Such is the cost of doing a rebuilding of the array after each deletion.

Figure 8. Timing for deletion of N intervals. No optimization has been done yet.

We can do better by simply logging each deletion to a BitSet at the time of deletion and then, lazy, only when needed, do a single run of array shifts to fill in the deleted intervals. With this optimization we see significant improvement (Figure 9).

Figure 9. Timing for deletion of N intervals after optimization of the linked-list algorithm using a BitSet and lazy initialization.

**Advantages and disadvantages**

The advantage of NCList is that it pre-partitions the binary search of *N* objects into a set of *n* binary searches of *m­i* ≤ *N* objects, where SUM(*i*){*mi*} = *N*. Depending upon the extent of nesting, this could be significant. With minimally nested sets, however, it is unlikely that this advantage would be noticeable.

The primary advantages of the linked list approach include:

(1) It processes queries very efficiently, with a single binary search, followed by a single link-based check.

(2) It requires minimal initialization, with very little allocated memory (just simple arrays IntervalI[N] and int[N]). The simple linked list avoids the necessity for all the nesting structure that comes with NCNodes and NCList, as well as all initialization that goes with those objects.

(3) It allows for “lazy" initialization. That is, we can do all the loading of the list, including minor addition/removal with the option to not sort the actual list or build the links until it is absolutely necessary (the first findOverlap() call, generally). Rebuilding after addition or removal is simply a recalculation of the offsets array.

(4) The return list is in the same order (albeit reversed, for performance reasons) as the original sorted list. In contrast, IntervalStoreJ’s implementation of NCList uses of separate nested and unnested lists, which are processed sequentially. It thus returns a list that might or might not be ordered. In some situations, this could be an advantage.

**Timing results: query (see testQuery.xlsx**

Timing results for querying (Table 1 and Figure 9) suggest that using a linked list is from two to three times faster than NCList alone or the IntervalStoreJ/NCList implementation. In fact, compared to NCList, the linked list alternative will return 100,000 queries from a set containing 464K intervals in the time it takes NCList to return 100,000 queries from a list that contains only 2K intervals. All three method times are linear in log N for large N and governed by other factors at low N.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| **logN** | **N** | **IntNC** | **NCList** | **IntLink** |
| 3.33 | 2154 | 160.4 | 222.9 | 88.2 |  |
| 3.67 | 4641 | 165.1 | 232.8 | 90.6 |  |
| 4.00 | 10000 | 173.5 | 241.8 | 95.4 |  |
| 4.33 | 21544 | 183.9 | 262.6 | 99.4 |  |
| 4.67 | 46415 | 201.2 | 306.9 | 105.7 |  |
| 5.00 | 100000 | 244.8 | 365.3 | 121.5 |  |
| 5.33 | 215443 | 289.7 | 406.5 | 144.3 |  |
| 5.67 | 464158 | 327.3 | 435.1 | 169.6 |  |
| 6.00 | 1000000 | 363.7 | 467.8 | 189.1 |  |

Table 1. Timing results (in ms) for returning 100,000 queries from a “sequence” of length N \* 10 that contains N intervals of pseudorandom length 1 to 50 for IntervalStore/NCList (“IntNC”), Nclist alone, and IntervalStore/linked list (“IntLink”). The start positions of the intervals within the sequence are in the range 1 to N \* 10 - 50. Each query has a length of 1000 and a pseudorandom position within the sequence.

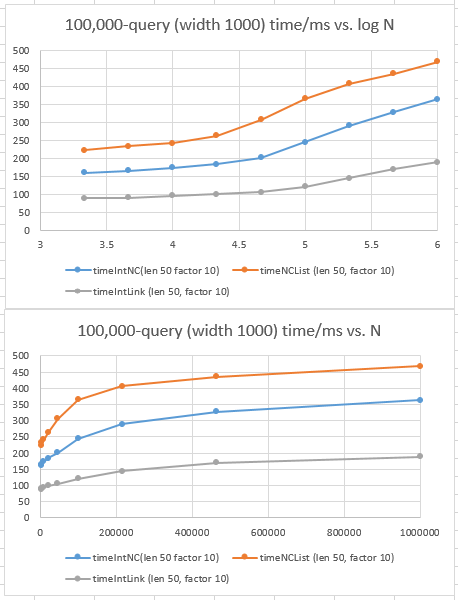


Figure 9. Query time vs. logN and N for the linked-list variation of IntervalStore (lowest set), along with the IntervalStore implementation of NCList (middle data set), and NCList without IntervalStore (highest set).

Full run:

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| [RemoteTestNG] detected TestNG version 6.14.2 | | | |  |  |  |  |
| Java version: 1.8.0\_191 |  |  |  |  |  |  |  |
| amd64 Windows 10 10.0 cores:4 | |  |  |  |  |  |  |
| 14 Aug 2019 21:09:15 GMT | |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| Test | size N | tests | time/ms | rate/(N/ms) | time stderr | rate stderr | |
| # Query IntStoreNCList store interval size 50 store sequence factor 10 query width -1000 query count 100000 | | | | | | | |
| IntStoreNCList query | 2154 | 10 | 160.4 | 13.5 | 2.93 | 0.24 |  |
| IntStoreNCList query | 4641 | 10 | 165.1 | 28.1 | 0.54 | 0.09 |  |
| IntStoreNCList query | 10000 | 10 | 173.5 | 57.6 | 0.7 | 0.23 |  |
| IntStoreNCList query | 21544 | 10 | 183.9 | 117.2 | 0.48 | 0.3 |  |
| IntStoreNCList query | 46415 | 10 | 201.2 | 230.7 | 0.79 | 0.89 |  |
| IntStoreNCList query | 100000 | 10 | 244.8 | 408.4 | 0.54 | 0.9 |  |
| IntStoreNCList query | 215443 | 10 | 289.7 | 743.7 | 0.47 | 1.2 |  |
| IntStoreNCList query | 464158 | 10 | 327.3 | 1418.4 | 1.16 | 4.95 |  |
| IntStoreNCList query | 1000000 | 10 | 363.7 | 2749.4 | 0.57 | 4.33 |  |
| # dimensions [7 1000000] |  |  |  |  |  |  |  |
| # Query IntStoreNCList0 store interval size 50 store sequence factor 10 query width -1000 query count 100000 | | | | | | | |
| IntStoreNCList0 query | 2154 | 10 | 183.3 | 11.8 | 3.89 | 0.22 |  |
| IntStoreNCList0 query | 4641 | 10 | 190.5 | 24.4 | 1.6 | 0.19 |  |
| IntStoreNCList0 query | 10000 | 10 | 197.1 | 50.7 | 0.56 | 0.14 |  |
| IntStoreNCList0 query | 21544 | 10 | 207 | 104.1 | 0.46 | 0.23 |  |
| IntStoreNCList0 query | 46415 | 10 | 225.2 | 206.1 | 0.43 | 0.39 |  |
| IntStoreNCList0 query | 100000 | 10 | 286.5 | 351.2 | 8.01 | 8.63 |  |
| IntStoreNCList0 query | 215443 | 10 | 315.6 | 683 | 2.03 | 4.21 |  |
| IntStoreNCList0 query | 464158 | 10 | 354.2 | 1310.4 | 0.59 | 2.19 |  |
| IntStoreNCList0 query | 1000000 | 10 | 389.6 | 2567 | 0.99 | 6.6 |  |
| # dimensions [7 0] |  |  |  |  |  |  |  |
| # Query IntStoreLink store interval size 50 store sequence factor 10 query width -1000 query count 100000 | | | | | | | |
| IntStoreLink query | 2154 | 10 | 88.2 | 24.5 | 2.24 | 0.52 |  |
| IntStoreLink query | 4641 | 10 | 90.6 | 51.2 | 0.62 | 0.34 |  |
| IntStoreLink query | 10000 | 10 | 95.4 | 104.8 | 0.41 | 0.45 |  |
| IntStoreLink query | 21544 | 10 | 99.4 | 216.8 | 0.24 | 0.53 |  |
| IntStoreLink query | 46415 | 10 | 105.7 | 439.3 | 0.34 | 1.43 |  |
| IntStoreLink query | 100000 | 10 | 121.5 | 823.4 | 0.3 | 2 |  |
| IntStoreLink query | 215443 | 10 | 144.3 | 1493.6 | 0.58 | 5.89 |  |
| IntStoreLink query | 464158 | 10 | 169.6 | 2748.3 | 3.96 | 54.12 |  |
| IntStoreLink query | 1000000 | 10 | 189.1 | 5287.4 | 0.29 | 8.23 |  |
| # dimensions [126 416364] | |  |  |  |  |  |  |
| # Query IntStoreLink0 store interval size 50 store sequence factor 10 query width -1000 query count 100000 | | | | | | | |
| IntStoreLink0 query | 2154 | 10 | 83.1 | 25.9 | 0.18 | 0.06 |  |
| IntStoreLink0 query | 4641 | 10 | 87 | 53.4 | 0.81 | 0.47 |  |
| IntStoreLink0 query | 10000 | 10 | 89.7 | 111.5 | 0.28 | 0.34 |  |
| IntStoreLink0 query | 21544 | 10 | 93.6 | 230.2 | 0.31 | 0.76 |  |
| IntStoreLink0 query | 46415 | 10 | 99.7 | 465.7 | 0.31 | 1.46 |  |
| IntStoreLink0 query | 100000 | 10 | 120 | 833 | 0.29 | 2.01 |  |
| IntStoreLink0 query | 215443 | 10 | 146 | 1476.1 | 0.14 | 1.45 |  |
| IntStoreLink0 query | 464158 | 10 | 170.2 | 2726.5 | 0.42 | 6.71 |  |
| IntStoreLink0 query | 1000000 | 10 | 193.3 | 5173.2 | 0.19 | 5.14 |  |
| # dimensions [126 416364] | |  |  |  |  |  |  |
| # Query NCList store interval size 50 store sequence factor 10 query width -1000 query count 100000 | | | | | | | |
| NCList query | 2154 | 10 | 222.9 | 9.7 | 0.71 | 0.03 |  |
| NCList query | 4641 | 10 | 232.8 | 19.9 | 0.41 | 0.03 |  |
| NCList query | 10000 | 10 | 241.8 | 41.3 | 0.51 | 0.09 |  |
| NCList query | 21544 | 10 | 262.6 | 82.8 | 9.44 | 2.31 |  |
| NCList query | 46415 | 10 | 306.9 | 151.2 | 0.4 | 0.2 |  |
| NCList query | 100000 | 10 | 365.3 | 273.7 | 0.49 | 0.37 |  |
| NCList query | 215443 | 10 | 406.5 | 530 | 0.19 | 0.25 |  |
| NCList query | 464158 | 10 | 435.1 | 1066.9 | 0.21 | 0.52 |  |
| NCList query | 1000000 | 10 | 467.8 | 2142.7 | 8.04 | 32.38 |  |
| # dimensions [7 528974] |  |  |  |  |  |  |  |
| # Query NCList0 store interval size 50 store sequence factor 10 query width -1000 query count 100000 | | | | | | | |
| NCList0 query | 2154 | 10 | 230.3 | 9.4 | 2.1 | 0.08 |  |
| NCList0 query | 4641 | 10 | 239.7 | 19.4 | 0.86 | 0.07 |  |
| NCList0 query | 10000 | 10 | 246.3 | 40.6 | 0.27 | 0.04 |  |
| NCList0 query | 21544 | 10 | 260.3 | 82.8 | 0.85 | 0.27 |  |
| NCList0 query | 46415 | 10 | 310.2 | 149.6 | 0.37 | 0.18 |  |
| NCList0 query | 100000 | 10 | 365 | 274 | 0.64 | 0.48 |  |
| NCList0 query | 215443 | 10 | 404.9 | 532.1 | 0.33 | 0.44 |  |
| NCList0 query | 464158 | 10 | 434.4 | 1068.6 | 0.66 | 1.62 |  |
| NCList0 query | 1000000 | 10 | 462.4 | 2163.4 | 3.36 | 14.88 |  |
| # dimensions [7 ?] |  |  |  |  |  |  |  |
| # resultcounts [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 100, 113, 96, 112, 100, 93, 98, 112, 88] | | | | | |  |  |
|  |  |  |  |  |  |  |  |
| PASSED: testLoadTimeBulk | |  |  |  |  |  |  |
| PASSED: testLoadTimeIncrementalAllowDulicates | | | |  |  |  |  |
| PASSED: testLoadTimeIncrementalNoDuplicates | | | |  |  |  |  |
| PASSED: testQueryTime |  |  |  |  |  |  |  |
| PASSED: testRemoveTime |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| =============================================== | | | |  |  |  |  |
| Default test |  |  |  |  |  |  |  |
| Tests run: 5, Failures: 0, Skips: 0 | |  |  |  |  |  |  |
| =============================================== | | | |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| =============================================== | | | |  |  |  |  |
| Default suite |  |  |  |  |  |  |  |
| Total tests run: 5, Failures: 0, Skips: 0 | | |  |  |  |  |  |
| =============================================== | | | |  |  |  |  |

test/intervalstore/nonc/ISListTimingTests.java settings:

/\*\*

\* factor to multiply first parameter of generateIntervals(sequenceWidth,

\* count, length) by to set store sequence width; higher number reduces number

\* of overlaps

\*/

**private** **static** **final** **int** ***QUERY\_STORE\_SEQUENCE\_SIZE\_FACTOR*** = 10;// 10;

/\*\*

\* interval size for the store; absolute(negative) or maximum(positive);

\*/

**private** **static** **final** **int** ***QUERY\_STORE\_INTERVAL\_SIZE*** = 50;// -1 for SNPs;

/\*\*

\* width of query intervals; negative for absolute, positive for max value

\*

\*/

// private static final int QUERY\_WINDOW = -1;// overview single-pixel overlap

**private** **static** **final** **int** ***QUERY\_WINDOW*** = -1000;// -1000 standard view

/\*\*

\* number of queries to generate (independently of the size of the sequence

\*

\*/

**private** **static** **final** **int** ***QUERY\_COUNT*** = 100000;

**int** sequenceWidth = count \* ***QUERY\_STORE\_SEQUENCE\_SIZE\_FACTOR***;

…

List<Range> ranges = generateIntervals(sequenceWidth, count,

***QUERY\_STORE\_INTERVAL\_SIZE***);

List<Range> queries = generateIntervals(sequenceWidth, ***QUERY\_COUNT***,

***QUERY\_WINDOW***);

…

/\*\*

\* Generates a list of <code>count</code> intervals of length [1,length] in

\* the range [1, sequenceWidth]

\*

\* **@param** sequenceWidth

\* scale of the sequence, based on the number of intervals present,

\* not the number of queries

\* **@param** count

\* the number of intervals to generate

\* **@param** length

\* maximum (positive) or absolute(negative) number of intervals to

\* generate

\*

\* **@return list of intervals**

\*/

**private** **synchronized** List<Range> generateIntervals(**int** sequenceWidth,

**int** count, **int** length)

{

**int** maxPos = sequenceWidth - Math.*abs*(length);

List<Range> ranges = **new** ArrayList<>();

**for** (**int** j = 0; j < count; j++)

{

**int** from = 1 + rand.nextInt(maxPos);

**int** to = from + (length < 0 ? -length - 1 : rand.nextInt(length));

ranges.add(**new** Range(from, to));

}

**return** ranges;

}

**Timing results – Loading (see testLoad.xlsx)**

15 Aug 2019 21:11:19 GMT

Test size N tests time/ms rate/(N/ms) time stderr rate stderr

# incr allowDuplicates:true IntStoreNCList

IntStoreNCList incr load dup 2154 10 1.5 1485.1 0.09 110.44

IntStoreNCList incr load dup 4641 10 3.4 1416.6 0.24 106.29

IntStoreNCList incr load dup 10000 10 7.4 1401.6 0.42 83.57

IntStoreNCList incr load dup 21544 10 16.5 1368.6 1.28 92.09

IntStoreNCList incr load dup 46415 10 43.3 1077.6 1.23 25.18

IntStoreNCList incr load dup 100000 10 172.2 582.9 3.74 11.57

IntStoreNCList incr load dup 215443 10 765.2 282.7 17.15 5.55

IntStoreNCList incr load dup 464158 10 3496.1 132.8 15.56 0.59

**IntStoreNCList incr load dup 1000000 10 18245.9 54.8 40.36 0.12**

# incr allowDuplicates:true IntStoreLink

IntStoreLink incr load dup 2154 10 3.9 603.9 0.37 58.82

IntStoreLink incr load dup 4641 10 5.3 917.6 0.45 49.58

IntStoreLink incr load dup 10000 10 11.7 869.1 0.52 32.64

IntStoreLink incr load dup 21544 10 26.5 831.4 1.64 34.71

IntStoreLink incr load dup 46415 10 65.7 714.1 2.22 24.46

IntStoreLink incr load dup 100000 10 148.7 696.3 11.62 33.90

IntStoreLink incr load dup 215443 10 356.7 607.8 9.76 15.54

IntStoreLink incr load dup 464158 10 870.2 534.3 12.36 7.21

**IntStoreLink incr load dup 1000000 10 2200.7 454.7 19.94 4.09**

# incr allowDuplicates:true NCList

NCList incr load dup 2154 10 1.5 1563.8 0.13 156.47

NCList incr load dup 4641 10 3.7 1353.7 0.32 114.84

NCList incr load dup 10000 10 7.4 1374.5 0.29 42.92

NCList incr load dup 21544 10 17.0 1320.1 1.19 79.90

NCList incr load dup 46415 10 50.1 927.0 0.48 8.80

NCList incr load dup 100000 10 206.5 487.1 5.72 11.64

NCList incr load dup 215443 10 906.3 237.9 9.40 2.37

NCList incr load dup 464158 10 4359.8 106.5 18.97 0.46

**NCList incr load dup 1000000 10 23051.1 43.6 495.51 0.91**

# incr allowDuplicates:false IntStoreNCList

IntStoreNCList incr load nodup 2154 10 2.7 901.9 0.32 112.45

IntStoreNCList incr load nodup 4641 10 5.1 939.1 0.30 51.51

IntStoreNCList incr load nodup 10000 10 10.1 1001.2 0.30 26.86

IntStoreNCList incr load nodup 21544 10 27.6 780.3 0.30 8.37

IntStoreNCList incr load nodup 46415 10 84.7 550.4 1.96 11.30

IntStoreNCList incr load nodup 100000 10 308.5 329.2 13.18 13.27

IntStoreNCList incr load nodup 215443 10 1067.5 202.3 17.50 3.24

IntStoreNCList incr load nodup 464158 10 4411.9 105.3 50.45 1.16

**IntStoreNCList incr load nodup 1000000 10 22540.3 44.4 254.92 0.49**

# incr allowDuplicates:false IntStoreLink

IntStoreLink incr load nodup 2154 10 2.8 902.8 0.62 77.97

IntStoreLink incr load nodup 4641 10 7.2 676.0 0.51 49.04

IntStoreLink incr load nodup 10000 10 11.6 868.3 0.24 17.19

IntStoreLink incr load nodup 21544 10 26.7 807.0 0.23 7.14

IntStoreLink incr load nodup 46415 10 69.3 676.8 2.46 21.94

IntStoreLink incr load nodup 100000 10 160.2 629.2 5.08 16.76

IntStoreLink incr load nodup 215443 10 371.5 585.2 12.54 17.21

IntStoreLink incr load nodup 464158 10 976.6 476.7 17.87 8.66

**IntStoreLink incr load nodup 1000000 10 2546.9 393.6 43.56 6.37**

# incr allowDuplicates:false NCList

NCList incr load nodup 2154 10 1.8 1298.3 0.17 118.44

NCList incr load nodup 4641 10 3.5 1375.4 0.24 86.87

NCList incr load nodup 10000 10 7.8 1298.4 0.28 40.66

NCList incr load nodup 21544 10 21.0 1028.4 0.31 15.11

NCList incr load nodup 46415 10 69.5 669.3 0.93 8.52

NCList incr load nodup 100000 10 262.7 383.3 7.89 9.73

NCList incr load nodup 215443 10 1107.9 195.4 26.48 4.39

NCList incr load nodup 464158 10 4899.2 94.8 43.72 0.85

**NCList incr load nodup 1000000 10 23859.4 42.0 257.01 0.44**