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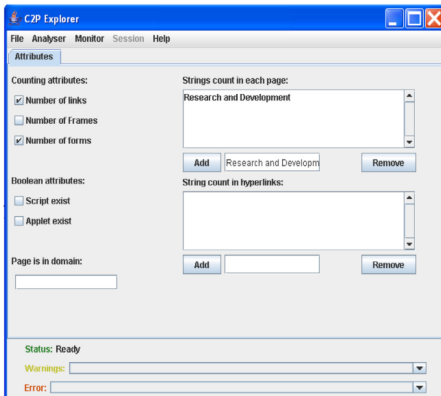
Run-time verification of web applications

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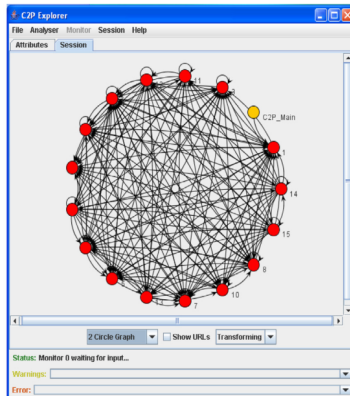
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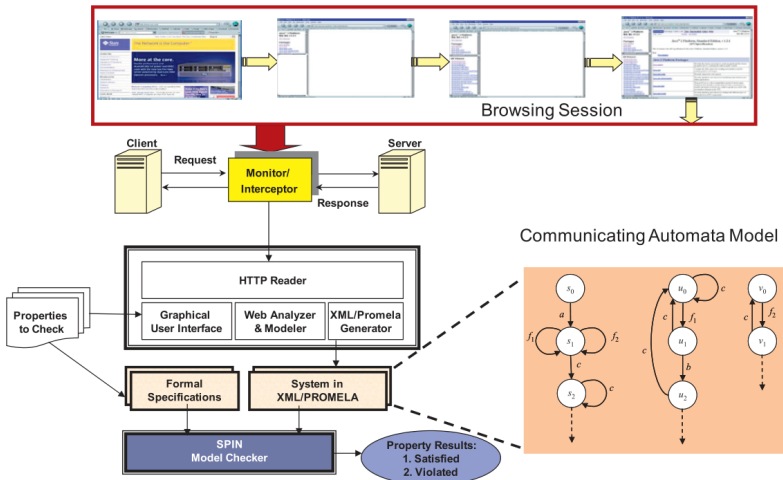
- Paper from 2013
- Tool for automatic verification of web applications
- Empirical results



(a)



(b)



- *Web Application Under Test (WAUT)*: the web application taken in consideration in a particular definition, discussion, etc...
- *request*: string l that represents a web request performed by a WAUT
- *response*: tuple $\langle u, c, I, L, V \rangle$ which represents the response that the web server sent to the WAUT
 - $u = l$
 - c represents the status code of the response [FNR22]
 - $I = \text{"target"}$ attribute of the forms contained in the response
 - $L = \text{URLs}$ of the links contained in the response
 - $V = \langle v_1, \dots, v_k \rangle$ vector where v_i is the valuation of the page attribute i



Some definitions first

- *browsing session*: denoted RRS , it is a recorded sequence of request-response exchanges that a user performs when visiting a WAUT
- *local browsing session*: denoted RRS as well, it is a recorded sequence of request-response exchanges that a user performs in a single browser window or frame

Communicating automata model

Single-display automaton

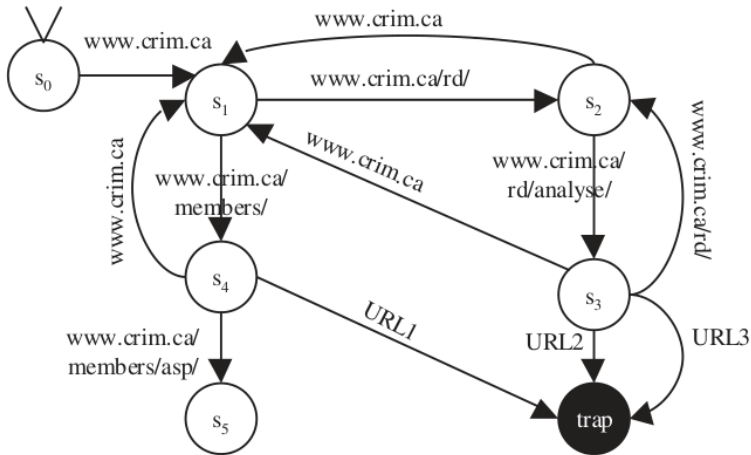
Convert a browsing session of a single-display application into an automaton.

- 1 the inactive state $s_0 = \langle u_0, c_0, I_0, L_0, V_0 \rangle$ is defined;
- 2 the set of states is defined by the set of *responses*, a response being $\langle u_i, c_i, I_i, L_i, V_i \rangle$
- 3 the alphabet is built from the union of the requests (*Req*), the URIs associated with links in the observed responses (Γ), and the actions that correspond to the unexplored forms in the observed responses Δ . $\Sigma = Req \cup \Gamma \cup \Delta$;
- 4 there is a transition (s_i, l_{i+1}, s_{i+1}) from state s_i to state s_{i+1} if there is a **link** or a **form action** that goes from the page represented by s_i to the page represented by s_{i+1} ;
- 5 for each unexplored link $l \in L_i$ or form $a \in I_i$, the automaton has a transition from the state representing the page $\langle u_i, c_i, I_i, L_i, V_i \rangle$ to a so-called *trap* state $t \in T$.



- from the construction of a single-display automaton, it is possible to derive **deduced** links
- i.e. links that are not visited during the browsing session, but present in at least one of the responses

Example of single-display automaton



From single-display to multi-display:

- *response*: $\langle u, c, I, F, L, V \rangle$ with F being a set of frames in the page. The target t is defined; if no target is present $t = \varepsilon$.

Additional changes are:

- $\langle l, t \rangle \in L$
- $\langle a, t \rangle \in I$
- $\langle f, b \rangle \in F$
- the *requests* are now made of the link as before, with the addition of the referer r (link from which the request started) and the target t . They are denoted as $\langle r, l, t \rangle$

Convert a browsing session of a multi-display application into a communicating automata model.

- ① a browsing session is split into a local browsing session (RRS_1, \dots, RRS_k) , one for each window and frame;
- ② convert each local browsing session into an automaton;
 - ① convert a RRS to a single-display automaton;
 - ② the alphabet Σ_i is extended with the source pages of the frames (src attribute), $\Sigma_i := \Sigma_i \cup \Phi_i$;
 - ③ the case in which the user clicks on a link or submits a form while a frame is loading is handled by adding a transition from each state of the local automaton to the response state;
 - ④ each unexplored link $\langle r_i, l_i, t_i \rangle \in \Gamma_i$ is mapped to a loop in the state it targets (self-loop);
- ③ create the communicating automata via the *parallel composition operator*, denoted $A_1 \parallel A_2$. The compositions of multiple automata is denoted $A_1 \parallel \dots \parallel A_k$



Extending the automata model

- there is the need to characterize states of the automata
- because the browser automatically triggers frame requests upon loading the page that contains them
- extension happens via addition of a *context variable*
- *transient* and *stable* states

We build the Extended Automaton Q_i . Σ_i^d is the set of those transitions who cause the automaton to pass through a transient state, called “designated set of transitions”.

- ① the set of states S_i , alphabet Σ_i and initial state s_{0i} are unchanged;
- ② x_i is the context variable of Q_i , x_{0i} is the context variable's initial state;
- ③ for each transition $(s, a, s') \in T_i$, $s, s' \in S_i$, $a \in \Sigma_i$:
 - ① if $s = s'$ and $a \in \Sigma_i^d$, then $(s, a, x_i := x_i - 1, s)$ is a transition in Q_i , where $x_i := x_i - 1$ is the update of the transition; or
 - ② $(s, a, x_i := |init(s') \cap \Sigma_i^d|, s')$ is a transition in Q_i , where $x_i := |init(s') \cap \Sigma_i^d|$ is the update of the transition.

- 1 build the single-display automata;
- 2 extend each automaton;
- 3 the set of designated transitions Σ_i^d is the **set of frames of the browsing session**;
- 4 x_i is initially set to 0;
- 5 at each state s_i , x_i is the number of browser triggered events enabled in s_i ;
- 6 each automaton is unfolded (transformed to its equivalent non-extended version);
- 7 the unfolded automata are composed using the composition operator.

Property specification



Property specification

- LTL is used
- authors introduce 2 new operators that allow to specify properties over a subset of the state
- \mathfrak{S} -scope operator over **propositional logic expressions**
- **In** operator over **logical formulas**

Example

$$G(((\neg Home \wedge \neg Shopping) \rightarrow (Promotions = 0)) \wedge \\ ((Home \wedge Shopping) \rightarrow (Promotions \leq 2)))$$

simplifies to

Example

$$G(((Promotions \leq 2) \textbf{In} (Home \vee Shopping)) \vee (Promotions = 0))$$

Implementation and empirical evaluation



- the tool can
 - record a browsing session
 - build an internal representation of the session
 - evaluate a set of properties against the internal representation
 - visualize the communicating automata
- the set of properties are categorized as
 - non-functional/general
 - functional/specific

- Non-functional:
 - ① Broken links and deadlocks are absent.
 - ② Number of links in each display (single or multi) should not exceed a certain threshold (depends on size of application).
 - ③ Number of images in each display (single or multi) should not exceed a certain threshold (depends on size of application).
 - ④ Number of links in each display (single or multi) is balanced.
 - ⑤ Combinations of certain words/objects are absent.

- Functional
 - 1 Home page is reachable from every other page.
 - 2 Page X is reachable from page Y without going through a cer- tain page Z.
 - 3 Secure pages are not reachable without authentication process.
 - 4 In e-commerce applications, promotions of certain products are only present either on the Home page or on Shopping pages and, for each page, the number of promotions does not exceed two.
 - 5 Privacy policy page in e-commerce applications is reachable from every page.

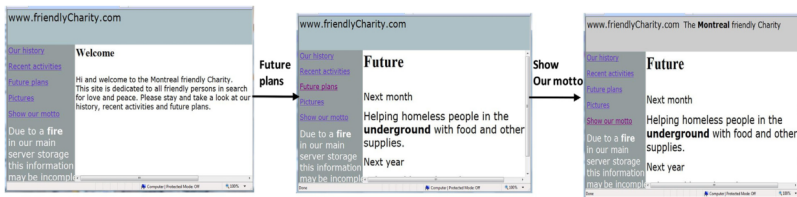
- most of the properties were violated
- small and large WAUT have **less** violations compared to medium-sized ones

An example of a specification where the authors found a counterexample:

“Combination of certain words are absent”

$$G((montreal \wedge fire \wedge underg) \vee ((montreal \wedge fire) \vee ((montreal \wedge underg) \vee ((underg \wedge fire) \vee montreal \vee underg \vee fire))))$$

Counterexample



Conclusions

- using multiple frames is not common practice in web app development
- nowadays applications are client-side rendered (via JavaScript) starting from JSON instead of HTML
- the approach presented might be more useful for websites, which use more of a mixed approach compared to web applications

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