In [30]:

```
import random
import numpy as np
import copy
import time
import matplotlib.pyplot as plt
import pandas as pd
```

In [31]:

```
random. seed(1)
n=100 #number of objects
b=5 #number of bins
c=50

#Generate random locations
vj=random.choices(range(10, 100), k=n)
wj=random.choices(range(5, 20), k=n)
```

Exercise 1

Solution Encoding

The solution is represented with an n by b matrix where n is the number of items and b is the number of containers. Entry (i,j) represents whether item i is assigned to container j with binary encoding.

The code below randomly generates a solution that might not be feasible. Each item has 1/3 chance to be put in the containers with equal probability.

In [32]:

The code below fixes an infeasible solution by randomly removing items from the overweighted bags.

```
In [33]:
```

```
#input: x-a table of arrangement that might not be feasible c-capacity
#output: x-a table of a feasible arrangement
def fix(x,c):
    #check whether the result is valid
    n, b=x. shape
   valid=True
   overweight={}
    for i in range(b):
        weight = 0
        for j in range(n):
            weight = wj[j] *x[j, i]
        if weight >c:
            valid=False
            overweight[i]=weight
    #randomly remove items until it meets the constraint
    if valid==False:
        for i, w in overweight. items():
            in_bag=[]
            for j in range(n):
                if x[j, i] == 1:
                    in_bag. append(j)
            while w>c:
                a=random.randint(0,len(in_bag)-1)
                x[in\_bag[a], i]=0
                w=wj[in\_bag[a]]
                in_bag.pop(a)
   return x
```

The code below is used to convert a numpy result table to a more readable one.

In [34]:

```
def final table(x):
        container=list(range(1,b+1))
        container.append('Total')
        package=[]
        for i in range(b):
            package. append ([])
            for j in range(n):
                if x[j, i] == 1:
                    package[i].append(j+1)
        package.append('')
        profits=[]
        weights=[]
        for i in range(b):
            profit=0
            weight=0
            for j in package[i]:
                profit + = vj[j-1]
                weight = wj[j-1]
            profits.append(profit)
            weights.append(weight)
        profits.append(sum(profits))
        weights.append('')
        data={'Container':container, 'Packages':package, 'Profit':profits, 'Weight':weights}
        return pd. DataFrame (data)
```

Mutation

For each item, it has a 0.1% chance of mutation. After the mutation, it will either be placed in another bag, or just removed from the bag.

In [57]:

```
\begin{array}{l} \text{def mutation}(x): \\ & n,b=x.\,\text{shape} \\ & \text{for i in range}(n): \\ & \text{\#randomly choose a number among 1 to 1000, the number has 0.1% chance to be 100} \\ & \text{m=random.randint}(1,1000) \\ & \text{if } m==100: \\ & \text{for j in range}(b): \\ & \text{if } x[i,j]==1: \\ & x[i,j]=0 \\ & \text{\#randomly choose a container to put the item in, if k=b, then just remove the item from k=random.randint(0,b)} \\ & \text{if } k!=b: \\ & x[i,k]=1 \\ & \text{return } x \end{array}
```

Fitness

Fitness in this case is just the total amount of profit.

```
In [58]:
```

```
#input: x-a table of a feasible arrangement
#output: profit-the fitness/total profit of this arrangement
def fitness(x):
    n, b=x. shape
    profit=0
    for i in range(n):
        for j in range(b):
            profit+=vj[i]*x[i,j]
    return profit
```

Evolution Algorithm

The initial population are uniformly randomly generated. The population size is 10. The selection strategy is roulette wheel selection. The reproduction strategy is mutation only, 5 offsprings will be reproduced each iteration. The replacement strategy is generation replacement with elitism, only the best 10 among the 15 will make it to the next round.

```
In [59]:
```

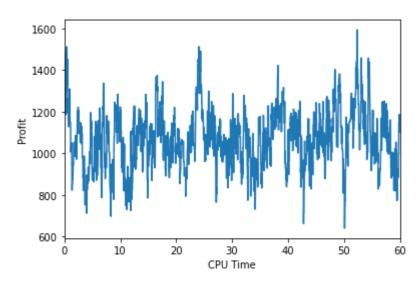
```
start=time.time()
#generate 10 initial solutions
population=[]
for i in range (10):
    a=generate solution(n, b)
    d=fix(a, c)
    population. append (d)
fitness_list=[]
for i in population:
    fit=fitness(i)
    fitness list.append(fit)
end=time.time()
time_list=[0]
value_list=[max(fitness_list)]
while end-start<60:
    #roulette wheel selection
    fitness list=[]
    for i in population:
        fit=fitness(i)
        fitness_list.append(fit)
    k=sum(fitness list)
    for i in range (len (fitness list)):
        j=fitness_list[i]/k
        fitness list[i]=j
    z=sum(fitness_list[0:9])
    fitness_1ist[-1]=1-z
    chosen=np. random. choice (np. arange (10), size=5, replace=False, p=fitness_list)
    #mutation
    for i in range (len (chosen)):
        j=mutation(population[chosen[i]])
        k=fix(j,c)
        population. append(k)
    #select the best 10 to next iteration
    dict={}
    for i in range(len(population)):
        fit=fitness(population[i])
        dict[i]=fit
    list1=sorted(dict.items(), key=lambda x:x[1])
    list2=[]
    for i in list1:
        list2.append(i[0])
    new pop=[]
    for i in range (5, len(list2)):
        new pop. append(population[list2[i]])
    best val=list1[-1][1]
    population=copy.deepcopy(new pop)
    end=time.time()
    time list.append(end-start)
    value list.append(best val)
dict={}
for i in range(len(population)):
    fit=fitness(population[i])
    dict[i]=fit
list1=sorted(dict.items(), key=lambda x:x[1])
print(final table(population[list1[-1][0]]))
```

```
plt.xlabel('CPU Time')
plt.ylabel('Profit')
plt.xlim((0,60))
plt.plot(time_list, value_list)
```

```
Container
                           Packages
                                      Profit Weight
0
                                         296
          1
              [13, 27, 29, 41, 82]
                                                  37
1
          2
                  [55, 66, 76, 96]
                                         243
                                                  46
2
          3
                   [6, 33, 40, 57]
                                         118
                                                  46
3
          4
                       [24, 34, 72]
                                         107
                                                  36
          5
               [5, 15, 68, 69, 80]
4
                                         338
                                                  43
5
      Total
                                        1102
```

Out[59]:

[<matplotlib.lines.Line2D at 0x1e97dc95970>]



Exercise 2

Crossover

The crossover here is uniform crossover with p=0.5, which is randomly select the arrangement of each item from both parent.

In [60]:

```
#input: x,y-two feasible arrangements act as parents
#output: result-the offspring
def crossover(x,y):
    n, b=x. shape
    result=np. zeros((n,b))
    for i in range(n):
        a=random.randint(0,1)
        if a==0:
            for j in range(b):
                result[i, j]=x[i, j]
        else:
            for j in range(b):
                result[i, j]=y[i, j]
        return result
```

The initial population are uniformly randomly generated. The population size is 10. The selection strategy is roulette wheel selection. The reproduction strategies are both mutation and crossover, 10 pairs of parents will

placement with elitism, only the best 10 among the 20 will make it to the next round.					

```
In [61]:
```

```
start=time.time()
#generate 10 initial solutions
population=[]
for i in range (10):
    a=generate solution(n, b)
    d=fix(a, c)
    population.append(d)
fitness_list=[]
for i in population:
    fit=fitness(i)
    fitness list.append(fit)
end=time.time()
time_list=[0]
value_list=[max(fitness_list)]
while end-start<60:
    #roulette wheel selection
    fitness list=[]
    for i in population:
        fit=fitness(i)
        fitness_list.append(fit)
    k=sum(fitness list)
    for i in range (len (fitness list)):
        j=fitness_list[i]/k
        fitness list[i]=j
    z=sum(fitness_list[0:9])
    fitness list[-1]=1-z
    chosen list=[]
    for i in range (10):
        chosen=np. random. choice (np. arange (10), size=2, replace=False, p=fitness_list)
        chosen_list.append(chosen)
    #crossover and mutation
    for i in chosen list:
        a=crossover(population[i[0]], population[i[1]])
        d=mutation(a)
        k=fix(d,c)
        population. append(k)
    #select the best 10 to next iteration
    dict={}
    for i in range (len (population)):
        fit=fitness(population[i])
        dict[i]=fit
    list1=sorted(dict.items(), key=lambda x:x[1])
    list2=[]
    for i in list1:
        list2.append(i[0])
    new pop=[]
    for i in range (10, len(list2)):
        new_pop. append (population[list2[i]])
    best val=list1[-1][1]
    population=copy.deepcopy(new pop)
    end=time.time()
    time_list.append(end-start)
    value_list.append(best_val)
dict={}
for i in range (len (population)):
```

```
fit=fitness(population[i])
    dict[i]=fit
list1=sorted(dict.items(), key=lambda x:x[1])
print(final_table(population[list1[-1][0]]))
plt.xlabel('CPU Time')
plt.ylabel('Profit')
plt.xlim((0,60))
plt.plot(time_list, value_list)
```

```
{\tt Container}
                                    Packages
                                               Profit Weight
0
                       [23, 47, 79, 82, 91]
                                                  397
1
              [18, 41, 51, 52, 69, 75, 80]
                                                  545
                                                           50
2
           3
                        [8, 42, 54, 93,
                                                           50
                                         96]
                                                  409
3
           4
                       [13, 53, 83, 86, 95]
                                                  438
                                                           47
4
           5
                  [19, 24, 29, 59, 63, 97]
                                                  420
                                                           50
5
      Total
                                                 2209
```

Out[61]:

[<matplotlib.lines.Line2D at 0x1e97c424970>]

