Consider the Fibonacci function, F(n) (see Proposition 3.20). Show by induction that F(n) is $\Omega((3/2)^n)$.

Lets find c and n_0 such that $F(n) \ge c(\frac{3}{2})^n$ for constant c and $n \ge n_0$. For $c = \frac{4}{9}$ and $n_0 = 1$ everything works great

$$\begin{array}{cccc}
n & F(n) & \frac{4}{9}(\frac{3}{2})^n \\
1 & 1 & \frac{2}{3} \\
2 & 1 & 1 \\
3 & 2 & \frac{3}{2} \\
4 & 3 & 2\frac{1}{4}
\end{array}$$

Inductive Hippotesis:

$$F(k) \ge c(\frac{3}{2})^k$$
, for some $k \ge n_0$

Lets schow that $F(k+1) \ge c(\frac{3}{2})^{k+1}$

$$F(k+1) = F(k) + F(k-1)$$

Lets apply out Hippotesis

$$\begin{split} F(k+1) &\geq c(\frac{3}{2})^k + c(\frac{3}{2})^{k-1} \\ &= c(\frac{3}{2})^{k-1} \cdot \frac{3}{2} + c(\frac{3}{2})^{k-1} \\ &= c(\frac{3}{2})^{k-1}(\frac{3}{2}+1) \\ &> c(\frac{3}{2})^{k-1}(\frac{3}{2})^2, \text{ since } \frac{5}{2} > \frac{9}{4} \\ &= c(\frac{3}{2})^{k+1} \end{split}$$