

何時給 project: April 26, 2017. 何時交 project: May 16, 2017 遲交不收，抄襲 0 分。

In multilayer perceptron model, use gradient descent method to solve the following problems:

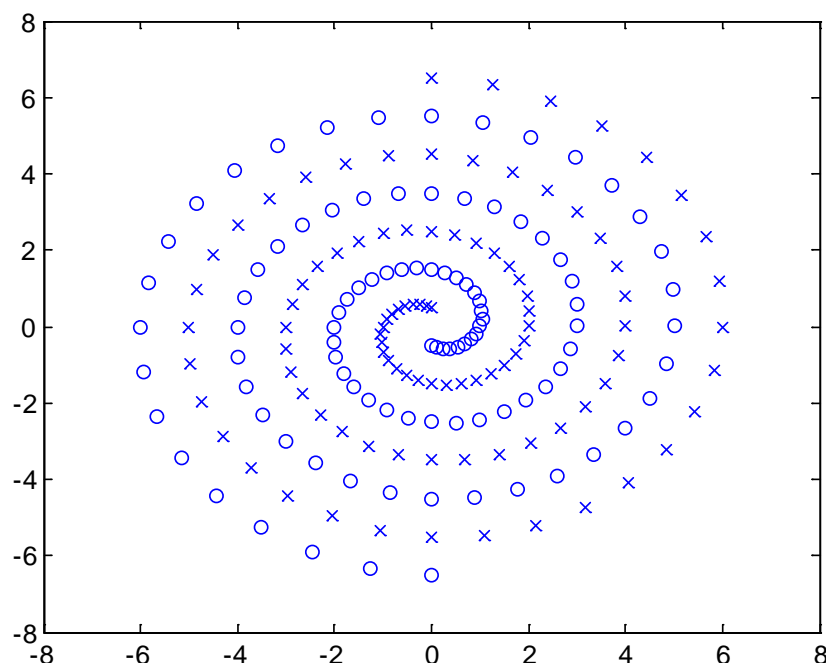
1. Two spiral problem:

$$(x_i, y_i) = (r_i \sin \theta_i, r_i \cos \theta_i) \in C_1, \text{ where } r_i = 6.5 \times \frac{(104 - i)}{104}, \theta_i = \frac{\pi}{16} i, i = 0, 1, 2, \dots, 96$$

$$(x_j, y_j) = (-r_j \sin \theta_j, -r_j \cos \theta_j) \in C_2, \text{ where}$$

$$r_j = 6.5 \times \frac{(104 - j)}{104}, \theta_j = \frac{\pi}{16} j, j = 0, 1, 2, \dots, 96$$

Desired output ( $d_1, d_2$ ) of  $C_1$  is (1, 0) and desired output of  $C_2$  is (0, 1).



Design a network to classify above 194 patterns into their corresponding two classes. That is, the number of hidden layers and hidden nodes is designed by you.

2. Double-moon problem:

Use the following scripts to generate data.

```
N=200;
theta1 = linspace(-180,180, N)*pi/360;

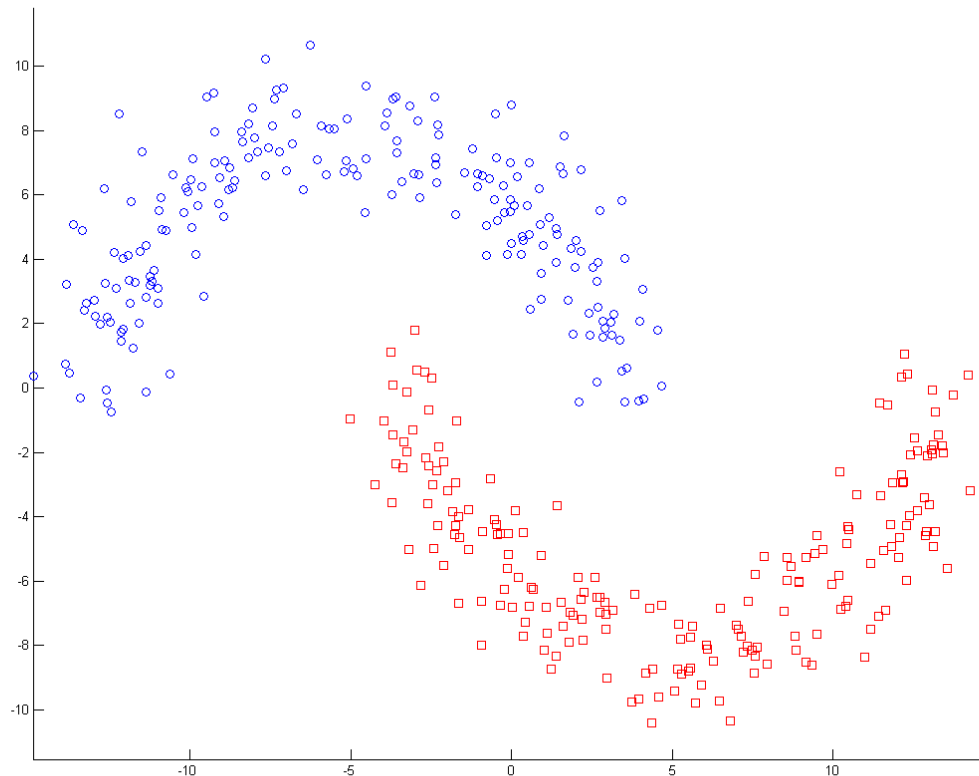
r = 8
x1 = -5 + r*sin(theta1)+randn(1,N);
y1 = r*cos(theta1)+randn(1,N);

x2 = 5 + r*sin(theta1)+randn(1,N);
y2 = -r*cos(theta1)+randn(1,N);
```

```
figure;
hold on;
axis equal;
plot(x1,y1,'bo');
plot(x2,y2,'rs');
```

Blue points are for class 1, and red points belong to class 2.

Design a network to classify above 400 patterns into their corresponding two classes.



3. Given 4 classes with Gaussian distribution:

$$M_1 = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \quad \Sigma_1 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \quad M_2 = \begin{bmatrix} 14 \\ 0 \end{bmatrix} \quad \Sigma_2 = \begin{bmatrix} 1 & 0 \\ 0 & 4 \end{bmatrix}, \quad M_3 = \begin{bmatrix} 7 \\ 14 \end{bmatrix} \quad \Sigma_3 = \begin{bmatrix} 4 & 0 \\ 0 & 1 \end{bmatrix},$$

$$M_4 = \begin{bmatrix} 7 \\ 7 \end{bmatrix} \quad \Sigma_4 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \quad \text{use multilayer perceptron to find the decision regions.}$$

For each problem:

Describe parameters of your network: number of hidden layers, number of hidden nodes, learning rate parameter ( $\eta$ ), stop criterion, ..., etc.

Plot the figure of average error vs. iteration,

Plot the decision region.

寫 MATLAB program 不要用 function。

## Discussion (10%)

How to determine the hidden node number in each problem? Describe in detail.

Describe any phenomenon you watched, any try to explain it if possible.

Any experiment like changing learning rate parameter, designing more layers, determining the hidden node number, or adding momentum term is greatly encouraged. 需要用到 high order inputs?

## References

### 要交的東西:

- (1) 在指定日的上課前，交紙本報告 (包含敘述如何做，flowchart，結果，討論，參考文獻，及 Matlab programs).
- (2) 將要交紙本報告的 doc file 及分開的 MATLAB program file 建成一個 directory (資料夾)，壓縮成 rar 檔後，上傳到 e3 system.

Directory name 的名稱: Proj#3\_姓名\_NN\_2017\_Spring。