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1 Esercizio 3.2

${\bf 1.1}\quad {\bf Calcolo~di~NULL,~FIRST~e~FOLLOW}$

	NULL	FIRST	FOLLOW
$\langle \text{prog} \rangle$		{ assign, print, read, for, if, { }	{ \$ }
$\langle statlist \rangle$		{ assign, print, read, for, if, { }	{ EOF, } }
$\langle statlistp \rangle$	x	<pre>(;)</pre>	{ EOF, } }
$\langle stat \rangle$		{ assign, print, read, for, if, { }	{ ;, else, end, EOF, } }
$\langle assignlist \rangle$		{[}	{ ;, else, end, EOF, } }
$\langle assignlistp \rangle$	X	{ [}	{ ;, else, end, EOF, } }
$\langle idlist \rangle$		{ ID }	{),] }
$\langle idlistp \rangle$	X	{ , }	{),] }
$\langle \text{bexpr} \rangle$		{ <, >, <=, >=, ==, <> }	{)}
$\langle \exp r \rangle$		(+, -, *, /, NUM, ID)	{ ,,;, to, +, -, *, /,), NUM, ID }
$\langle \text{exprlist} \rangle$		(+ -, *, /, NUM, ID)	{) }
$\langle \text{exprlistp} \rangle$	X	{ , }	{) }

1.2 Calcolo degli insiemi GUIDA

```
GUIDA(\langle prog \rangle \rightarrow \langle statlist \rangle EOF)
                                                                                                                                                                { assign, print, read, for, if, { }
GUIDA(\langle statlist \rangle \rightarrow \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                                { assign, print, read, for, if, { }
GUIDA(\langle statlistp \rangle \rightarrow ; \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                                {;}
GUIDA(\langle statlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                                { EOF, } }
GUIDA(\langle stat \rangle \rightarrow assign \langle assignlist \rangle)
                                                                                                                                                                { assign }
GUIDA(\langle stat \rangle \rightarrow print (\langle assignlist \rangle))
                                                                                                                                                                { print }
GUIDA(\langle stat \rangle \rightarrow read (\langle idlist \rangle))
                                                                                                                                                                 { read }
GUIDA(\langle stat \rangle \rightarrow for (ID := \langle expr \rangle ; \langle bexpr \rangle) do \langle stat \rangle)
                                                                                                                                                                { for }
GUIDA(\langle stat \rangle \rightarrow for (\langle bexpr \rangle) do \langle stat \rangle)
                                                                                                                                                                { for }
\mathrm{GUIDA}(\langle stat \rangle \to \mathtt{if} \ (\ \langle bexpr \rangle \ ) \ \langle stat \rangle \ \mathtt{else} \ \langle stat \rangle \ \mathtt{end})
                                                                                                                                                                { if }
GUIDA(\langle stat \rangle \rightarrow if \ (\langle bexpr \rangle) \ \langle stat \rangle \ end)
                                                                                                                                                                { if }
GUIDA(\langle stat \rangle \rightarrow \{ \langle statlist \rangle \})
                                                                                                                                                                { }
GUIDA(\langle assignlist \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                                {[]}
GUIDA(\langle assignlistp \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                                {[]}
GUIDA(\langle assignlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                                { ;, else, end, EOF, } }
GUIDA(\langle idlist \rangle \rightarrow ID \langle idlistp \rangle)
                                                                                                                                                                { ID }
\mathrm{GUIDA}(\langle idlistp \rangle \rightarrow , \mathrm{ID} \langle idlistp \rangle)
                                                                                                                                                                { , }
                                                                                                                                                                { ), ] }
GUIDA(\langle idlistp \rangle \to \varepsilon)
GUIDA(\langle bexpr \rangle \rightarrow \langle \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                { < }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                { > }
                                                                                                                                                                 { <= }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                { <= }
GUIDA(\langle bexpr \rangle \rightarrow == \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                    ==
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 { <> }
GUIDA(\langle expr \rangle \rightarrow + (\langle exprlist \rangle))
                                                                                                                                                                \(\) - \(\)
GUIDA(\langle expr \rangle \to \neg \langle expr \rangle \langle expr \rangle)
GUIDA(\langle expr \rangle \rightarrow * (\langle exprlist \rangle))
                                                                                                                                                                { * }
GUIDA(\langle expr \rangle \rightarrow / \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                {/}
GUIDA(\langle expr \rangle \rightarrow NUM)
                                                                                                                                                                { NUM }
GUIDA(\langle expr \rangle \rightarrow ID)
                                                                                                                                                                { ID }
GUIDA(\langle exprlist \rangle \rightarrow \langle expr \rangle \langle exprlistp \rangle)
                                                                                                                                                                { +, -, *, /, NUM, ID }
\mathrm{GUIDA}(\langle exprlistp \rangle \rightarrow , \langle expr \rangle \rightarrow \langle exprlistp \rangle)
                                                                                                                                                                { , }
{ ) }
GUIDA(\langle exprlistp \rangle \rightarrow \varepsilon)
```

1.3 Trasformazione in una grammatica LL(1) equivalente

La grammatica data non è LL(1) per via dei seguenti insiemi guida per la variabile $\langle stat \rangle$.

1.3.1 Produzione per for

Dati gli insiemi guida non LL(1) della grammatica per for:

$\overline{\mathrm{GUIDA}(\langle stat \rangle \to \mathtt{for} \ (\ \mathtt{ID} := \langle expr \rangle \ ; \ \langle bexpr \rangle \) \ \mathtt{do} \ \langle stat \rangle)}$	{ for }
$\mathrm{GUIDA}(\langle stat angle ightarrow \mathtt{for}$ ($\langle bexpr angle$) do $\langle stat angle)$	$\{ \ for \ \}$

Fattorizzando la parte <u>non</u> comune ad ambo le produzioni introducendo una variabile $\langle statc \rangle$, otteniamo un nuovo insieme guida per $\langle stat \rangle$ che risulta essere LL(1):

$$\begin{split} & \text{GUIDA}(\langle stat \rangle \rightarrow \text{for } (\ \langle statc \rangle \ \langle bexpr \rangle \) \ \text{do} \ \langle stat \rangle) \\ & \text{GUIDA}(\langle statc \rangle \rightarrow \text{ID} := \langle expr \rangle \ ;) \\ & \text{GUIDA}(\langle statc \rangle \rightarrow \varepsilon \\ & \text{GUIDA}(\langle statc \rangle \rightarrow \varepsilon \\ \end{split}$$

1.3.2 Produzione per if

Dati gli insiemi guida non LL(1) della grammatica per if:

$\overline{ ext{GUIDA}(\langle stat angle ightarrow ext{if } (\langle bexpr angle) \langle stat angle ext{ else } \langle stat angle ext{ end})}$	{ if }
$\mathrm{GUIDA}(\langle stat angle ightarrow \mathtt{if}$ ($\langle bexpr angle$) $\langle stat angle$ end)	{ if }

Fattorizzando la parte <u>non</u> comune ad ambo le produzioni introducendo una variabile $\langle statc \rangle$, otteniamo un nuovo insieme guida per $\langle stat \rangle$ che risulta essere LL(1):

$$\begin{split} & \text{GUIDA}(\langle stat \rangle \to \text{if } (\ \langle bexpr \rangle \) \ \langle stat \rangle \langle statp \rangle \ \text{end}) \\ & \text{GUIDA}(\langle statp \rangle \to \text{else} \ \langle stat \rangle) \\ & \text{GUIDA}(\langle statp \rangle \to \varepsilon) \end{split} \qquad \qquad \left\{ \begin{array}{l} \text{if } \} \\ & \text{else} \ \} \\ & \text{end} \ \} \end{split}$$

1.4 Grammatica LL(1) completa

```
GUIDA(\langle prog \rangle \rightarrow \langle statlist \rangle EOF)
                                                                                                                                                            { assign, print, read, for, if, { }
GUIDA(\langle statlist \rangle \rightarrow \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                            { assign, print, read, for, if, { }
GUIDA(\langle statlistp \rangle \rightarrow ; \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                            {;}
GUIDA(\langle statlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                            { EOF, } }
GUIDA(\langle stat \rangle \rightarrow assign \langle assignlist \rangle)
                                                                                                                                                            { assign }
GUIDA(\langle stat \rangle \rightarrow print (\langle assignlist \rangle))
                                                                                                                                                            { print }
GUIDA(\langle stat \rangle \rightarrow read (\langle idlist \rangle))
                                                                                                                                                            { read }
GUIDA(\langle stat \rangle \rightarrow for (\langle statc \rangle \langle bexpr \rangle) do \langle stat \rangle)
                                                                                                                                                            { for }
GUIDA(\langle stat \rangle \rightarrow if \ (\langle bexpr \rangle) \ \langle stat \rangle \langle statp \rangle \ end)
                                                                                                                                                            { if }
GUIDA(\langle stat \rangle \rightarrow \{ \langle statlist \rangle \})
                                                                                                                                                            { }
GUIDA(\langle statc \rangle \rightarrow ID := \langle expr \rangle;)
                                                                                                                                                            { <, >, <=, >=, ==, <> }
GUIDA(\langle statc \rangle \to \varepsilon)
GUIDA(\langle statp \rangle \rightarrow else \langle stat \rangle)
                                                                                                                                                            { else }
GUIDA(\langle statp \rangle \to \varepsilon)
                                                                                                                                                            { end }
GUIDA(\langle assignlist \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                            { [ ]
GUIDA(\langle assignlistp \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                            { [ }
GUIDA(\langle assignlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                            { ;, else, end, EOF, } }
GUIDA(\langle idlist \rangle \rightarrow ID \langle idlistp \rangle)
                                                                                                                                                            { ID }
                                                                                                                                                            { , }
{ ), ] }
GUIDA(\langle idlistp \rangle \rightarrow , ID \langle idlistp \rangle)
GUIDA(\langle idlistp \rangle \to \varepsilon)
GUIDA(\langle bexpr \rangle \to \langle \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { < }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { > }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { <= }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { <= }
GUIDA(\langle bexpr \rangle \rightarrow == \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { == }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { <> }
GUIDA(\langle expr \rangle \rightarrow + (\langle exprlist \rangle))
                                                                                                                                                            { + }
\mathrm{GUIDA}(\langle expr\rangle \to \neg \langle expr\rangle \langle expr\rangle)
                                                                                                                                                            { - }
                                                                                                                                                            { * }
GUIDA(\langle expr \rangle \rightarrow * (\langle exprlist \rangle))
GUIDA(\langle expr \rangle \rightarrow / \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { / }
GUIDA(\langle expr \rangle \rightarrow NUM)
                                                                                                                                                            { NUM }
GUIDA(\langle expr \rangle \rightarrow ID)
                                                                                                                                                            { ID }
                                                                                                                                                            { +, -, *, /, NUM, ID }
GUIDA(\langle exprlist \rangle \rightarrow \langle expr \rangle \langle exprlistp \rangle)
GUIDA(\langle exprlistp \rangle \rightarrow , \langle expr \rangle \rightarrow \langle exprlistp \rangle)
                                                                                                                                                            { , }
GUIDA(\langle exprlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                            { ) }
```