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# 1 Esercizio 3.2

## ${\bf 1.1}\quad {\bf Calcolo~di~NULL,~FIRST~e~FOLLOW}$

	NULL	FIRST	FOLLOW
$\langle \text{prog} \rangle$		{ assign, print, read, for, if, { }	{ \$ }
$\langle statlist \rangle$		{ assign, print, read, for, if, { }	{ EOF, } }
$\langle statlistp \rangle$	x	<pre>(;)</pre>	{ EOF, } }
$\langle stat \rangle$		{ assign, print, read, for, if, { }	{ ;, else, end, EOF, } }
$\langle assignlist \rangle$		{[}	{ ;, else, end, EOF, } }
$\langle assignlistp \rangle$	X	{ [ }	{ ;, else, end, EOF, } }
$\langle idlist \rangle$		{ ID }	{ ), ] }
$\langle idlistp \rangle$	X	{ , }	{ ), ] }
$\langle \text{bexpr} \rangle$		{ <, >, <=, >=, ==, <> }	{)}
$\langle \exp r \rangle$		( +, -, *, /, NUM, ID )	{ ,,;, to, +, -, *, /, ), NUM, ID }
$\langle \text{exprlist} \rangle$		{ +, -, *, /, NUM, ID }	{ ) }
$\langle \text{exprlistp} \rangle$	X	{ , }	{ ) }

### 1.2 Calcolo degli insiemi GUIDA

```
GUIDA(\langle prog \rangle \rightarrow \langle statlist \rangle EOF)
                                                                                                                                                                 { assign, print, read, for, if, { }
GUIDA(\langle statlist \rangle \rightarrow \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                                 { assign, print, read, for, if, { }
GUIDA(\langle statlistp \rangle \rightarrow ; \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                                 {;}
GUIDA(\langle statlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                                 { EOF, } }
GUIDA(\langle stat \rangle \rightarrow assign \langle assignlist \rangle)
                                                                                                                                                                 { assign }
GUIDA(\langle stat \rangle \rightarrow print (\langle exprlist \rangle))
                                                                                                                                                                 { print }
GUIDA(\langle stat \rangle \rightarrow read (\langle idlist \rangle))
                                                                                                                                                                 { read }
GUIDA(\langle stat \rangle \rightarrow for (ID := \langle expr \rangle ; \langle bexpr \rangle) do \langle stat \rangle)
                                                                                                                                                                 { for }
GUIDA(\langle stat \rangle \rightarrow for (\langle bexpr \rangle) do \langle stat \rangle)
                                                                                                                                                                 { for }
\mathrm{GUIDA}(\langle stat \rangle \to \mathtt{if} \ (\ \langle bexpr \rangle \ ) \ \langle stat \rangle \ \mathtt{else} \ \langle stat \rangle \ \mathtt{end})
                                                                                                                                                                 { if }
GUIDA(\langle stat \rangle \rightarrow if \ (\langle bexpr \rangle) \ \langle stat \rangle \ end)
                                                                                                                                                                 { if }
GUIDA(\langle stat \rangle \rightarrow \{ \langle statlist \rangle \})
                                                                                                                                                                 { }
GUIDA(\langle assignlist \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                                 {[]}
GUIDA(\langle assignlistp \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                                 {[]}
GUIDA(\langle assignlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                                 { ;, else, end, EOF, } }
GUIDA(\langle idlist \rangle \rightarrow ID \langle idlistp \rangle)
                                                                                                                                                                 { ID }
\mathrm{GUIDA}(\langle idlistp \rangle \rightarrow , \mathrm{ID} \langle idlistp \rangle)
                                                                                                                                                                 { , }
                                                                                                                                                                 { ), ] }
GUIDA(\langle idlistp \rangle \to \varepsilon)
GUIDA(\langle bexpr \rangle \rightarrow \langle \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 { < }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 { > }
                                                                                                                                                                 { <= }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 { <= }
GUIDA(\langle bexpr \rangle \rightarrow == \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                    ==
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 { <> }
GUIDA(\langle expr \rangle \rightarrow + (\langle exprlist \rangle))
                                                                                                                                                                 \(\) - \(\)
GUIDA(\langle expr \rangle \to \neg \langle expr \rangle \langle expr \rangle)
GUIDA(\langle expr \rangle \rightarrow * (\langle exprlist \rangle))
                                                                                                                                                                 { * }
GUIDA(\langle expr \rangle \rightarrow / \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 {/}
GUIDA(\langle expr \rangle \rightarrow NUM)
                                                                                                                                                                 { NUM }
GUIDA(\langle expr \rangle \rightarrow ID)
                                                                                                                                                                 { ID }
GUIDA(\langle exprlist \rangle \rightarrow \langle expr \rangle \langle exprlistp \rangle)
                                                                                                                                                                 { +, -, *, /, NUM, ID }
\mathrm{GUIDA}(\langle exprlistp \rangle \rightarrow , \langle expr \rangle \rightarrow \langle exprlistp \rangle)
                                                                                                                                                                 { , }
{ ) }
GUIDA(\langle exprlistp \rangle \rightarrow \varepsilon)
```

## 1.3 Trasformazione in una grammatica LL(1) equivalente

La grammatica data non è LL(1) per via dei seguenti insiemi guida per la variabile  $\langle stat \rangle$ .

### 1.3.1 Produzione per for

Dati gli insiemi guida non LL(1) della grammatica per for:

```
\begin{array}{l} \overline{\mathrm{GUIDA}(\langle stat \rangle \to \mathtt{for} \; (\; \mathtt{ID} := \langle expr \rangle \; ; \; \langle bexpr \rangle \; ) \; \mathtt{do} \; \langle stat \rangle)} & \qquad \qquad \{ \; \mathtt{for} \; \} \\ \overline{\mathrm{GUIDA}(\langle stat \rangle \to \mathtt{for} \; (\; \langle bexpr \rangle \; ) \; \mathtt{do} \; \langle stat \rangle)} & \qquad \qquad \{ \; \mathtt{for} \; \} \\ \end{array}
```

Fattorizzando la parte <u>non</u> comune ad ambo le produzioni introducendo una variabile  $\langle statc \rangle$ , otteniamo un nuovo insieme guida per  $\langle stat \rangle$  che risulta essere LL(1):

```
\begin{split} & \text{GUIDA}(\langle stat \rangle \rightarrow \text{for (} \langle statc \rangle \ \langle bexpr \rangle \ ) \ \text{do } \langle stat \rangle) \\ & \text{GUIDA}(\langle statc \rangle \rightarrow \text{ID := } \langle expr \rangle \ ;) \\ & \text{GUIDA}(\langle statc \rangle \rightarrow \varepsilon \\ & \text{ } \{ \text{ ror } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text{ } \{ \text{ constant } \} \\ & \text
```

### 1.3.2 Produzione per if

Dati gli insiemi guida non LL(1) della grammatica per if:

$\overline{ ext{GUIDA}(\langle stat  angle  ightarrow  ext{if } (\langle bexpr  angle ) \langle stat  angle  ext{ else } \langle stat  angle  ext{ end)}}$	{ if }
$\mathrm{GUIDA}(\langle stat  angle  ightarrow \mathtt{if}$ ( $\langle bexpr  angle$ ) $\langle stat  angle$ end)	$\{ \ \mathtt{if} \ \}$

Fattorizzando la parte <u>non</u> comune ad ambo le produzioni introducendo una variabile  $\langle statp \rangle$ , otteniamo un nuovo insieme guida per  $\langle stat \rangle$  che risulta essere LL(1):

```
\begin{split} & \text{GUIDA}(\langle stat \rangle \to \text{if (} \langle bexpr \rangle \text{ ) } \langle stat \rangle \langle statp \rangle \text{ end)} & \text{ { if } } \} \\ & \text{GUIDA}(\langle statp \rangle \to \text{else } \langle stat \rangle) & \text{ { else } } \} \\ & \text{GUIDA}(\langle statp \rangle \to \varepsilon) & \text{ { end } } \} \end{split}
```

## 1.4 Grammatica LL(1) equivalente

#### 1.4.1 Calcolo di NULL, FIRST e FOLLOW

	NULL	FIRST	FOLLOW
$\overline{\langle \text{prog} \rangle}$		{ assign, print, read, for, if, { }	{ \$ }
$\langle statlist \rangle$		{ assign, print, read, for, if, { }	{ EOF, } }
$\langle statlistp \rangle$	X	{;}	{ EOF, } }
$\langle \text{stat} \rangle$		{ assign, print, read, for, if, { }	{ ;, else, end, EOF, } }
$\langle statc \rangle$	X	{ ID }	{ <, >, <=, >=, ==, <> }
$\langle \text{statp} \rangle$	X	{ else }	$\{ \ \mathtt{end} \ \}$
$\langle assignlist \rangle$		[]	{ ;, else, end, EOF, } }
$\langle assignlistp \rangle$	X	{ [ }	{ ;, else, end, EOF, } }
$\langle idlist \rangle$		{ ID }	{ ), ] }
$\langle idlistp \rangle$	X	{ , }	{ ), ] }
$\langle \text{bexpr} \rangle$		{ <, >, <=, >=, ==, <> }	{)}
$\langle \exp r \rangle$		(+, -, *, /, NUM, ID )	{ ,,;, to, +, -, *, /, ), NUM, ID }
$\langle \text{exprlist} \rangle$		{ +, -, *, /, NUM, ID }	{ ) }
$\langle \text{exprlistp} \rangle$	X	{ , }	{ ) }

#### 1.4.2 Calcolo degli insiemi GUIDA

```
{ assign, print, read, for, if, { }
GUIDA(\langle prog \rangle \rightarrow \langle statlist \rangle EOF)
GUIDA(\langle statlist \rangle \rightarrow \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                              { assign, print, read, for, if, { }
GUIDA(\langle statlistp \rangle \rightarrow ; \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                              {;}
\text{GUIDA}(\langle statlistp \rangle \to \varepsilon)
                                                                                                                                                              { EOF, } }
GUIDA(\langle stat \rangle \rightarrow assign \langle assignlist \rangle)
                                                                                                                                                              { assign }
GUIDA(\langle stat \rangle \rightarrow print (\langle exprlist \rangle))
                                                                                                                                                              { print }
\mathrm{GUIDA}(\langle stat \rangle \to \mathtt{read} \ (\ \langle idlist \rangle \ ) \ )
                                                                                                                                                              { read }
GUIDA(\langle stat \rangle \rightarrow for (\langle statc \rangle \langle bexpr \rangle) do \langle stat \rangle)
                                                                                                                                                              { for }
GUIDA(\langle stat \rangle \rightarrow if \ (\langle bexpr \rangle) \ \langle stat \rangle \langle statp \rangle \ end)
                                                                                                                                                              { if }
GUIDA(\langle stat \rangle \rightarrow \{ \langle statlist \rangle \})
                                                                                                                                                              { } }
GUIDA(\langle statc \rangle \rightarrow ID := \langle expr \rangle ;)
                                                                                                                                                              { ID }
                                                                                                                                                              ( <, >, <=, >=, ==, <> )
GUIDA(\langle statc \rangle \rightarrow \varepsilon)
GUIDA(\langle statp \rangle \rightarrow else \langle stat \rangle)
                                                                                                                                                              { else }
GUIDA(\langle statp \rangle \to \varepsilon)
                                                                                                                                                              { end }
GUIDA(\langle assignlist \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                              { [ ]
GUIDA(\langle assignlistp \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                              { [ }
GUIDA(\langle assignlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                              { ;, else, end, EOF, } }
GUIDA(\langle idlist \rangle \rightarrow ID \langle idlistp \rangle)
                                                                                                                                                              { ID }
GUIDA(\langle idlistp \rangle \rightarrow , ID \langle idlistp \rangle)
                                                                                                                                                              { , }
{ ), ] }
GUIDA(\langle idlistp \rangle \to \varepsilon)
GUIDA(\langle bexpr \rangle \rightarrow \langle \langle expr \rangle \langle expr \rangle)
                                                                                                                                                              { < }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                              { > }
                                                                                                                                                              { <= }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
GUIDA(\langle bexpr \rangle \rightarrow \mathsf{<=} \langle expr \rangle \langle expr \rangle)
                                                                                                                                                              { <= }
                                                                                                                                                              { == }
GUIDA(\langle bexpr \rangle \rightarrow == \langle expr \rangle \langle expr \rangle)
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                              { <> }
GUIDA(\langle expr \rangle \rightarrow + (\langle exprlist \rangle))
                                                                                                                                                              { + }
\text{GUIDA}(\langle expr \rangle \to \neg \langle expr \rangle \langle expr \rangle)
                                                                                                                                                              { - }
                                                                                                                                                              { * }
GUIDA(\langle expr \rangle \rightarrow * (\langle exprlist \rangle))
GUIDA(\langle expr \rangle \rightarrow / \langle expr \rangle \langle expr \rangle)
                                                                                                                                                              { / }
GUIDA(\langle expr \rangle \rightarrow NUM)
                                                                                                                                                              { NUM }
GUIDA(\langle expr \rangle \rightarrow ID)
                                                                                                                                                              { ID }
GUIDA(\langle exprlist \rangle \to \langle expr \rangle \langle exprlistp \rangle)
                                                                                                                                                              { +, -, *, /, NUM, ID }
GUIDA(\langle exprlistp \rangle \rightarrow , \langle expr \rangle \langle exprlistp \rangle)
                                                                                                                                                             { , }
GUIDA(\langle exprlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                              { ) }
```