## Contents

1	Ese	rcizio 3.2	1
	1.1	Calcolo di NULL, FIRST e FOLLOW	1
	1.2	Calcolo degli insiemi GUIDA	2
	1.3	Trasformazione in una grammatica LL(1) equivalente	3
		1.3.1 Produzione per for	3
		1.3.2 Produzione per if	3
	1.4	Grammatica LL(1) completa	4

# 1 Esercizio 3.2

## ${\bf 1.1}\quad {\bf Calcolo~di~NULL,~FIRST~e~FOLLOW}$

	NULL	FIRST	FOLLOW
$\langle \text{prog} \rangle$		{ assign, print, read, for, if, { }	{ \$ }
$\langle statlist \rangle$		{ assign, print, read, for, if, { }	{ EOF, } }
$\langle statlistp \rangle$	x	<pre>(;)</pre>	{ EOF, } }
$\langle stat \rangle$		{ assign, print, read, for, if, { }	{ ;, else, end, EOF, } }
$\langle assignlist \rangle$		{[}	{ ;, else, end, EOF, } }
$\langle assignlistp \rangle$	X	{ [ }	{ ;, else, end, EOF, } }
$\langle idlist \rangle$		{ ID }	{ ), ] }
$\langle idlistp \rangle$	X	{ , }	{ ), ] }
$\langle \text{bexpr} \rangle$		{ <, >, <=, >=, ==, <> }	{)}
$\langle \exp r \rangle$		( +, -, *, /, NUM, ID )	{ ,,;, to, +, -, *, /, ), NUM, ID }
$\langle \text{exprlist} \rangle$		( + -, *, /, NUM, ID )	{ ) }
$\langle \text{exprlistp} \rangle$	X	{ , }	{ ) }

#### 1.2 Calcolo degli insiemi GUIDA

```
GUIDA(\langle prog \rangle \rightarrow \langle statlist \rangle EOF)
                                                                                                                                                                 { assign, print, read, for, if, { }
GUIDA(\langle statlist \rangle \rightarrow \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                                 { assign, print, read, for, if, { }
GUIDA(\langle statlistp \rangle \rightarrow ; \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                                 {;}
GUIDA(\langle statlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                                 { EOF, } }
GUIDA(\langle stat \rangle \rightarrow assign \langle assignlist \rangle)
                                                                                                                                                                 { assign }
GUIDA(\langle stat \rangle \rightarrow print (\langle exprlist \rangle))
                                                                                                                                                                 { print }
GUIDA(\langle stat \rangle \rightarrow read (\langle idlist \rangle))
                                                                                                                                                                 { read }
GUIDA(\langle stat \rangle \rightarrow for (ID := \langle expr \rangle ; \langle bexpr \rangle) do \langle stat \rangle)
                                                                                                                                                                 { for }
GUIDA(\langle stat \rangle \rightarrow for (\langle bexpr \rangle) do \langle stat \rangle)
                                                                                                                                                                 { for }
\mathrm{GUIDA}(\langle stat \rangle \to \mathtt{if} \ (\ \langle bexpr \rangle \ ) \ \langle stat \rangle \ \mathtt{else} \ \langle stat \rangle \ \mathtt{end})
                                                                                                                                                                 { if }
GUIDA(\langle stat \rangle \rightarrow if \ (\langle bexpr \rangle) \ \langle stat \rangle \ end)
                                                                                                                                                                 { if }
GUIDA(\langle stat \rangle \rightarrow \{ \langle statlist \rangle \})
                                                                                                                                                                 { }
GUIDA(\langle assignlist \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                                 {[]}
GUIDA(\langle assignlistp \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                                 {[]}
GUIDA(\langle assignlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                                 { ;, else, end, EOF, } }
GUIDA(\langle idlist \rangle \rightarrow ID \langle idlistp \rangle)
                                                                                                                                                                 { ID }
\mathrm{GUIDA}(\langle idlistp \rangle \rightarrow , \mathrm{ID} \langle idlistp \rangle)
                                                                                                                                                                 { , }
                                                                                                                                                                 { ), ] }
GUIDA(\langle idlistp \rangle \to \varepsilon)
GUIDA(\langle bexpr \rangle \rightarrow \langle \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 { < }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 { > }
                                                                                                                                                                 { <= }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 { <= }
GUIDA(\langle bexpr \rangle \rightarrow == \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                    ==
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 { <> }
GUIDA(\langle expr \rangle \rightarrow + (\langle exprlist \rangle))
                                                                                                                                                                 \(\) - \(\)
GUIDA(\langle expr \rangle \to \neg \langle expr \rangle \langle expr \rangle)
GUIDA(\langle expr \rangle \rightarrow * (\langle exprlist \rangle))
                                                                                                                                                                 { * }
GUIDA(\langle expr \rangle \rightarrow / \langle expr \rangle \langle expr \rangle)
                                                                                                                                                                 {/}
GUIDA(\langle expr \rangle \rightarrow NUM)
                                                                                                                                                                 { NUM }
GUIDA(\langle expr \rangle \rightarrow ID)
                                                                                                                                                                 { ID }
GUIDA(\langle exprlist \rangle \rightarrow \langle expr \rangle \langle exprlistp \rangle)
                                                                                                                                                                 { +, -, *, /, NUM, ID }
\mathrm{GUIDA}(\langle exprlistp \rangle \rightarrow , \langle expr \rangle \rightarrow \langle exprlistp \rangle)
                                                                                                                                                                 { , }
{ ) }
GUIDA(\langle exprlistp \rangle \rightarrow \varepsilon)
```

## 1.3 Trasformazione in una grammatica LL(1) equivalente

La grammatica data non è LL(1) per via dei seguenti insiemi guida per la variabile  $\langle stat \rangle$ .

### 1.3.1 Produzione per for

Dati gli insiemi guida non LL(1) della grammatica per for:

$\overline{ ext{GUIDA}(\langle stat  angle  ightarrow  ext{for (ID := } \langle expr  angle  ext{ ; } \langle bexpr  angle  ext{ ) do } \langle stat  angle)}$	{ for }	
$\mathrm{GUIDA}(\langle stat  angle  ightarrow \mathtt{for}$ ( $\langle bexpr  angle$ ) do $\langle stat  angle)$	{ for }	

Fattorizzando la parte <u>non</u> comune ad ambo le produzioni introducendo una variabile  $\langle statc \rangle$ , otteniamo un nuovo insieme guida per  $\langle stat \rangle$  che risulta essere LL(1):

$$\begin{split} & \text{GUIDA}(\langle stat \rangle \rightarrow \text{for } (\ \langle statc \rangle \ \langle bexpr \rangle \ ) \ \text{do} \ \langle stat \rangle) \\ & \text{GUIDA}(\langle statc \rangle \rightarrow \text{ID} := \langle expr \rangle \ ;) \\ & \text{GUIDA}(\langle statc \rangle \rightarrow \varepsilon \\ & \text{GUIDA}(\langle statc \rangle \rightarrow \varepsilon \\ \end{split} \ \ \left\{ \begin{array}{l} \text{ID} \ \rbrace \\ \{ <, >, <=, >=, ==, <> \ \rbrace \\ \end{array} \right. \end{split}$$

## 1.3.2 Produzione per if

Dati gli insiemi guida non LL(1) della grammatica per if:

$\overline{ ext{GUIDA}(\langle stat  angle}  ightarrow  ext{if } (\langle bexpr  angle ) \langle stat  angle  ext{ else } \langle stat  angle  ext{ end})$	{ if }
$\mathrm{GUIDA}(\langle stat  angle  ightarrow \mathtt{if}$ ( $\langle bexpr  angle$ ) $\langle stat  angle$ end)	$\{ \ \mathtt{if} \ \}$

Fattorizzando la parte <u>non</u> comune ad ambo le produzioni introducendo una variabile  $\langle statp \rangle$ , otteniamo un nuovo insieme guida per  $\langle stat \rangle$  che risulta essere LL(1):

$$\begin{split} & \text{GUIDA}(\langle stat \rangle \to \text{if } (\ \langle bexpr \rangle \ ) \ \langle stat \rangle \langle statp \rangle \ \text{end}) \\ & \text{GUIDA}(\langle statp \rangle \to \text{else} \ \langle stat \rangle) \\ & \text{GUIDA}(\langle statp \rangle \to \varepsilon) \end{split} \qquad \qquad \left\{ \begin{array}{l} \text{if } \} \\ & \text{else} \ \} \\ & \text{end} \ \right\} \end{split}$$

#### 1.4 Grammatica LL(1) completa

```
GUIDA(\langle prog \rangle \rightarrow \langle statlist \rangle EOF)
                                                                                                                                                            { assign, print, read, for, if, { }
GUIDA(\langle statlist \rangle \rightarrow \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                            { assign, print, read, for, if, { }
GUIDA(\langle statlistp \rangle \rightarrow ; \langle stat \rangle \langle statlistp \rangle)
                                                                                                                                                            {;}
GUIDA(\langle statlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                            { EOF, } }
GUIDA(\langle stat \rangle \rightarrow assign \langle assignlist \rangle)
                                                                                                                                                            { assign }
GUIDA(\langle stat \rangle \rightarrow print (\langle exprlist \rangle))
                                                                                                                                                            { print }
GUIDA(\langle stat \rangle \rightarrow read (\langle idlist \rangle))
                                                                                                                                                            { read }
GUIDA(\langle stat \rangle \rightarrow for (\langle statc \rangle \langle bexpr \rangle) do \langle stat \rangle)
                                                                                                                                                            { for }
GUIDA(\langle stat \rangle \rightarrow if \ (\langle bexpr \rangle) \ \langle stat \rangle \langle statp \rangle \ end)
                                                                                                                                                            { if }
GUIDA(\langle stat \rangle \rightarrow \{ \langle statlist \rangle \})
                                                                                                                                                            { }
GUIDA(\langle statc \rangle \rightarrow ID := \langle expr \rangle;)
                                                                                                                                                            { <, >, <=, >=, ==, <> }
GUIDA(\langle statc \rangle \to \varepsilon)
GUIDA(\langle statp \rangle \rightarrow else \langle stat \rangle)
                                                                                                                                                            { else }
GUIDA(\langle statp \rangle \to \varepsilon)
                                                                                                                                                            { end }
GUIDA(\langle assignlist \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                            { [ ]
GUIDA(\langle assignlistp \rangle \rightarrow [\langle expr \rangle \text{ to } \langle idlist \rangle] \langle assignlistp \rangle)
                                                                                                                                                            { [ }
GUIDA(\langle assignlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                            { ;, else, end, EOF, } }
GUIDA(\langle idlist \rangle \rightarrow ID \langle idlistp \rangle)
                                                                                                                                                            { ID }
                                                                                                                                                            { , }
{ ), ] }
GUIDA(\langle idlistp \rangle \rightarrow , ID \langle idlistp \rangle)
GUIDA(\langle idlistp \rangle \to \varepsilon)
GUIDA(\langle bexpr \rangle \to \langle \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { < }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { > }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { <= }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { <= }
GUIDA(\langle bexpr \rangle \rightarrow == \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { == }
GUIDA(\langle bexpr \rangle \rightarrow \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { <> }
GUIDA(\langle expr \rangle \rightarrow + (\langle exprlist \rangle))
                                                                                                                                                            { + }
\mathrm{GUIDA}(\langle expr\rangle \to \neg \langle expr\rangle \langle expr\rangle)
                                                                                                                                                            { - }
                                                                                                                                                            { * }
GUIDA(\langle expr \rangle \rightarrow * (\langle exprlist \rangle))
GUIDA(\langle expr \rangle \rightarrow / \langle expr \rangle \langle expr \rangle)
                                                                                                                                                            { / }
GUIDA(\langle expr \rangle \rightarrow NUM)
                                                                                                                                                            { NUM }
GUIDA(\langle expr \rangle \rightarrow ID)
                                                                                                                                                            { ID }
                                                                                                                                                           { +, -, *, /, NUM, ID }
GUIDA(\langle exprlist \rangle \rightarrow \langle expr \rangle \langle exprlistp \rangle)
GUIDA(\langle exprlistp \rangle \rightarrow , \langle expr \rangle \langle exprlistp \rangle)
                                                                                                                                                            { , }
GUIDA(\langle exprlistp \rangle \rightarrow \varepsilon)
                                                                                                                                                            { ) }
```