SGN-41007 Pattern Recognition and Machine Learning

Exercise Set 2: January 15 – 19, 2017

Exercises consist of both pen&paper and computer assignments. Pen&paper questions are solved at home before exercises, while computer assignments are solved during exercise hours. The computer assignments are marked by **pen&paper** and Pen&paper questions by **pen&paper**

1. **Pen&paper** Least squares fit. Two measurements x(n) and y(n) depend on each other in a linear manner, and there are the following measurements available:

$$\begin{array}{c|ccccc} n & 0 & 1 & 2 \\ \hline x(n) & 7 & 9 & 2 \\ y(n) & 11.6 & 14.8 & 3.5 \end{array}$$

We want to model the relationship between the two variables using the model:

$$y(n) = ax(n) + b.$$

Find the least squares estimates \hat{a} and \hat{b} that minimize the squared error.

2. **python** Least squares fit (like question 1 but with numpy). Download the following dataset onto your machine

http://www.cs.tut.fi/courses/SGN-41007/least_squares_data.zip

Extract the contents (two numpy arrays) and open in numpy (see numpy.load). We want to model the relationship between the two variables using the model:

$$y(n) = ax(n) + b.$$

Find the least squares estimates \hat{a} and \hat{b} that minimize the squared error.

3. **python** Same as last week (Moodle) Question 1, but without numpy.

Download the following file and extract the contents:

http://www.cs.tut.fi/courses/SGN-41007/exercises/locationData.zip

- a) Read the file into memory one line at a time (in a for loop). See similar example at the end of lecture slide set 1.
- b) Load the same data into another variable using numpy.loadtxt. Check that the contents of the two arrays are equal using numpy.all or numpy.any.

- 4. **python** Load Matlab data into Python.
 - a) Download the following file to your local folder:

```
http://www.cs.tut.fi/courses/SGN-41007/exercises/twoClassData.mat
```

b) Load the file contents into Python. This can be done as follows.

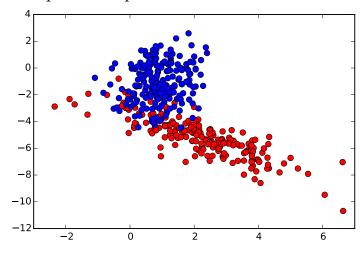
```
>>> from scipy.io import loadmat
>>> mat = loadmat("twoClassData.mat")
```

This generates a **dict** structure, whose elements can be accessed through their names.

```
>>> print(mat.keys()) # Which variables mat contains?
['y', 'X', '__version__', '__header__', '__globals__']
>>> X = mat["X"] # Collect the two variables.
>>> y = mat["y"].ravel()
```

The function ravel () transforms y from 400×1 matrix into a 400-length array. In Python these are different things unlike Matlab.

- c) The matrix X contains two-dimensional samples from two classes, as defined by y. Plot the data as a scatter plot like the picture below. Hints:
 - You can access all class 0 samples from X as: X [y == 0, :].
 - The samples can be plotted like: plt.plot(X[:, 0], X[:, 1], 'ro')



5. **python** Remove the uneven illumination from a microscope image using least squares fitting like we did at the lecture.

Download the following file to your local folder:

http://www.cs.tut.fi/courses/SGN-41007/exercises/uneven_illumination.jpg

Load the image into numpy array Z using the imread function of matplotlib.image¹. Finally, show the image on screen (using matplotlib.pyplot.imshow) and check that the image shape is 1300×1030 . Let's next fit a 2nd order surface to the grayscales.

- a) Create the explanatory variables (all x,y-coordinates in a matrix): X, Y = np.meshgrid(range(1300), range(1030))
- b) Vectorize the matrices X, Y, Z using ravel, e.g., z = Z.ravel().
- c) Prepare the design matrix H like in the lectures and solve the LS coefficients c.
- d) Compute the model prediction as z_pred = np.dot(H, c) and resize the vector to the original size.
- e) Subtract the model prediction from the original image and show the result on screen.



¹Note: There are several other ways of doing this, such as: matplotlib.image.imread, scipy.ndimage.imread, PIL.Image.open or cv2.imread