

A Physics-informed Neural Network modelling of a DC Motor



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What is a Physics-informed Neural Network (PINN)?

From my research studies, PINN is just your regular backpropagated neural network....

With the exception that the network's loss is not just a function of the error between the actual output and the predicted output....

The loss includes the residual losses which are derived your systems dynamic equations [1].

The inclusion of these residuals helps to ensure that any deviation of your network's output from the underlying physical law is penalized [2].

So why use PINN?

Physics-Informed Neural Network (PINN)

- Performs state (speed and current) and parameter estimation (resistance, inertia, etc) [1]
- Faster than conventional numerical solvers [2]
- Has higher accuracy and lesser computational costs than conventional numerical solvers [2]
- Exploits the underlying physical laws [1,2]

So let's have some fun and try it out to see how and if it truly works

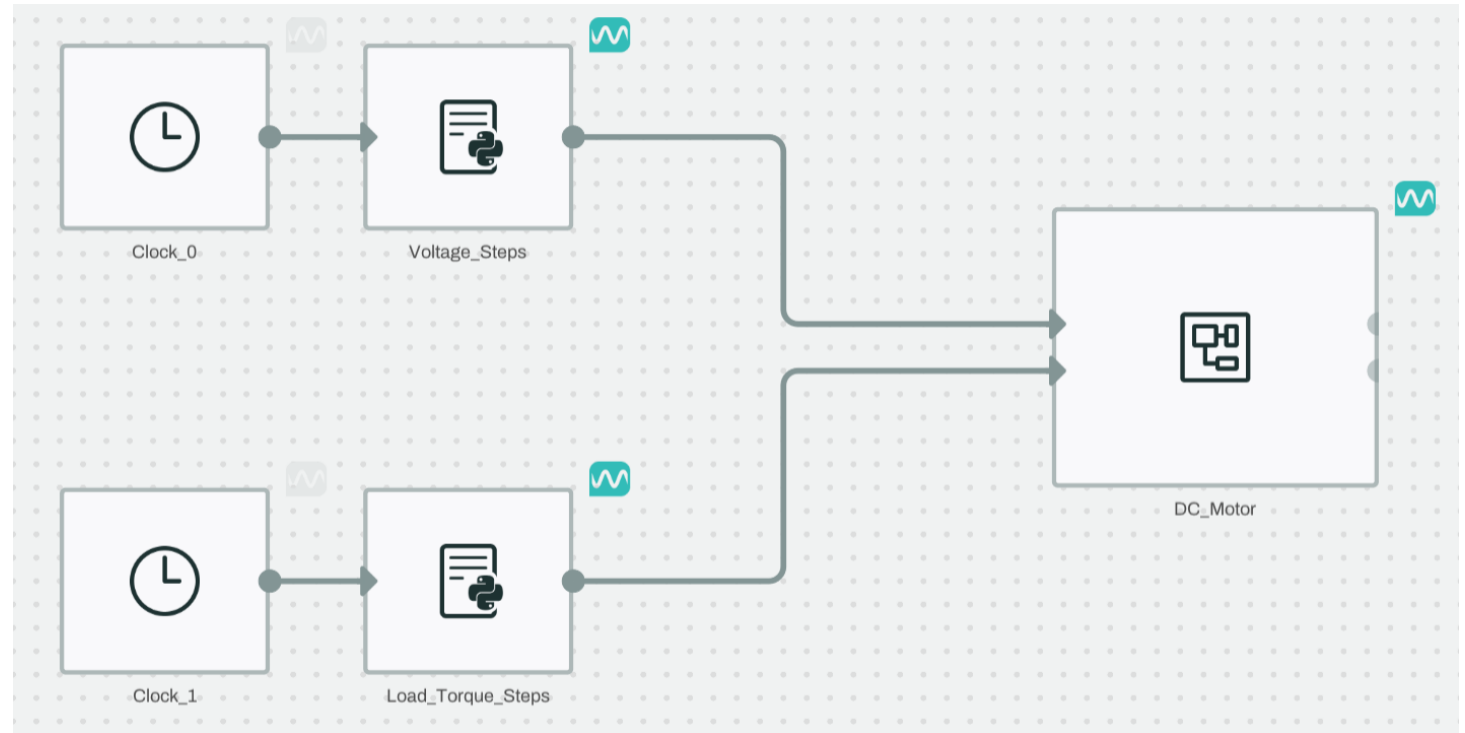
But first, lets generate the data that we will use to build the network...

I built a computer model of a DC motor using...Our Very Own--The Collimator



Data Generation from Collimator

- The Collimator Model is shown in the figure
- Collimator allows for easy download of your simulations data
- It comes by default in the .csv format



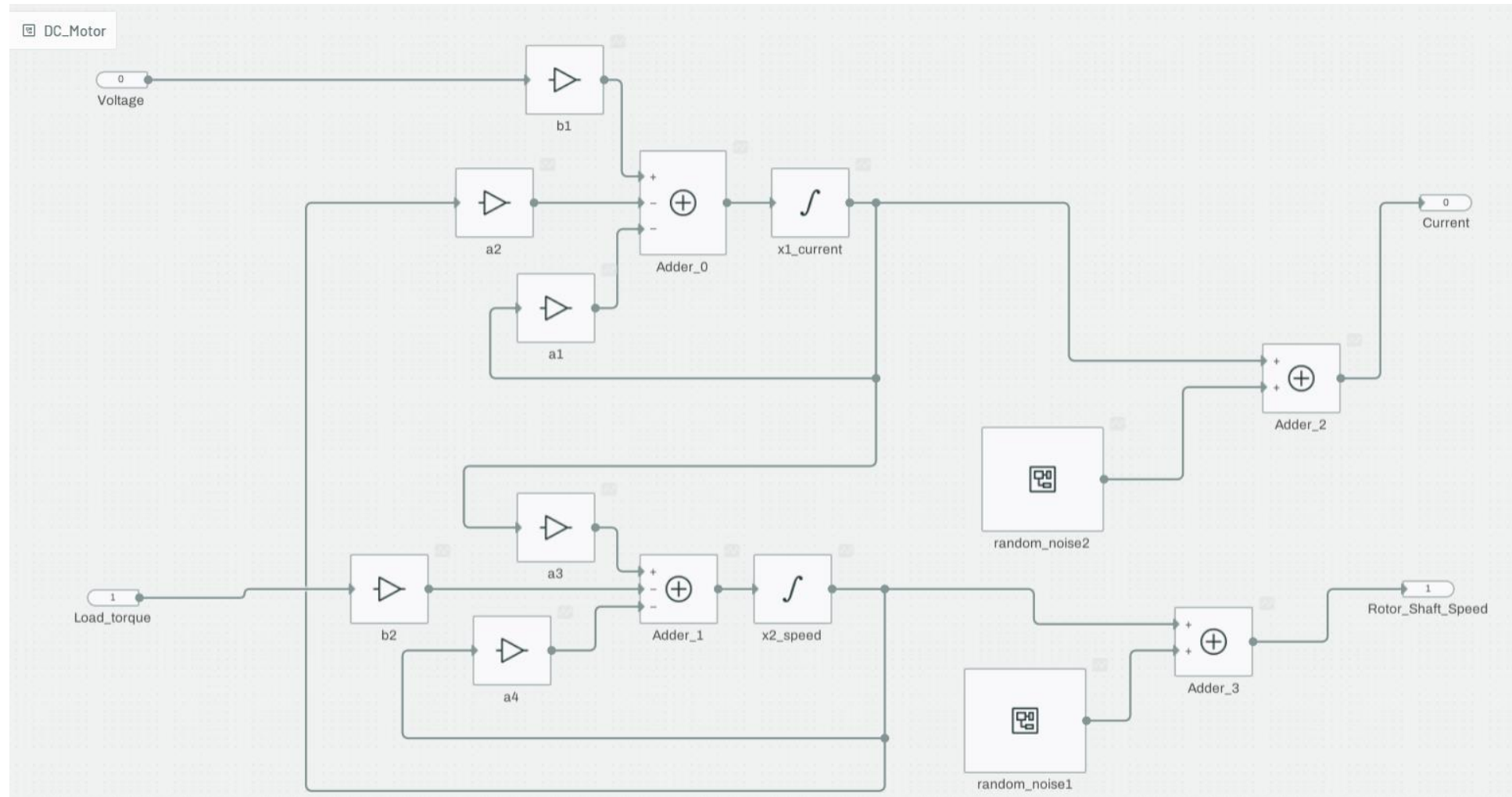
Simulation Parameters

- Simulation Time: 60 seconds
- Solver: fixed step , 0.01
- Motor Parameters in fig

```
1  #DC Motor's Parameters
2  R = 0.6 #ohms armature resistance
3  L = 0.035 #Henry armature inductance
4  Kb = 0.0191 #BEMF constant
5  Kt = 0.0187 #Torque constant
6  J = 0.000125 #Rotor's momement of inertia
7  B = 0.0000095 #Damping coefficient
```


DC Motor Block

- I added some noise to the outputs—speed and current



Voltage Steps

- Training Profile

```
Physics_Model / Voltage_Steps
▼ </> Step
1  #Training Data profile
2  Ts = 60
3  if in_0 >=0 and in_0 < 10:
4      out_0 = 4
5  elif in_0 >=10 and in_0 < 20:
6      out_0 = 8
7  elif in_0 >=20 and in_0 < 30:
8      out_0 = 12
9  elif in_0 >=30 and in_0 < 40:
10     out_0 = 16
11  elif in_0 >=40 and in_0 < 50:
12     out_0 = 20
13  elif in_0 >=50 and in_0 <=60:
14     out_0 = 24
15
```

- Testing Profile

```
Physics_Model / Voltage_Steps
▼ </> Step
16 #Testing Data profile
17 Ts = 60
18 if in_0 >=0 and in_0 < 8:
19     out_0 = 3
20 elif in_0 >=8 and in_0 < 15:
21     out_0 = 6
22 elif in_0 >=15 and in_0 < 28:
23     out_0 = 8
24 elif in_0 >=28 and in_0 < 35:
25     out_0 = 15
26 elif in_0 >=35 and in_0 < 48:
27     out_0 = 18
28 elif in_0 >=48 and in_0 <=60:
29     out_0 = 24
```

Load Torque Steps

- Training Profile

```
Physics_Model / Load_Torque_Steps  
▼ <> Step  
1  # # Training Data Profile  
2  Ts = 60  
3  if in_0 >=0 and in_0 < 5:  
4      out_0 = 0.1  
5  elif in_0 >=5 and in_0 < 15:  
6      out_0 = 0.15  
7  elif in_0 >=15 and in_0 < 25:  
8      out_0 = 0.2  
9  elif in_0 >=25 and in_0 < 30:  
10     out_0 = 0.3  
11  elif in_0 >=30 and in_0 < 35:  
12     out_0 = 0.4  
13  elif in_0 >=35 and in_0 < 55:  
14     out_0 = 0.55  
15  elif in_0 >=55 and in_0 <=60:  
16     out_0 = 0.6
```

- Testing Profile

```
Physics_Model / Load_Torque_Steps  
▼ <> Step  
19 # Testing Data Profile  
20 Ts = 60  
21 if in_0 >=0 and in_0 < 10:  
22     out_0 = 0.05  
23 elif in_0 >=10 and in_0 < 20:  
24     out_0 = 0.2  
25 elif in_0 >=20 and in_0 < 27:  
26     out_0 = 0.3  
27 elif in_0 >=27 and in_0 < 30:  
28     out_0 = 0.1  
29 elif in_0 >=30 and in_0 < 38:  
30     out_0 = 0.35  
31 elif in_0 >=38 and in_0 < 52:  
32     out_0 = 0.4  
33 elif in_0 >=52 and in_0 <=60:  
34     out_0 = 0.6
```

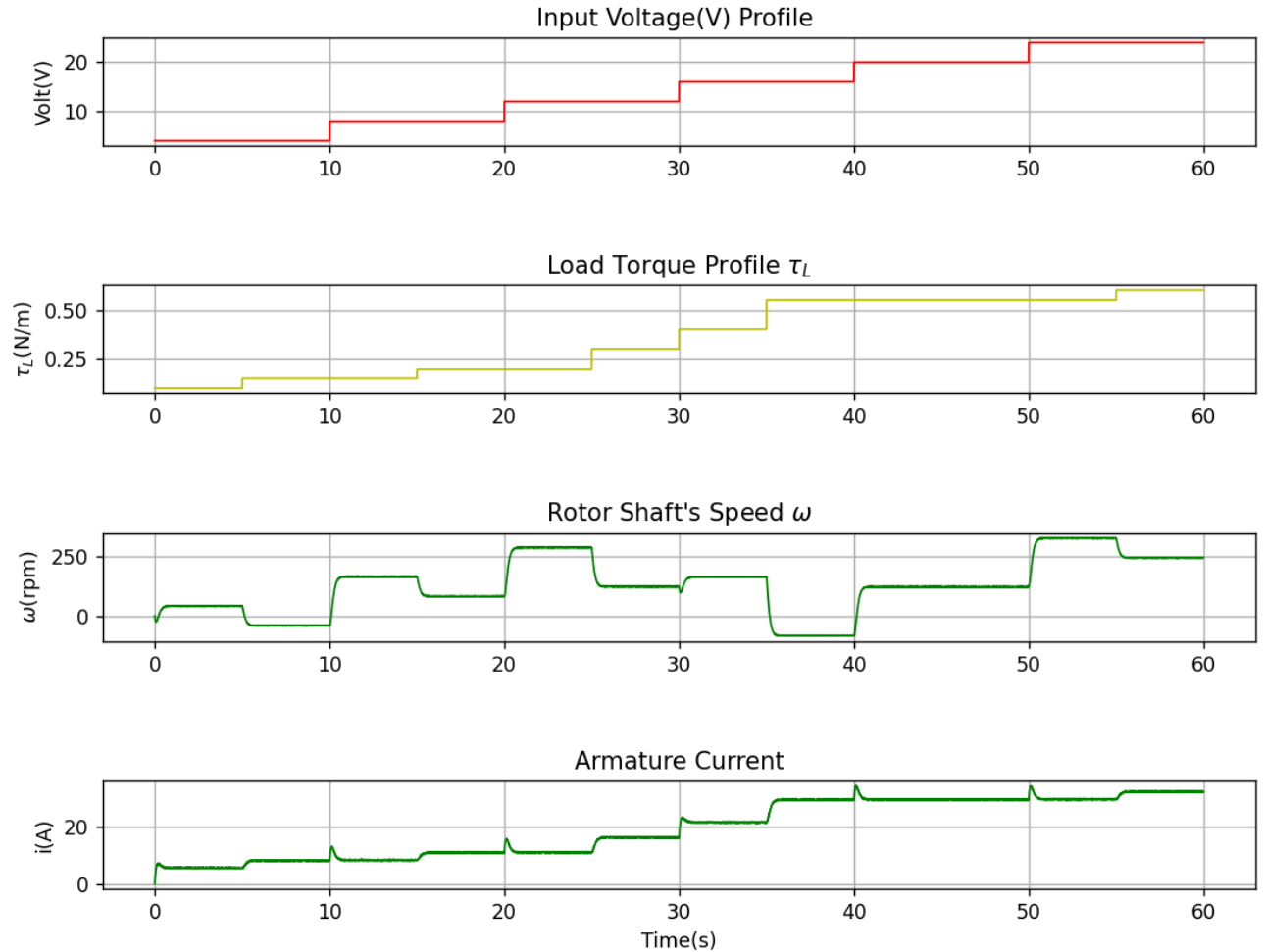
Super!

*Let's visualize the training data gotten
from collimator*



Visualization of the Training Data

- The training data included all the DC motor's operation in 2 modes:
 - a. Forward motoring
 - b. Reverse braking
- Such training allows the PINN to learn about those modes



Gute!!!

Next, lets build a PINN



PINN's Architecture

- I have used the exact architecture used in [1] as shown in the figure 11
- In [1], 2 PINNs where used to model the electrical and mechanical subsystems separately
- I used the same architecture as [1]

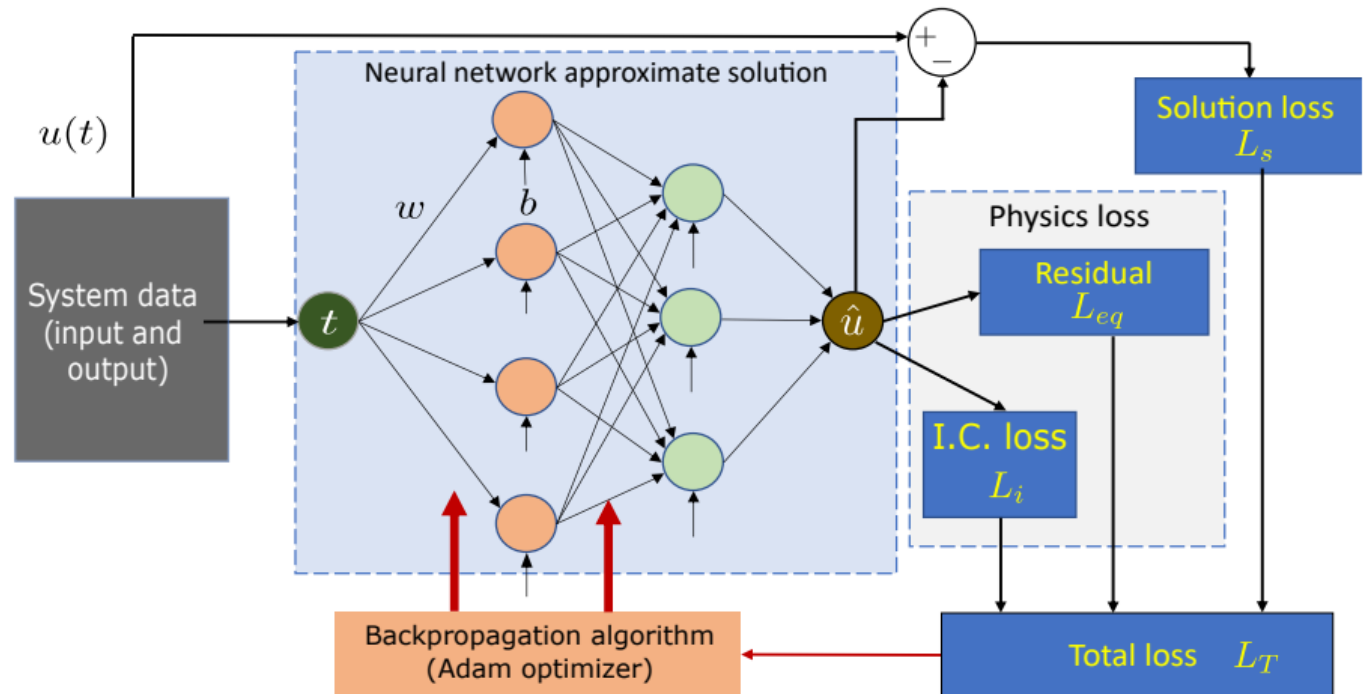


Figure 11. A PINN approach based on physics-guided loss formulation.

After building the PINN, let's test out some hyperparameters to find the most optimal.

And finally we will use the optimal set of hyperparameter to train the PINN and test the PINN with our test data

Hyperparameter Tuning

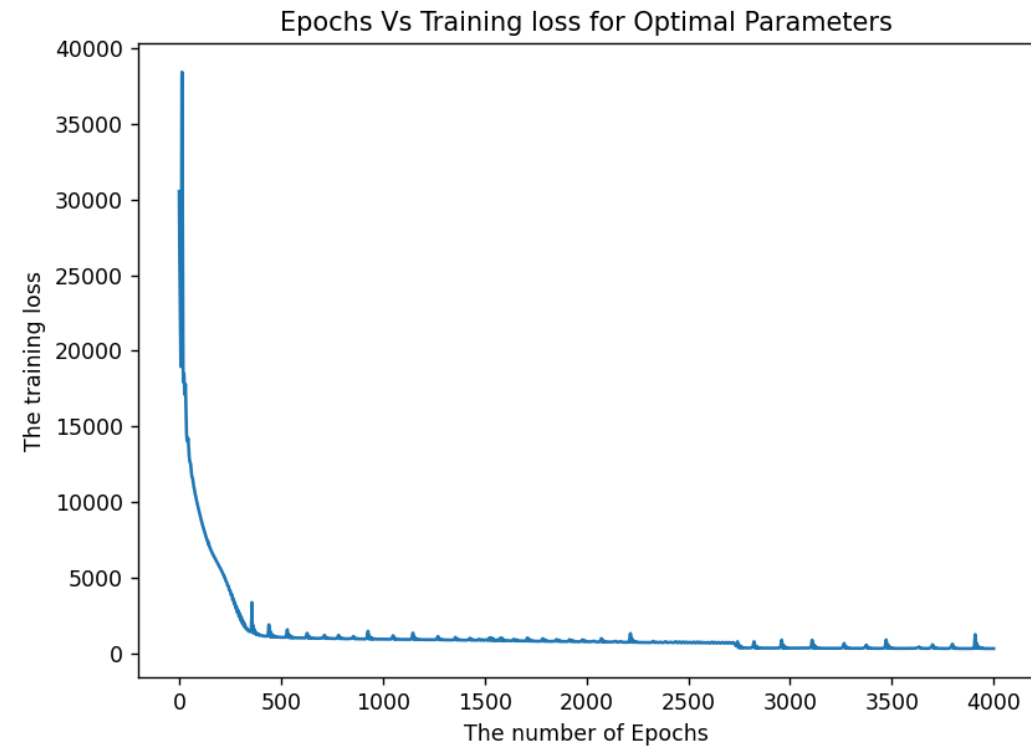
- I tested out 36 combinations of 11 types of hyperparameters as shown below

```
3      # Define hyperparameter search space
4      param_grid = {
5          'activation1': ['relu'],
6          'activation1_2': ['relu'],
7          'epochs': [4000],
8          'kernel_initializer': ['glorot_normal'],
9          'learning_rate': [0.01],
10         'no_of_hidden_layers': [3],
11         'no_of_hidden_layers2': [4],
12         'no_of_neurons_per_layer': [32,64],
13         'no_of_neurons_per_layer2': [32,64],
14         'dropout': [0.001, 0.01,0.1],
15         'dropout_2':[0.001,0.01,0.1]
16     }
17
18     # Generate all possible combinations of hyperparameters
19     param_combinations = list(ParameterGrid(param_grid))
20
```

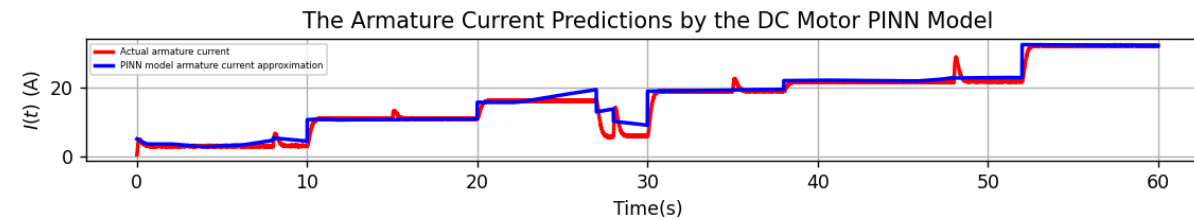
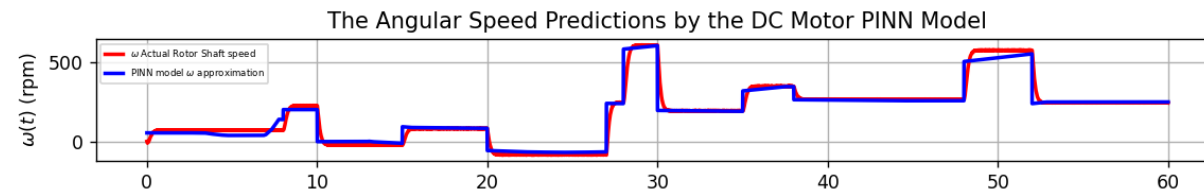
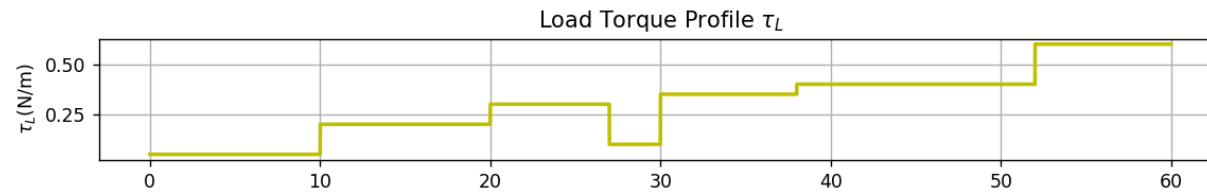
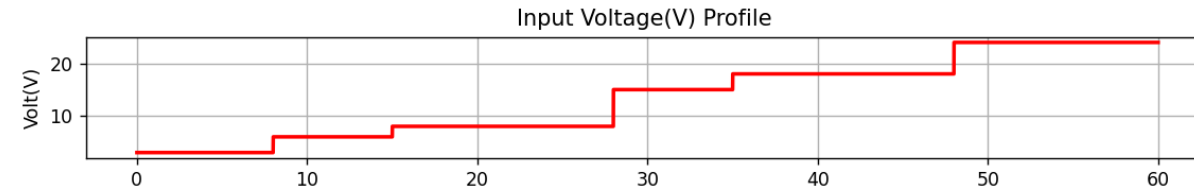
Optimal Parameter

- Total tuning time ~3.75Hours
- The combination of hyperparameters that produced the lowest loss(~199.7)is as shown below
- The plot of the loss per epoch is shown in the figure to the right

```
{'activation1': 'relu',  
 'activation1_2': 'relu',  
 'dropout': 0.01,  
 'dropout_2': 0.01,  
 'epochs': 4000,  
 'kernel_initializer': 'glorot_normal',  
 'learning_rate': 0.01,  
 'no_of_hidden_layers': 3,  
 'no_of_hidden_layers2': 4,  
 'no_of_neurons_per_layer': 64,  
 'no_of_neurons_per_layer2': 64}
```



Testing Results



What's next?

- 1. Generate and use data that spans the DC motor's 4 quadrants of operation*
- 2. Improve the PINN architecture: Combine both the electrical & mechanical subsystems into a single PINN network with two outputs?*
- 3. Deploy the models to a simulator and test its performance in a control application against a regular physics model*

*For more details 'click -> here' for the
jupyter notebook and data*

References

[1] Ayankoso S, Olejnik P. Time-Series Machine Learning Techniques for Modeling and Identification of Mechatronic Systems with Friction: A Review and Real Application. Electronics. 2023; 12(17):3669. <https://doi.org/10.3390/electronics12173669>

(Link to the research's codes: [[here](#)])

[2] G. S. Misyris, A. Venzke and S. Chatzivasileiadis, "Physics-Informed Neural Networks for Power Systems," 2020 IEEE Power & Energy Society General Meeting (PESGM), Montreal, QC, Canada, 2020, pp. 1-5, doi: 10.1109/PESGM41954.2020.9282004.

(Link to the research's code: [[here](#)])