

# Cryptography Basics

## Symmetric Key Cryptography

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# Outline

Symmetric encryption

- Symmetric encryption

- Stream ciphers

- Block ciphers and modes of operation

Hash functions

Message integrity

Authenticated encryption

# Symmetric cryptography

Symmetric cryptography includes:

- Symmetric encryption
- Hash functions
- Message authentication codes
- Authenticated encryption

# Symmetric encryption

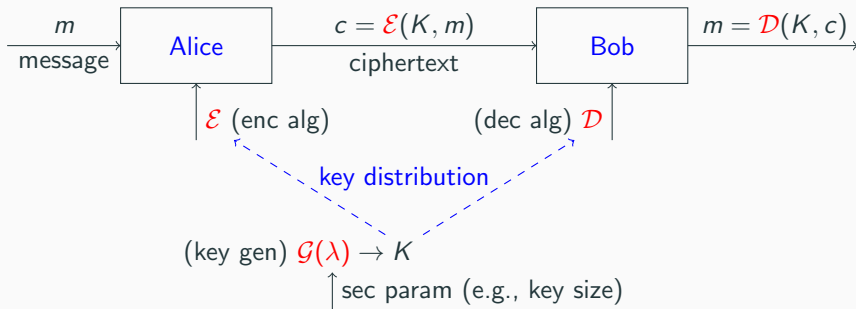
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# Symmetric encryption

Two main goals:

1. Secure communication
  - protects data in motion
  - IPsec and SSL&TLS use it
2. File protection
  - protects data at rest
  - cloud storage tools use it

# Symmetric encryption



## Key distribution:

- Alice and Bob meet and get  $K$ , or
- Alice and Bob use a dedicated mechanism/protocol

$\mathcal{S} = (\mathcal{G}, \mathcal{E}, \mathcal{D})$  - symmetric cipher

# Security models for symmetric encryption

Recall that a **security model** is a pair consisting of a **security goal**  $X$  and an **attack model**  $Y$ , usually written as  $X$ - $Y$ .

## Standard security goals for encryption:

1. **Semantic security** (SS)
2. **Indistinguishability** (IND)
3. **Non-malleability** (NM)

## Standard attack models for encryption:

1. **Chosen plaintext attack** (CPA)
2. **Non-adaptive chosen ciphertext attack** (CCA1)
3. **Adaptive chosen ciphertext attack** (CCA2)

# Security goals

## 1. Semantic security

- 1.1 Proposed by Goldwasser and Micali (1984), it was the first definition of security for encryption
- 1.2 It formalizes the fact that no adversary can obtain any partial information about the message of a given ciphertext (whatever can efficiently be computed about a message from its ciphertext can also be computed without the ciphertext)
- 1.3 It is a “polynomially bounded” version of the concept of **perfect secrecy** introduced by Shannon (1949)
- 1.4 It is complex and difficult to work with

- 2. **Indistinguishability** is an equivalent definition to semantic security which is somewhat simpler
- 3. **Non-malleability** means that, given a ciphertext  $c$  of some message  $m$ , no efficient adversary can construct another ciphertext  $c'$  of some message  $m'$  meaningfully related to  $m$



# Attack models

## 1. Passive attacks:

- 1.1 **Cipher-only attack** (COA):  $\mathcal{A}$  has access to the ciphertext
- 1.2 **Known plaintext attack** (KPA):  $\mathcal{A}$  knows pairs (plaintext, ciphertext)

## 2. Active attacks:

- 2.1 **Chosen plaintext attack** (CPA):  $\mathcal{A}$  has access to the encryption oracle (this is for free for PKE)
- 2.2 **Non-adaptive chosen ciphertext attack** (CCA1):  $\mathcal{A}$  has, in addition to the ability of a CPA adversary, access to a decryption oracle before the challenge phase
- 2.3 **Adaptive chosen ciphertext attack** (CCA2):  $\mathcal{A}$  has, in addition to the ability of a CCA1 adversary, access to a decryption oracle after the challenge phase. However, no decryption query is allowed involving the challenge ciphertext

# Proving security by indistinguishability

Indistinguishability, as a security model, requires that an adversary from a specific class of adversaries interact with the cryptographic scheme under the security study, as follows:

**Train** The adversary trains with the scheme according to his type;

**Challenge** At a given moment, the adversary will choose 2 (different) messages of equal length and will receive the ciphertext of one of them (chosen randomly uniformly);

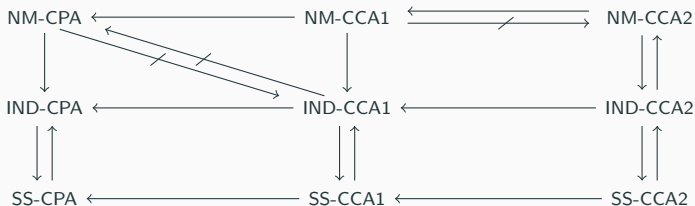
**Train** Depending on the class to which the adversary belongs, he can still train with the scheme;

**Guess** The adversary will have to decide from which of the two messages the ciphertext comes.

If the guessing probability is non-negligible greater than  $1/2$ , then the adversary wins the game, which means that the scheme is not secure for adversaries in this class.

# Relationships among security models

1. IND-COA (also called **indistinguishability in the presence of an eavesdropper**) is the weakest form of security where the adversary can only eavesdrop on ciphertexts;
2. IND-KPA (also called **indistinguishability under multiple encryption attack**) is stronger than IND-COA;
3. The diagram below only aims to create an image on the relationships between the other security models (some of these relationships are far from trivial).

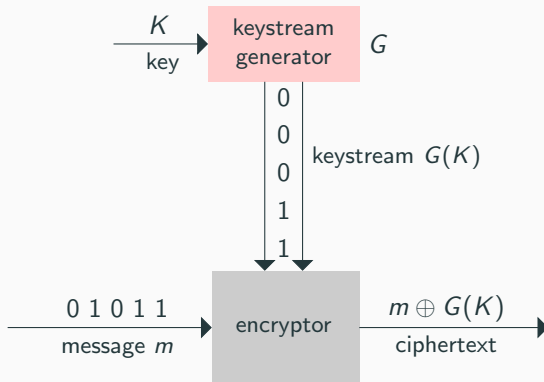


# Stream ciphers

## Main characteristics of a stream cipher:

- The message is viewed as a sequence of **blocks** (also called **characters**) of a very limited size, that can efficiently be enumerated in practice (e.g., bits or bytes)
- The secret key is **expanded** to a **keystream** of the same size as the message block size by a **keystream generator** initially seeded with the secret key
- The encryption is block-driven
- One-time pad (OTP) may be regarded as a stream cipher, but a quite impractical one

# Stream ciphers



## Theorem 1

*The SKE scheme above is IND-COA, provided that  $G$  is a PRG.*

# Stream ciphers: using the same key twice

## Using the same key twice:

- If  $c_1 = m_1 \oplus G(K)$  and  $c_2 = m_2 \oplus G(K)$ , then  $c_1 \oplus c_2 = m_1 \oplus m_2$
- Natural language text contains enough redundancy to allow the adversary to recover  $m_1$  and  $m_2$  from  $c_1 \oplus c_2$

## Real scenarios:

- Microsoft implementation of PPTP in Windows NT uses RC4. Its original implementation uses the same key to encrypt messages from  $A$  to  $B$  and from  $B$  to  $A$  (see [ScMu1998.pdf](#) on the course site)
- Microsoft have used RC4 to protect Word and Excel document. When encrypted documents were modified and saved, the same key was used (see [Wu2005.pdf](#) on the course site)

Never use the same key to encrypt more than one message with stream ciphers !

# Stream ciphers: malleability

## Malleability:

- From an encryption  $c = m \oplus G(K)$  of  $m$  one can simply obtain an encryption of  $m \oplus m'$  by  $c' = c \oplus m'$

## Real scenarios:

- Assume that the adversary knows a prefix  $m_1$  of  $m$  ( $m_1$  might be a standard header filled with someone's address, name, etc.)
- The adversary wants to replace  $m_1$  by  $m_2$  ( $m_2$  might be a header filled with information up to his desire)
- The adversary may compute  $c \oplus (m_1 \oplus m_2)0 \cdots 0$  to obtain what he wants

Stream ciphers do not guarantee integrity !

# The stream cipher RC4

1. RC4 was proposed by Ronald Rivest in 1987 as a trade secret but posted anonymously in September 1994 on a mailing list
2. RC4 was used in a large variety of applications: SSL/TLS, WEP, WPA, MS-PPTP etc.
3. Recent results have shown that the *RC4\_gen* output is biased (see AlFardan et al. (2013)):

$$3.1 \text{ (Mantin \& Shamir, 2001)} \quad P(Z_2 = 0x00) \approx \frac{1}{128}$$

$$3.2 \text{ (Gupta et al., 2012)} \quad P(Z_r = 0x00) \approx \frac{1}{256} + \frac{c_r}{256^2} \text{ for } 3 \leq r \leq 255, \\ \text{where } c_3 = 0.351089 \text{ and } 0.242811 \leq c_r \leq 1.337057 \text{ for } r \geq 4$$

4. Several other variants of RC4 have been proposed: *RC4A*, *VMPC*, *RC4<sup>+</sup>*, *Spritz*



# Other practical stream ciphers

## 1. CSS (Content Scrambling System)

- Designed in 1980's for preventing unauthorized duplication of DVDs
- Can be brute-force attacked in time  $2^{40}$  (the seed space size). A faster attack to recover the seed (time  $2^{16}$ ) was proposed by Frank Stevenson in 1999

## 2. A5/1, A5/2, A5/3 stream ciphers for GSM encryption

- All have been cryptanalysed (see Barkan et al. (2003))

## 3. E0 stream cipher for Bluetooth encryption

- The most efficient cryptanalysis requires the first 24 bits of  $2^{23.8}$  frames (a frame is 2745 bits long) and  $2^{38}$  computations to recover the key (see Lu et al. (2005))

## 4. Salsa, designed by Bernstein in 2005 (see Bernstein (2008b))

## 5. ChaCha, designed by Bernstein in 2008 (see Bernstein (2008a))

# Block ciphers

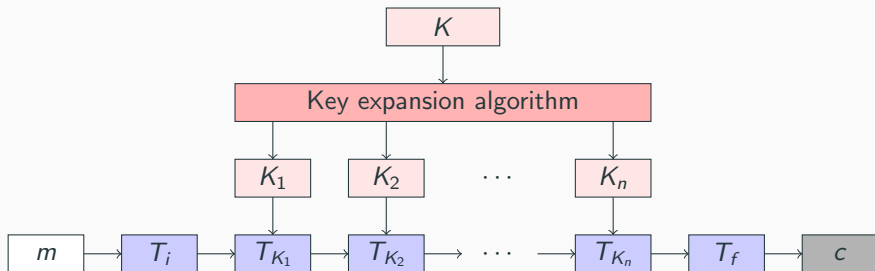
An intensively used method to encrypt a message is the next one::

1. View the message as a sequence of **blocks** of a larger size so that the enumeration of all blocks is infeasible in practice
2. Iteratively encrypt each message block by another block

## Remark 2

1. *The encryption of a message block by another block is done by **families of permutations** (i.e., **block ciphers**) or **families of functions***
2. *The iteration method is crucial and it is called **mode of operation***
3. *In the encryption process of a message block, the encryption key is **expanded** to a fixed number of **round keys***

# Block ciphers



- $T_i$  is an initial transformation, and  $T_f$  is a final transformation
- $T_{K_i}$  is a transformation induced by  $K_i$ ,  $1 \leq i \leq n$

$$c = (T_f \circ T_{K_n} \circ \dots \circ T_{K_1} \circ T_i)(m)$$

# DES and AES block cipher

## 1. DES:

- $\mathcal{M} = \mathcal{C} = \{0, 1\}^{64}$
- $\mathcal{K} = \{0, 1\}^{56}$
- The number of rounds is 16

## 2. AES:

- $\mathcal{M} = \mathcal{C} = \mathcal{M}_{4 \times m}(\mathbb{Z}_2^8)$ , where  $m \in \{4, 6, 8\}$
- $\mathcal{K} = \mathcal{M}_{4 \times k}(\mathbb{Z}_2^8)$ , where  $k \in \{4, 6, 8\}$
- The number of rounds varies on the key and message block length

	$m = 4$	$m = 6$	$m = 8$
$k = 4$	10	12	14
$k = 6$	12	12	14
$k = 8$	14	14	14

# Pseudo-random functions

A **pseudo-random function** (PRF) is a family  $\mathcal{F}$  of functions with the following properties:

1. **Efficiently computable**: Each function  $f \in \mathcal{F}$  can be computed by a deterministic poly-time algorithm;
2. **Pseudo-randomness**: If we randomly choose a function from this family then its input-output behavior is computationally indistinguishable from that of a random function.

The adversary is allowed to train with  $f \in \mathcal{F}$  to establish the pseudo-randomness of  $f$  (see “indistinguishability”)!

# Pseudo-random permutations

Pseudo-random permutations (PRPs) are special cases of PRFs.

$\mathcal{F}$	Content type	Efficient computability	Pseudo-randomness
PRF	functions	each $f$	$\mathcal{A}$ trains with $f$
weak PRP	permutations	each $f$ and $f^{-1}$	$\mathcal{A}$ trains with $f$
strong PRP	permutations	each $f$ and $f^{-1}$	$\mathcal{A}$ trains with $f$ and $f^{-1}$

## Remark 3

1. Strong PRP are simply referred to as PRP
2. PRP are sometimes called *block ciphers*

# PRP candidates

1.  $DES = (DES_K)_{K \in \{0,1\}^{56}}$ , where

$$DES_K : \{0,1\}^{64} \rightarrow \{0,1\}^{64}$$

2.  $3DES = (3DES_K)_{K \in \{0,1\}^{168}}$ , where

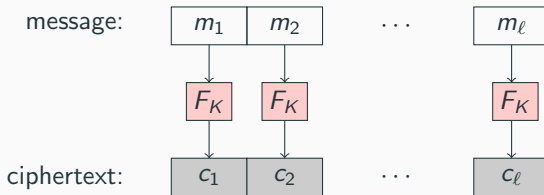
$$3DES_K : \{0,1\}^{64} \rightarrow \{0,1\}^{64}$$

3.  $AES-128 = (AES_K)_{K \in \{0,1\}^{128}}$ , where

$$AES_K : \{0,1\}^{128} \rightarrow \{0,1\}^{128}$$

# Electronic Code Block (ECB)

$F = (F_K)_K$  is a PRP



## Theorem 4

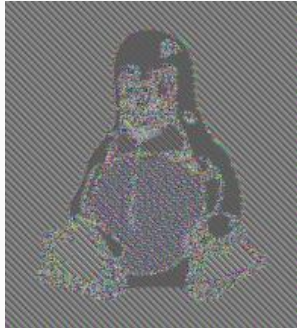
*ECB is not IND-KPA.*



# ECB illustrated



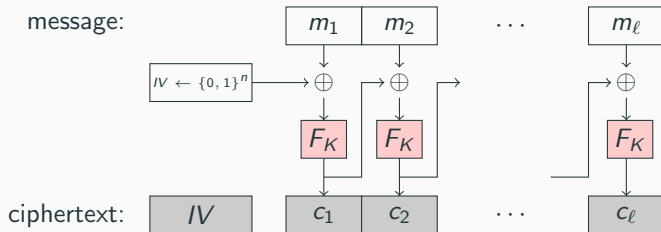
Original image



ECB encryption

# Cipher Block Chaining (CBC)

$F = (F_K)_K$  is a PRP



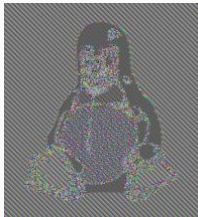
## Theorem 5

If  $F = (F_K)_K$  is a PRP, then CBC with  $F$  is IND-CPA.

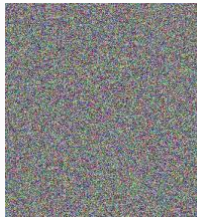
# CBC versus ECB



Original image



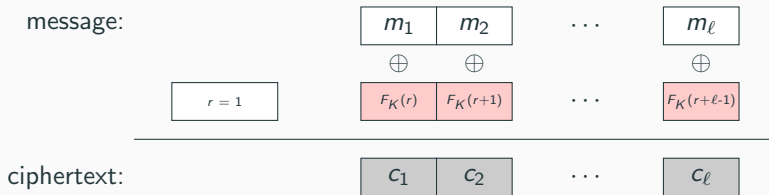
ECB encryption



CBC encryption

# Deterministic counter mode (DCTR)

$F = (F_K)_K$  is a PRF



The scheme works like a stream cipher with the PRG  $G$  given by

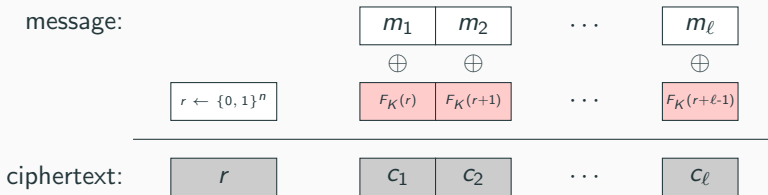
$$G(K) = F_K(1) \parallel F_K(2) \parallel \dots \parallel F_K(\ell)$$

## Theorem 6

If  $F = (F_K)_K$  is a PRF, then DCTR with  $F$  is IND-KPA but not IND-CPA.

# Counter mode (CTR)

$F = (F_K)_K$  is a PRF



The scheme works like a stream cipher with the PRG  $G$  given by

$$G(K) = F_K(r) \parallel F_K(r+1) \parallel \dots \parallel F_K(r+\ell-1)$$

## Theorem 7

If  $F = (F_K)_K$  is a PRF, then CTR with  $F$  is IND-CPA.

# Output feedback (OFB) and cipher feedback (CFB)

1. The key stream in CTR mode is

$$F_K(r) \parallel F_K(r+1) \parallel F_K(r+2) \parallel \dots$$

where  $r \leftarrow \{0, 1\}^n$

2. The OFB and CFB modes are defined as the CTR mode but with a different key stream generation :

- 2.1 The key stream in OFB mode is

$$F_K(r) \parallel F_K(F_K(r)) \parallel F_K(F_K(F_K(r))) \parallel \dots$$

where  $r \leftarrow \{0, 1\}^n$

- 2.2 The key stream in CFB mode is

$$F_K(r) \parallel F_K(c_1) \parallel F_K(c_2) \parallel \dots$$

where  $r \leftarrow \{0, 1\}^n$

# Hash functions

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# Hash functions

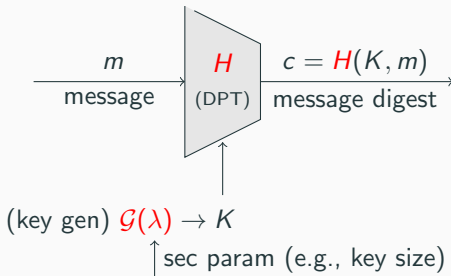
A **hash function** outputs a fixed-length bitstring (e.g., 128 or 160) when applied to an arbitrary-length bitstring.

Hash functions are **used in many cryptographic applications** such as:

- signing messages, in connection with digital signatures (signing a document should be a fast operation and the signature should be small so that it can be put on a smart card);
- identifying files on peer-to-peer file sharing networks;
- ensuring security of micro-payment schemes (e.g., PayWord);
- etc.



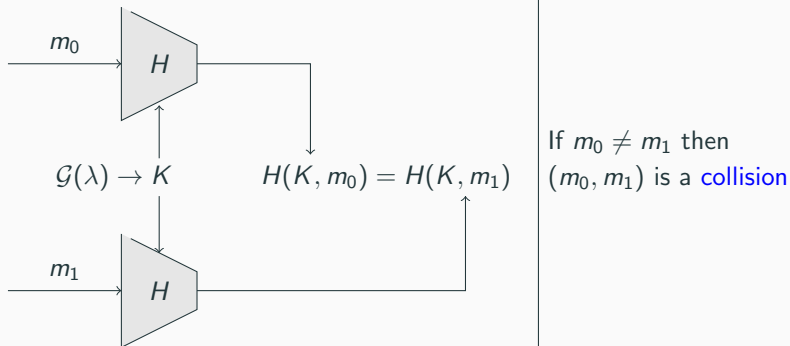
# Hash functions



$\mathcal{H} = (\mathcal{G}, H)$  - (keyed) hash function

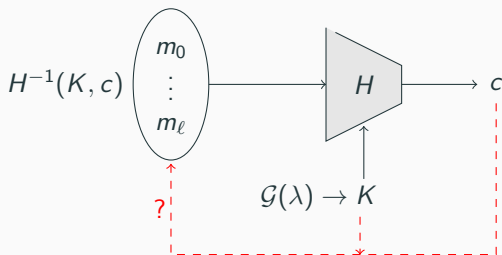
When no key is used,  $H$  is called a hash function.

# Collision-resistant hash functions



A keyed hash function  $\mathcal{H}$  is **collision-resistant** (CRHF) if no adversary, given a randomly generated key  $K$ , can compute a collision  $(m_0, m_1)$  for  $H$  under  $K$  with a higher than negligible probability.

# One-way hash functions



A keyed hash function  $\mathcal{H}$  is **one-way** (OWHF) if no adversary, given a randomly generated key  $K$  and a message digest  $c$  obtained with  $K$ , can compute  $m \in H^{-1}(K, c)$  with a higher than negligible probability.

## Theorem 8

*Any CRHF is also a OWHF, as long as the domain of the hash function is significantly larger than its range.*

# Looking for collisions

## Theorem 9

*Let  $m$  be the number of possible message digests of a hash function  $H$  under some key  $K$ . If we compute message digests for  $r$  messages chosen uniformly at random and*

$$\lfloor \sqrt{2cm} \rfloor < r < m$$

*for some real constant  $c > 0$ , then the probability to get a collision is higher than  $1 - e^{-c}$  ( $e$  is Euler's number,  $e = 2.71828 \dots$ ).*

If  $c \geq \ln 2 \sim 0.693$ , then  $1 - e^{-c} > \frac{1}{2}$

## Example 10

Let  $m = 2^{40}$  and  $r$  such that  $1.200.000 \approx \lfloor 2^{20} \sqrt{2 \ln 2} \rfloor < r < 2^{40}$ .

The probability of getting a collision is greater than  $1/2$ . Therefore, 40-bit message digests do not ensure security.

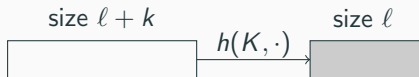
# Construction of CRHFs

Two practical techniques to construct CRHFs:

1. The Merkle-Damgard (MD) transform
2. The sponge construction

# The MD transform

- Use a **compression function**  $h : \mathcal{K} \times \{0, 1\}^{\ell+k} \rightarrow \{0, 1\}^{\ell}$

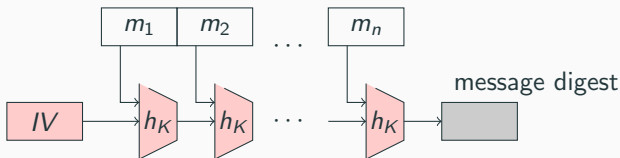


- Use an **MD-complaint padding**  $pad : \{0, 1\}^{<2^\ell} \rightarrow \bigcup_{n \geq 1} \{0, 1\}^{n\ell}$   
with the following properties:

- $m$  is a prefix of  $pad(m)$
- if  $|m_1| = |m_2|$  then  $|pad(m_1)| = |pad(m_2)|$
- if  $m_1 \neq m_2$ , then the last block of  $pad(m_1)$  is different than the last block of  $pad(m_2)$

# The MD transform

- Iterate  $h$  on messages  $m$  as follows:
  - $pad(m) = m_1 \parallel \dots \parallel m_n$  with  $|m_i| = k$  for all  $i$
  - $V := IV$ , where  $IV \leftarrow \{0, 1\}^\ell$
  - for  $i := 1$  to  $n$  do  $V := h(K, m_i \parallel V)$
  - return  $V$



## Theorem 11

*If  $h$  is collision-resistant, then the MD-transform based on  $h$  is so.*

# The MD transform in practice

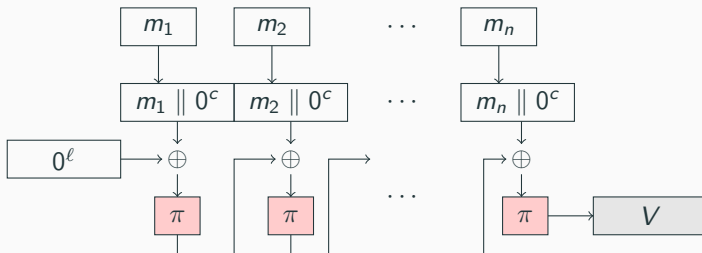
Practical hash functions based on the MD-transform:

- MD4 – developed by Rivest in 1990. It was the starting point for the development of a series of similar hash functions
- SHA (Secure Hash Algorithm) or SHA-0 – developed by NSA in 1993 (withdrawn shortly after publication because of some flaw)
- MD5 – the strengthened successor of MD4 (Rivest 1995)
- SHA-1 – developed by NSA in 1995; not longer approved after 2010
- SHA-2 family includes 6 hash functions, SHA-224, SHA-256, SHA-384, SHA-512, SHA-512/224, SHA-512/256 (the last two are truncated versions of SHA-512)



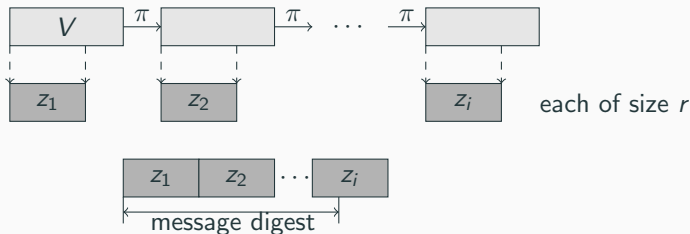
# The sponge construction

- Choose a **permutation**  $\pi : \{0, 1\}^\ell \rightarrow \{0, 1\}^\ell$  ( $\pi$  has no key!) and write  $\ell = r + c$  ( $r$  is the **rate** and  $c$  is the **capacity**)
- Pad  $m$  and divide it into  $r$ -bit blocks  $m_1 \cdots m_n$
- Absorbing phase**



# The sponge construction

- Squeezing phase



## Theorem 12

*If  $\pi$  is a random permutation and  $2^\ell$  and  $2^c$  are super-poly, then the sponge construction yields a CRHF.*

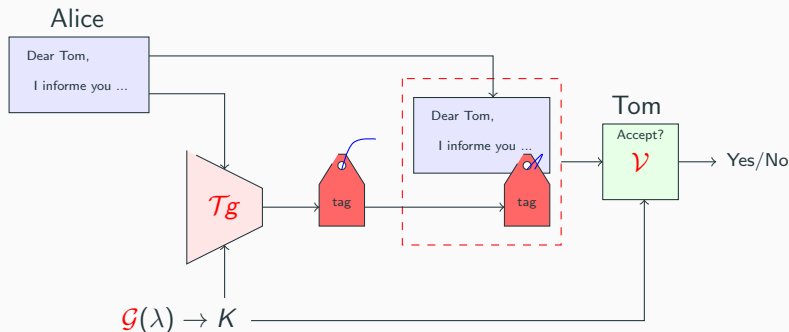
The sponge construction is the basis of SHA-3 standard.

# Message integrity

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# Message authentication codes

Message authentication codes (MACs) = used to prove message integrity based on a shared secret key between parties



$\mathcal{S} = (\mathcal{G}, \mathcal{T}_g, \mathcal{V})$  – MAC system

A MAC system  $S$  is **secure** if no adversary, who has been allowed to train with the MAC system, can generate valid tags for messages of his choice, except with negligible probability.

MAC systems can be obtained from:

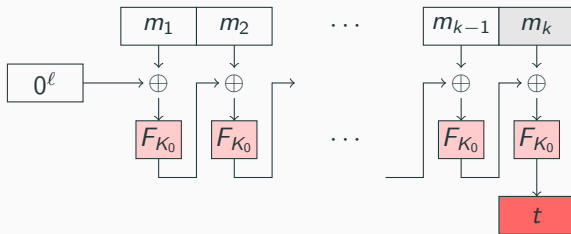
1. PRFs
2. Hash functions

# MACs from PRFs: CMAC

If  $F$  is a PRF on messages of length  $\ell$ , define the following MAC scheme, called **Cipher-based MAC** (CMAC) (see Dworkin (2005)):

1. Generate three keys  $K_0$ ,  $K_1$ , and  $K_2$  of length  $\ell$  from  $K$ ;
2. Break the message  $m$  into  $m = (m_1, \dots, m_{k-1}, m_k)$ ;
3. Randomize the last block:
  - If  $|m_k| = \ell$  then replace  $m_k$  by  $m_k \oplus K_1$ ;
  - If  $|m_k| < \ell$  then replace  $m_k$  by  $(m_k \parallel 1 \parallel 0^j) \oplus K_2$ ;
4. Apply  $F$  with  $K_0$  in the CBC mode and **output only the last block** as the message tag.

# MACs from PRFs: CMAC



## Theorem 13

*CMAC is secure, provided that  $F$  is a PRF.*

# MACs from CRHFs: HMAC

Let  $H$  be a hash function defined by the MD transform from a compression function  $h(K, m)$ . Define  $F_H$  by

$$F_H((K_1, K_2), m) = H(K_2 \parallel H(K_1 \parallel m))$$

## Theorem 14

*If  $h$  and  $h'$  given by  $h'(K, m) = h(m, K)$  are PRFs, then  $F_H$  is a PRF.*

For a proof of this theorem please see Boneh and Shoup (2020).

The HMAC construction uses one single key  $K$  from which two keys are derived:  $K_1 = K \oplus \text{ipad}$  and  $K_2 = K \oplus \text{opad}$ .

HMAC-SHA1 and HMAC-SHA256 are instances of the above construction, with  $H = \text{SHA1}$  and  $H = \text{SHA256}$ , respectively.



# **Authenticated encryption**

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# The need for authenticated encryption

Combining secure encryption schemes with secure MACs may lead to error-prone systems (see Krawczyk (2001), Bernstein (2013))

## Definition 15

Let  $S$  be a cipher.

1.  $S$  provides **ciphertext integrity** (CI) if no adversary can output valid ciphertexts, except with negligible probability.
2.  $S$  provides **authenticated encryption** (AE) if:
  - 2.1  $S$  is IND-CPA secure
  - 2.2  $S$  provides CI.

## Theorem 16

*If  $S$  is AE secure then it is IND-CCA secure.*

# Constructing AE secure ciphers

One popular way to construct AE secure ciphers is to combine an IND-CPA secure cipher with a secure MAC. There are two main variants:

1. **Encrypt-then-MAC** (EtM)

- 1.1  $c \leftarrow \mathcal{E}(K, m)$ ,  $t \leftarrow \mathcal{Tg}(K', c)$ , output  $(c, t)$

- 1.2 Used in IPsec, TLS 1.2 and later versions, and in the NIST standard GCM

2. **MAC-then-Encrypt** (MtE)

- 2.1  $t \leftarrow \mathcal{Tg}(K', m)$ ,  $c \leftarrow \mathcal{E}(K, (m, t))$ , output  $c$

- 2.2 Used in SSL 3.0, TLS 1.0, and in 802.11i WiFi encryption protocol

The keys  $K$  and  $K'$  are chosen independently

## Theorem 17

*If  $S$  is an IND-CPA secure cipher and  $S'$  is a secure MAC, then the EtM construction is a secure AE.*

Common mistakes in implementing the EtM construction:

1. Use the same key for the cipher and the MAC
2. Apply the MAC only to part of the ciphertext (we may lose ciphertext integrity) – discovered in 2013 at RNCryptor facility in Apple's iOS

# MAC-then-Encrypt

MtE is not generally secure:

1. The attack POODLE on SSL 3.0
2. Padding oracle timing attack in TLS 1.0
3. Informative error messages in TLS 1.0

There are secure instances of MtE:

1. The randomized counter mode of the cipher assures AE security

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