

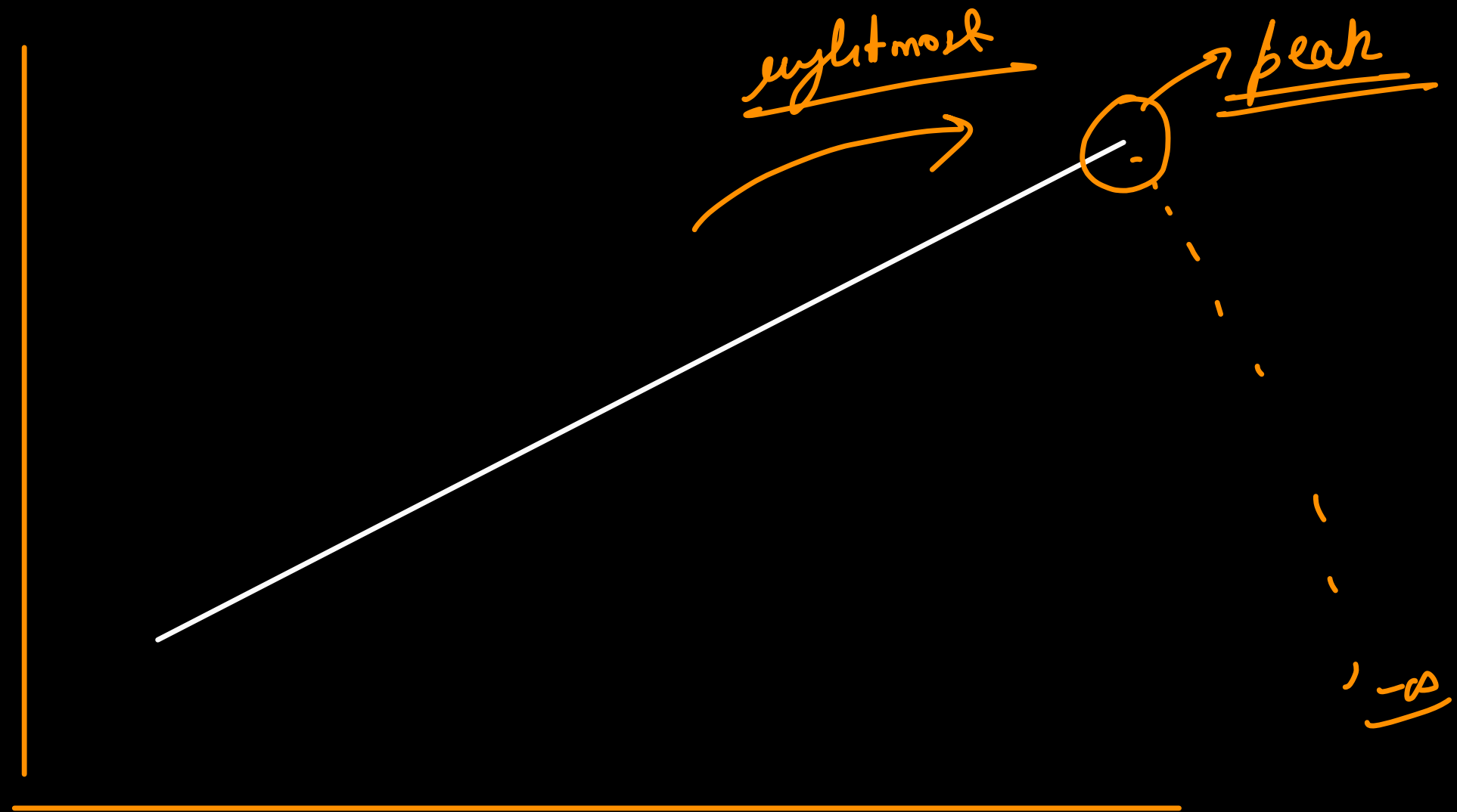
$-\infty$ $\overset{1}{\downarrow}$ $[1, \textcircled{2}, 1, 3, 5, \textcircled{6}, 4]$ $\overset{2}{\downarrow}$ $-\infty$
 $1 < 2 > 1$ $5 < 6 > 4$

$a[i-1] < \textcircled{a[i]} > a[i+1]$
 $\xrightarrow{\text{peak}}$
 \downarrow

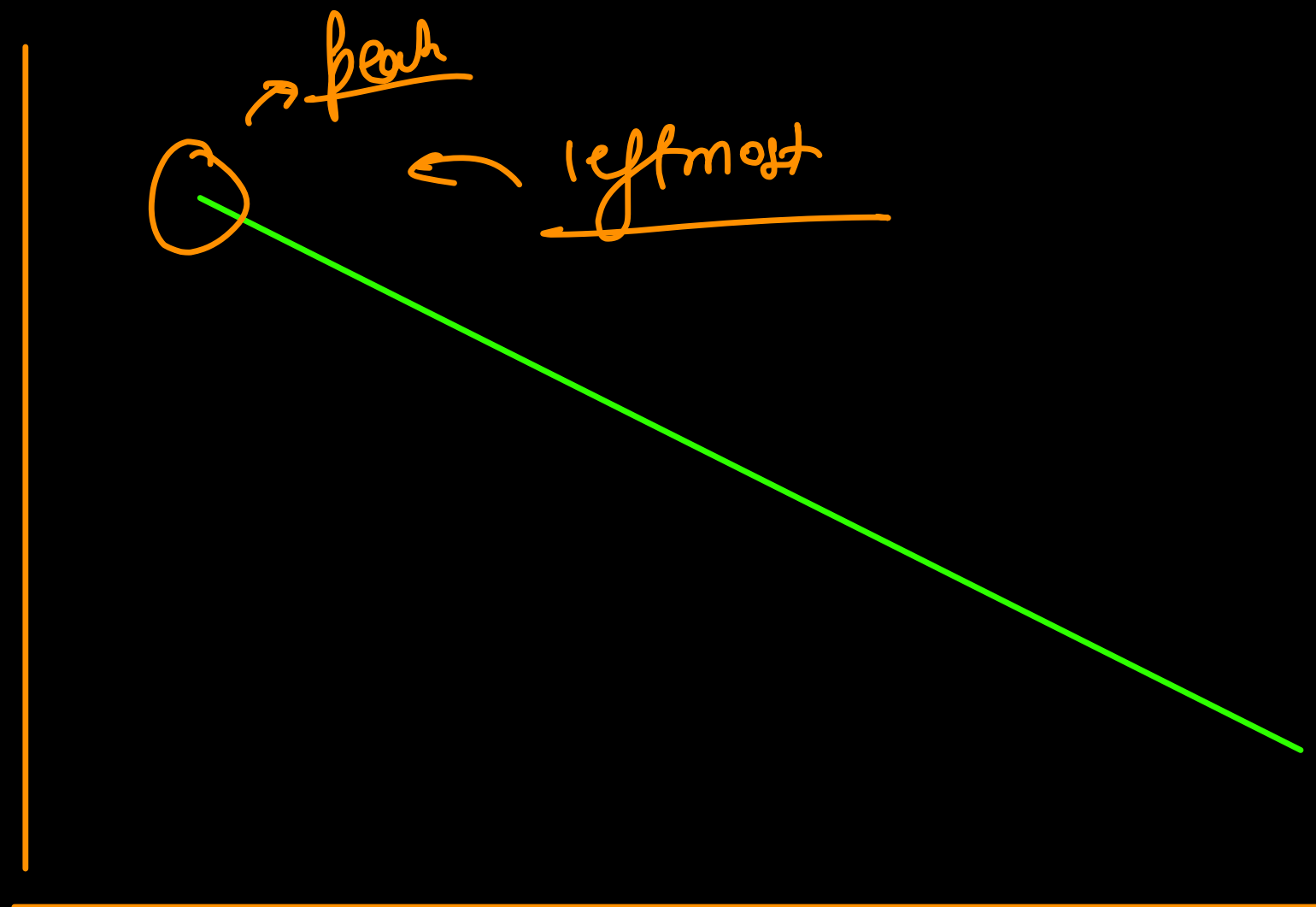
peak
 any one of the
peak

the element at i^{th} index
 will be the peak
 element if it is greater
 than the neighbors

Case I →
whole array is
sorted in inc
order



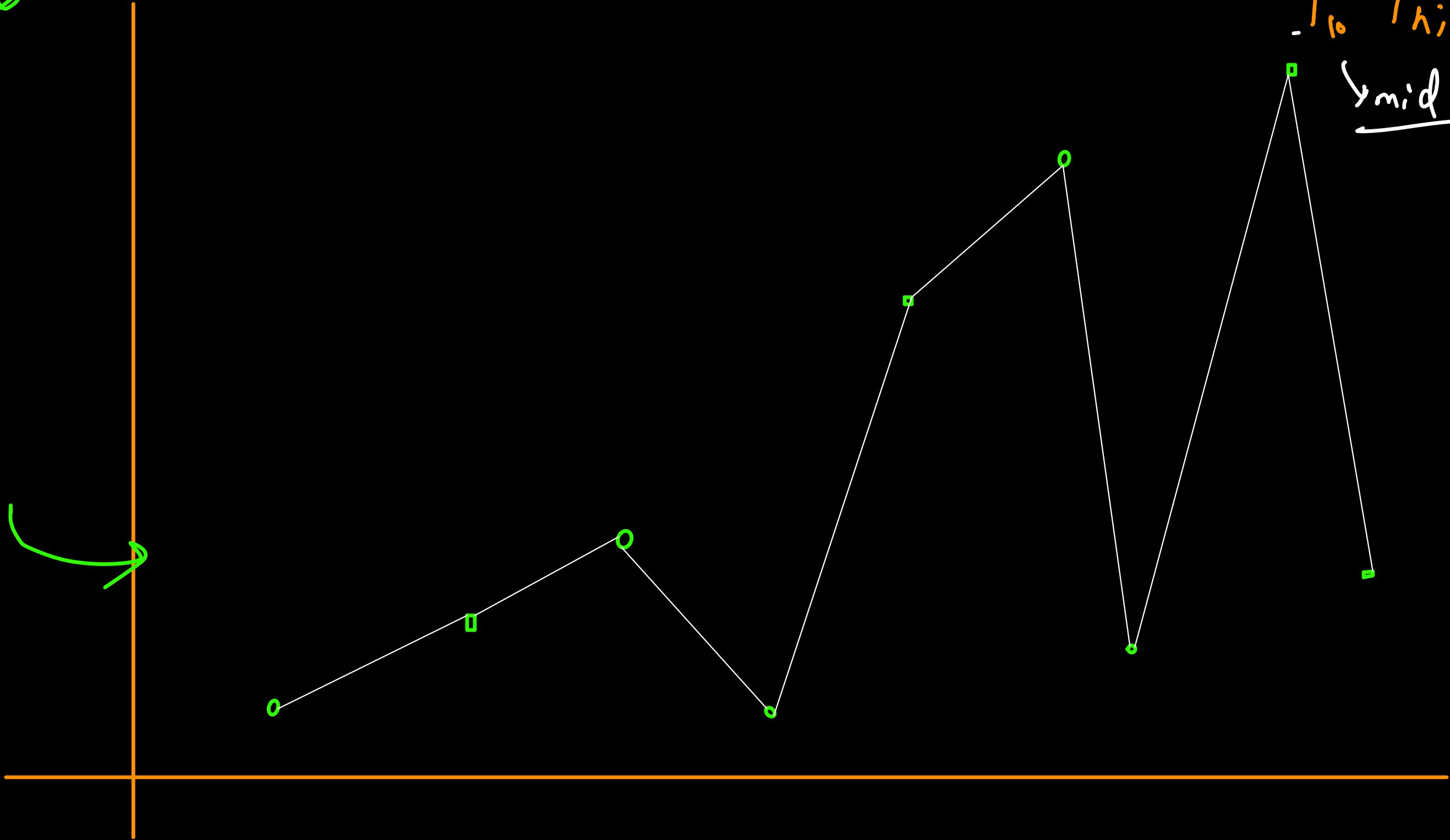
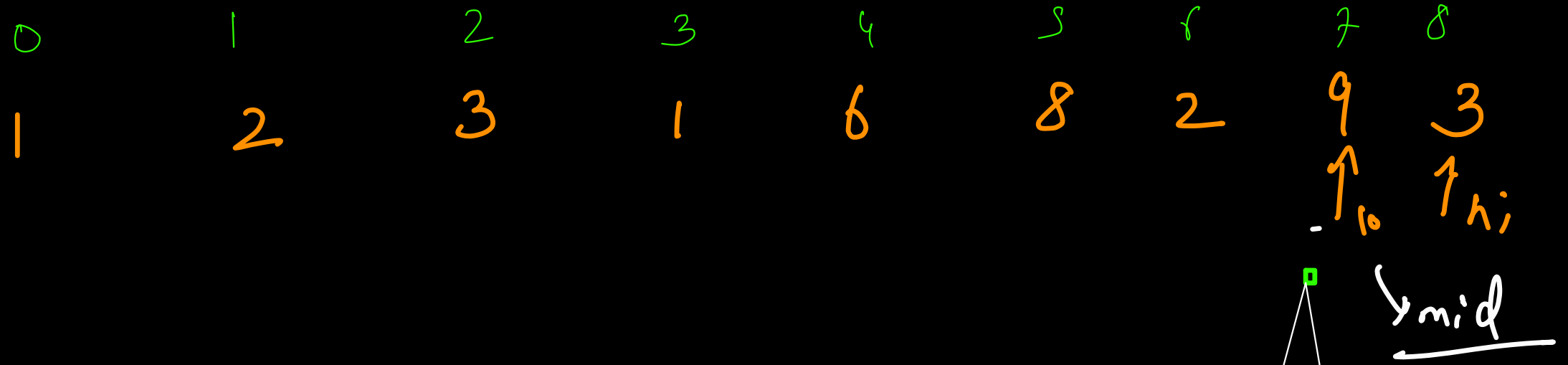
Case II →
whole array is
sorted in dec
order



if we are on an inc curve, we will find ans on
the right side

else if we are on a pure decrease, we will find ans
on the left side

~~$\log N$~~



while $(lo \leq hi)$ {

if $(a[mid] > a[mid+1] \text{ and } a[mid] > a[mid-1])$

return mid

if $(a[mid] > a[mid+1])$ {

$hi = mid - 1$

} else {

$lo = mid + 1$

}

}

Time $\rightarrow O(\log n)$

Space $\rightarrow \underline{\underline{O(1)}}$

write ($lo \leq hi$)

$mid = lo + (hi - lo) / 2;$

$O(\log n)$

if ($mid + 1 \geq n$ and $a[mid] > a[mid + 1]$)
return mid;

if ($mid - 1 < 0$ and $a[mid] > a[mid + 1]$)
return mid

if ($a[mid] > a[mid + 1]$ and $a[mid] > a[mid - 1]$)

return mid

if ($a[mid] > a[mid + 1]$) {
 $hi = mid - 1$

} else {

$lo = mid + 1$

}

}

Qⁿ Given a sorted (asc) array where every element is present twice only one element is present once. find the single element in $O(\log n)$ time.

[1, 1, 3, 3, 8, 8, 10, 11, 11, 13, 13]

Ans \rightarrow 6 (index)

asc

← ^{low high}
[1, 1, 2, 3, 3, 4, 7, 8, 8]
0 1 2 3 4 5 6 7 8

first-occ → even
2nd occ → odd → single element

→ first occ → odd
2nd occ → even

How to distinguish if an element is 1st or 2nd index
 $i \geq 0$ and $a[i] == a[i-1]$
→ 2nd occ

while (lo < hi)

mid = lo + (hi - lo) / 2

if (a[mid] != a[mid-1] and a[mid] != a[mid+1])

return mid;

if (a[mid] == a[mid-1]) → mid 2nd occ

if (mid % 2 == 0)

hi = mid - 2;

else

lo = mid + 1

else { → 1st occ

if (mid % 2 == 0)

lo = mid + 2

else

hi = mid - 1

JOIN THE DARKSIDE

$O(\log N)$

$O(1)$

Binary Search On Ans

Search Space

→ array of element

→ set

→ range of no.

↓
min - max possible
value of the quantity

→ search space

what is the quantity
we want to calc

Square Root

$$x \rightarrow 100$$

$$\sqrt{x}$$

square root of a number x , will always lie in the range $[1, x-1]$ search space

① Linear Search

$$ans = -1$$

for ($i=1$; $i \leq x-1$; $i++$)

if ($i*i \leq x$)

$$ans = i;$$

else

break;

$$\mathcal{O}(\sqrt{x})$$

j

$$x=100$$

$i = 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11$

$ans = 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$

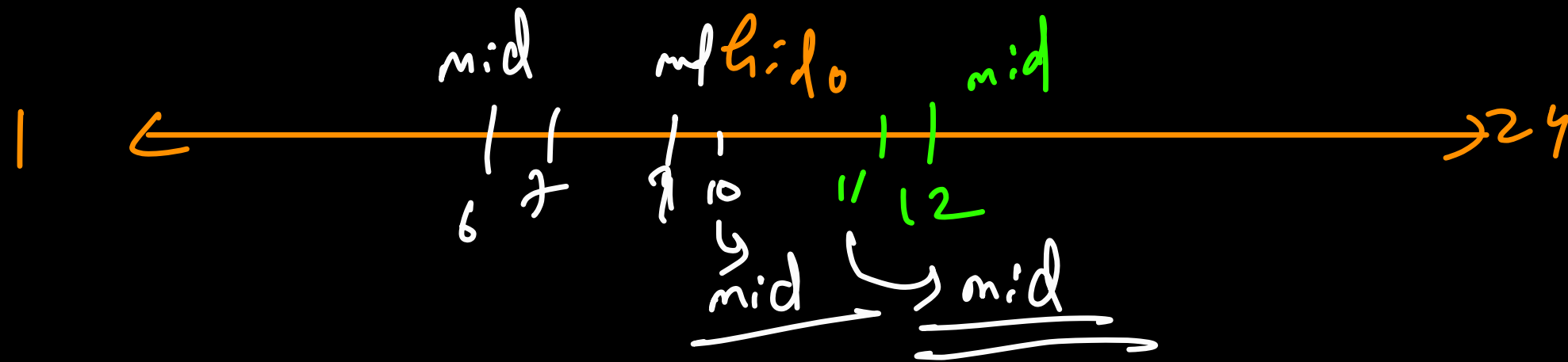
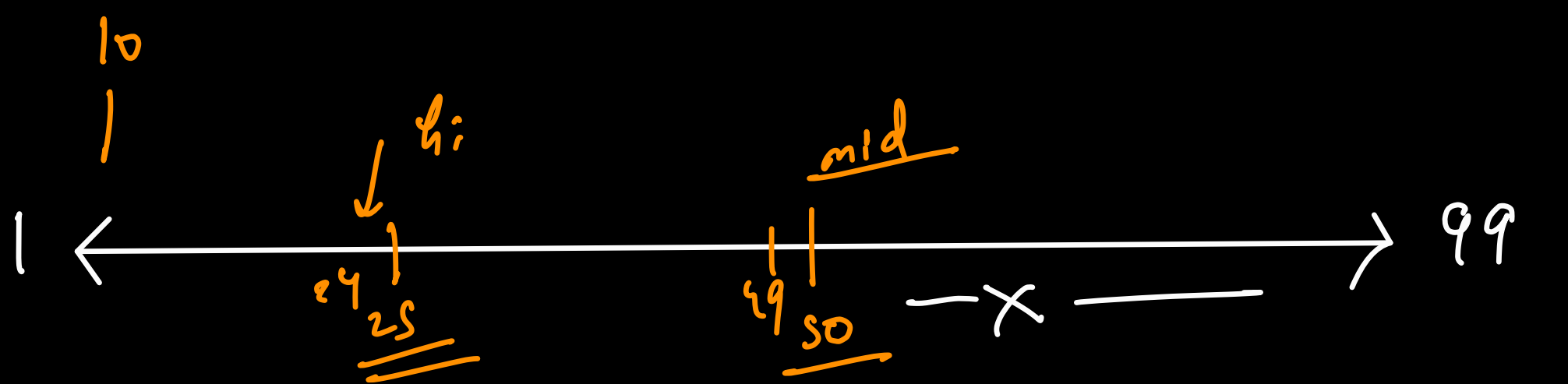
first no. greater than root x
we break the loop.

ans will be biggest value
less than or equal to \sqrt{x} .

Binary Search

$$\text{mid}^2 \leq x$$

mid can be
a potential
ans



if ($\text{mid}^2 > x$)
 ↳ discard right
 $\text{hi} = \text{mid} - 1$

~~ans = 8~~ ~~9~~ ~~10~~

else {
 ↳ discard left
 $\text{lo} = \text{mid} + 1$
 ans = mid
}

$O(\log x)$
 $O(1)$ → space

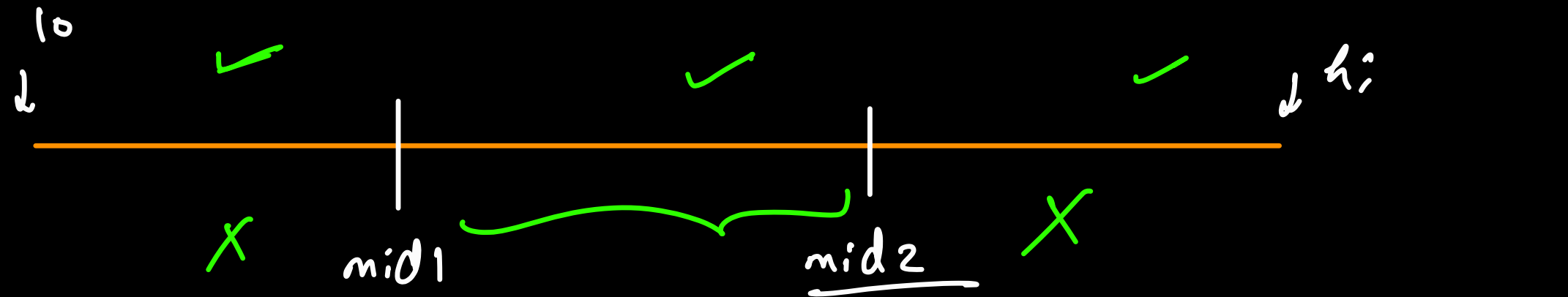


$$\underline{x \rightarrow 10^9}$$

$$\sqrt{x} \rightarrow \underline{\underline{10^5}}$$

$$\log x \rightarrow \underline{\underline{30}}$$

Ternary Search



$$n \rightarrow \frac{1}{3} \rightarrow \underline{\underline{\log_3 n}}$$

$$mid1 = lo + \frac{(hi - lo)}{3}$$

$$mid2 = hi - \left(\frac{hi - lo}{3} \right)$$

$$n \rightarrow \frac{1}{2} \rightarrow \underline{\underline{\log_2 n}}$$

$$\boxed{\log_3 n < \log_2 n}$$



if (a[mid] > x) {

}

else {

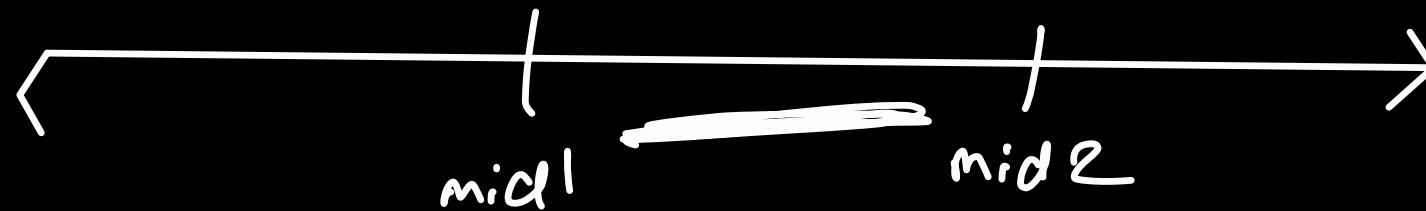
}

if (x ≤ mid1)

else if (x ≥ mid2)

else {

}



$$n \rightarrow \frac{n}{2} \rightarrow \frac{n}{4} \rightarrow \frac{n}{8} \dots \frac{n}{2^k} \quad \text{K elements}$$

$$\frac{n}{2^k} = 1$$

$$k = \log_2 n$$

total iterations of
B.S

total comp \rightarrow $\log_2 n$

$$n \rightarrow \frac{n}{3} \rightarrow \frac{n}{9} \rightarrow \frac{n}{27} \dots \frac{n}{3^m} \quad \text{m iterations}$$

$$\frac{n}{3^m} = 1 \rightarrow n = 3^m$$

Take \log_3 both sides

$$\log_3 n = m$$

Total iterations

Total comp in binary search $\Rightarrow \underline{\underline{2 \log_3 n}}$

$$\log_2 n$$

$$2 \log_3 n$$

you can convert the base

$$2 \log_3 n \rightarrow \frac{2 \log_2 n}{\log_2 3}$$

$$\log_2 3 \rightarrow \underline{\underline{1.585}}$$

$$\log_2 n$$

$$1 \times \log_2 n$$

$$\downarrow$$

$$< \frac{2}{\log_2 3} \times \log_2 n$$

$$1.26 \times \log_2 n$$

Hence, Binary Search is always br than ternary search
for big n .

$x \rightarrow$ ~~1234~~

Ans \rightarrow 4321.

Ans = Ans * 10 + last digit

4321
 \rightarrow 4000
 $+ 300$
 $+ 20$
 $+ 1$
