



**POLITECNICO**  
MILANO 1863

DEPARTMENT OF  
MECHANICAL ENGINEERING

# **ADVANCED DYNAMICS OF MECHANICAL SYSTEMS**

**Assignment 1 – Part B  
Experimental Modal Analysis  
of a light rail wheel**

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# TARGET

Identify the modal parameters of a real system through Experimental Modal Analysis.

## Contents:

- The structure under test
- Experimental setup
  - Constraints → how to fix the system
  - Input → how to excite the system
  - Output → what to measure
- Signal processing (FRF and coherence function)

# CONTEXT AND MOTIVATION

Railway noise can be regarded as environmental noise, resulting from the operation of rail vehicles.

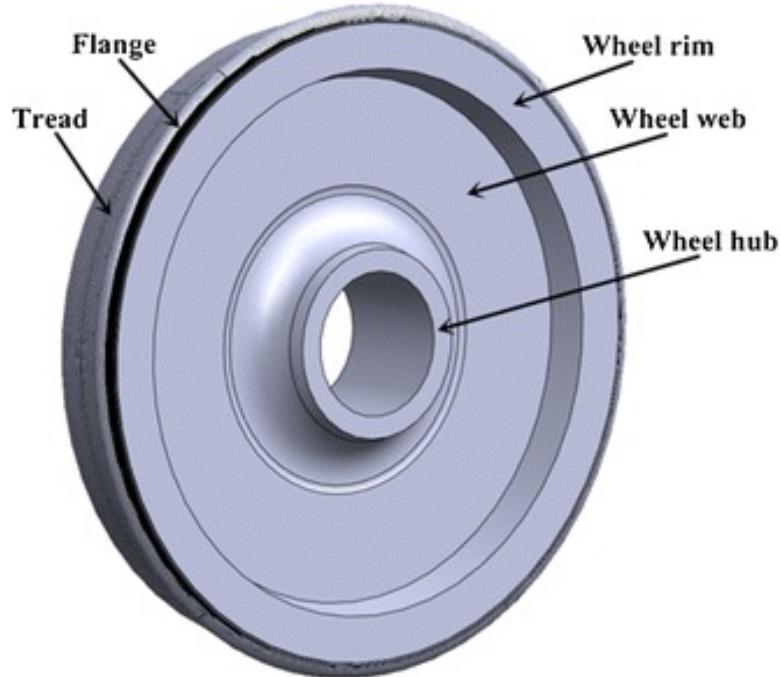
In many railway noise problems (especially rolling noise and curve squeal noise), the wheel plays a fundamental role in terms of sound radiation.

In particular, the axial vibration of the wheel surface results into efficient sound radiation (the surface vibration of the wheel induces a perturbation of the surrounding air and generates a consequent radiated sound field).



# THE STRUCTURE UNDER TEST

Resilient wheel of a light rail vehicle



Resilient wheel



Wheelset

# EXPERIMENTAL SETUP



## Constraints

Resilient wheel suspended through elastic supports  
(free-free system)

## Input

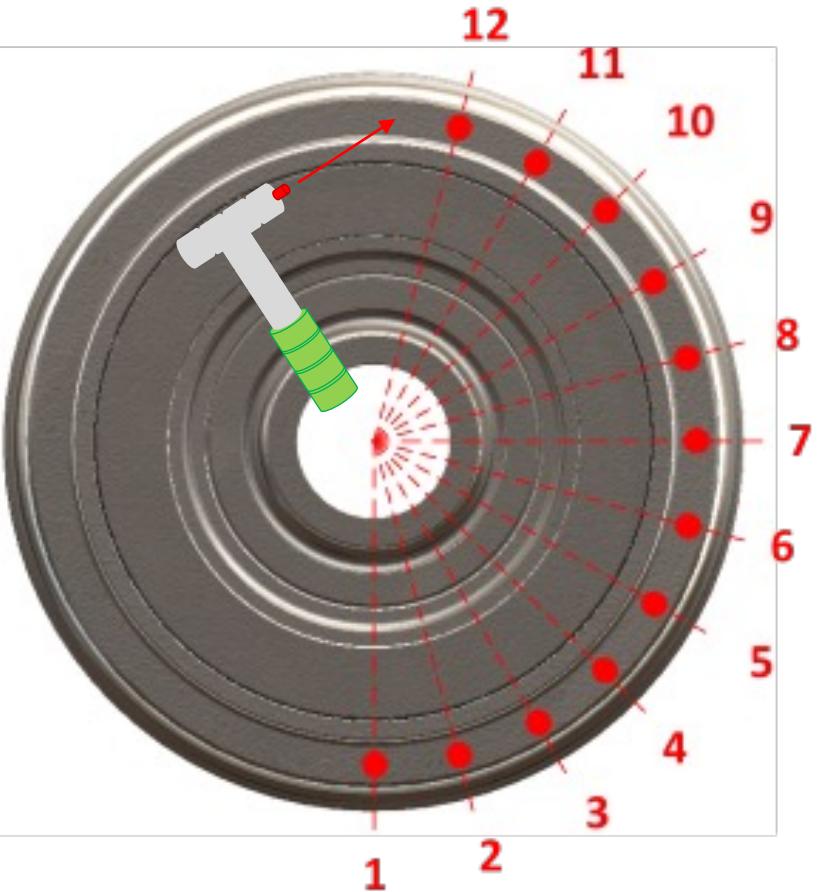
Dynamometric impact hammer applying an axial load

## Output

Piezoelectric accelerometers to sense the axial vibration of the wheel rim.

Due to the symmetry of the structure, 12 measurement positions have been considered, which are located only on half of the wheel, with a regular angular spacing of  $15^\circ$

# EXPERIMENTAL SETUP



## Constraints

Resilient wheel suspended through elastic supports  
(free-free system)

## Input

Dynamometric impact hammer applying an axial load

## Output

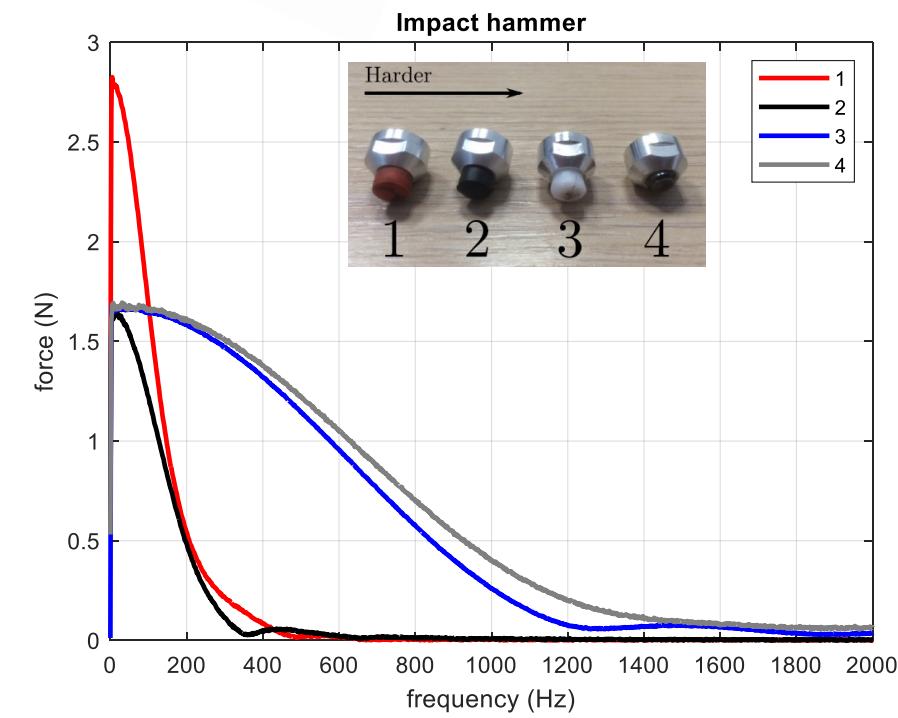
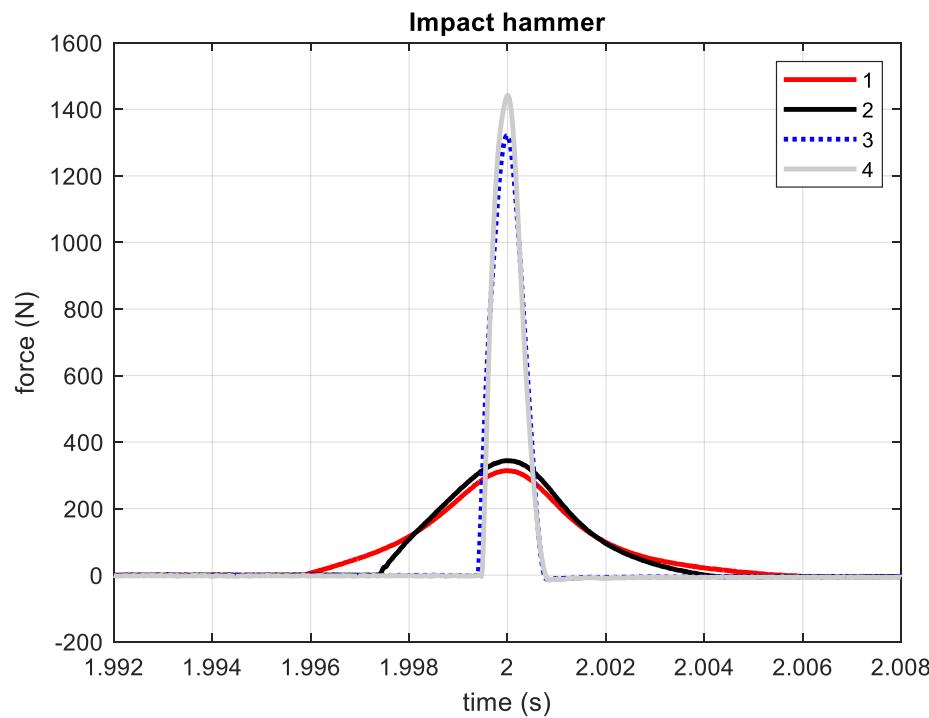
Piezoelectric accelerometers to sense the axial vibration of the wheel rim.

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# EXPERIMENTAL SETUP

## DYNAMOMETRIC IMPACT HAMMER

- Impulsive excitation excites all frequencies (theoretically)
- The bigger the hammer, the lower the frequency range
- The harder the tip, the higher the frequency range



# EXPERIMENTAL SETUP

## PIEZOELECTRIC ACCELEROMETER

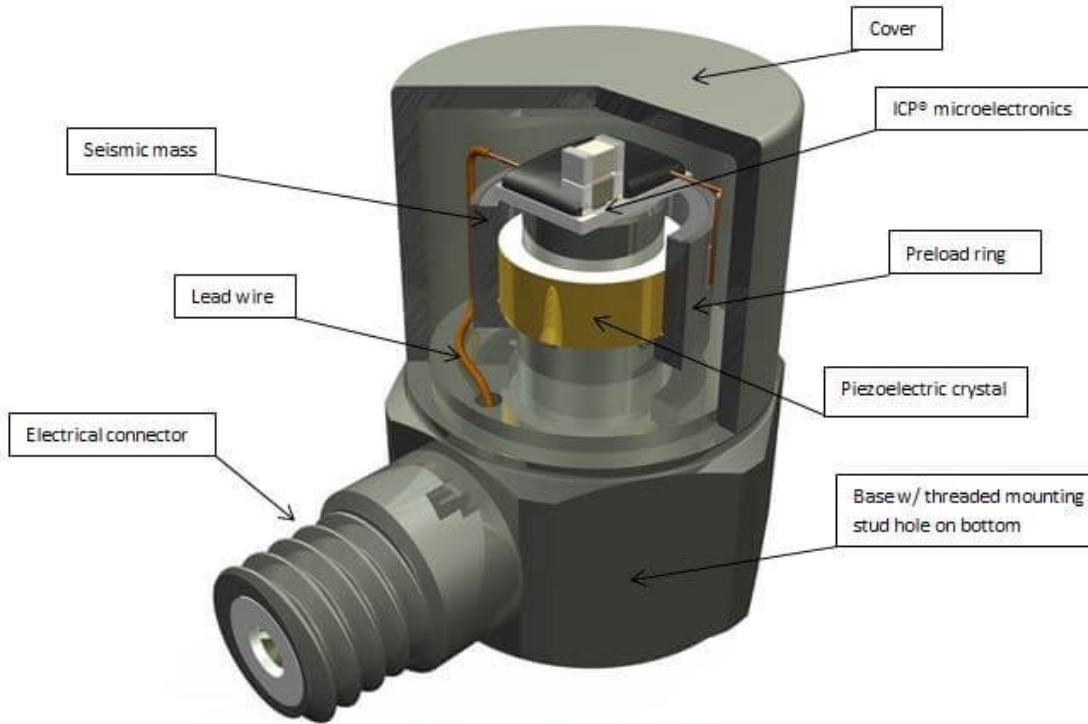


Figure 1: Typical ICP® Accelerometer

### Performance

Sensitivity( $\pm 10\%$ )  
Measurement Range

### ENGLISH

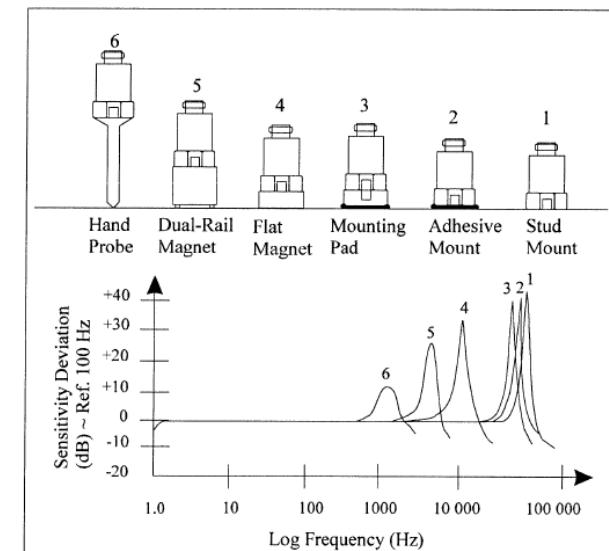
100 mV/g  
 $\pm 50$  g pk

### SI

10.2 mV/(m/s<sup>2</sup>)  
 $\pm 491$  m/s<sup>2</sup> pk

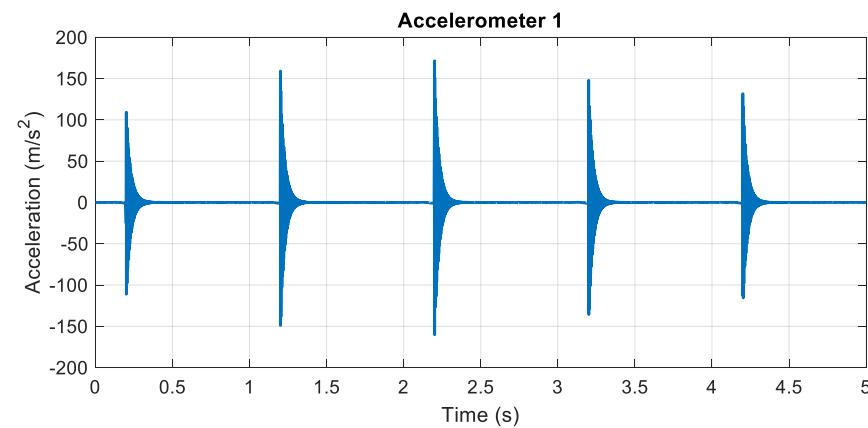
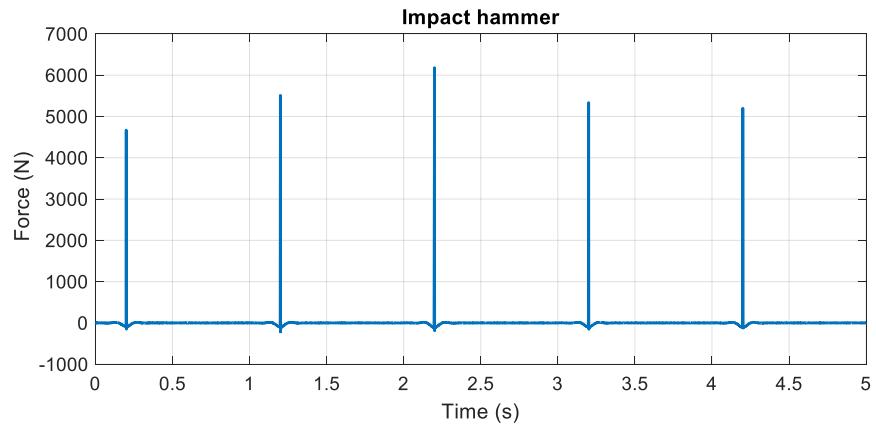
### Physical

Sensing Element	Ceramic
Sensing Geometry	Shear
Housing Material	Titanium
Sealing	Welded Hermetic
Size (Hex x Height)	9/32 in x 18.5 mm
Weight	2.0 gm
Electrical Connector	10-32 Coaxial Jack
Electrical Connection Position	Top
Mounting Thread	5-40 Male
Mounting Torque	90 to 135 N-cm

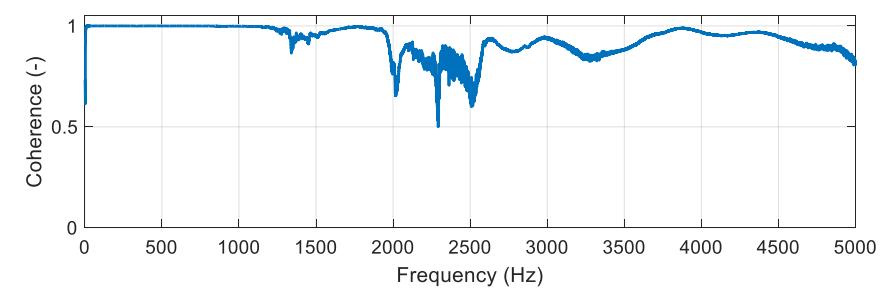
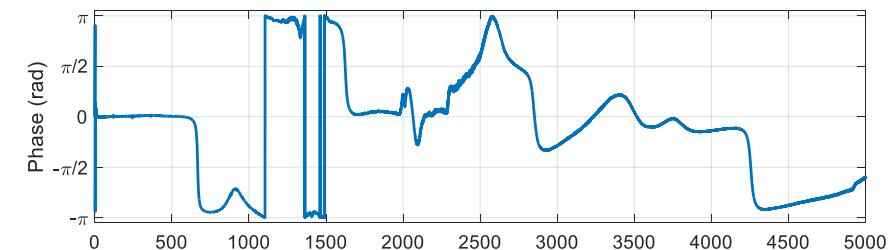
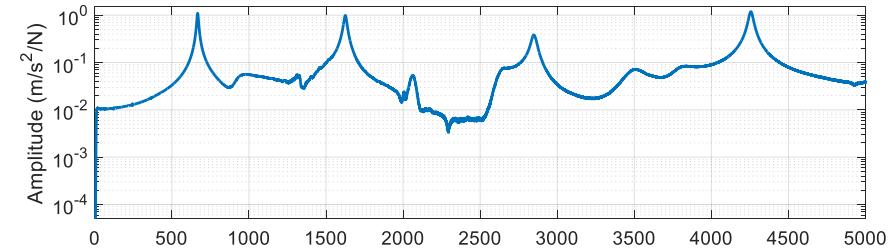


# SIGNAL PROCESSING

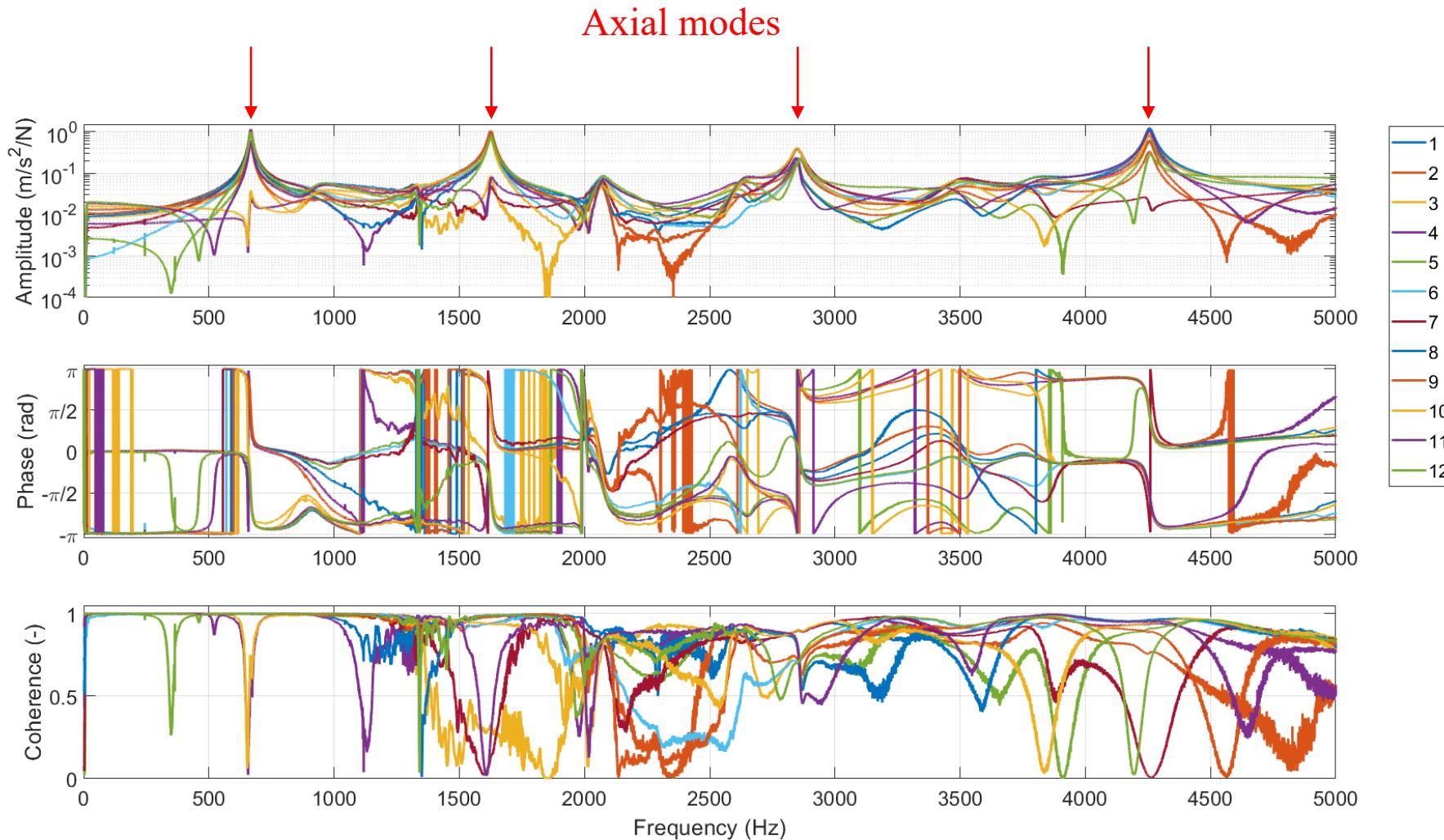
## Time histories



## Frequency Response Function



# EXPERIMENTAL FREQUENCY RESPONSE FUNCTIONS



# DATA PROVIDED

The provided Data.mat file contains the following variables:

- **freq** frequency vector (resolution 0.333 Hz)
- **frf** Inertance ( $m/s^2/N$ ) frequency response functions (complex)  
collected by columns according to the measuring grid shown in slide 6
- **cohe** coherence function, collected by columns

Hints to plot the identified mode shapes:

- Measuring grid with regular angular spacing of  $15^\circ$  → define an angular spatial domain
- Polar symmetry of the system → polarplot Matlab function

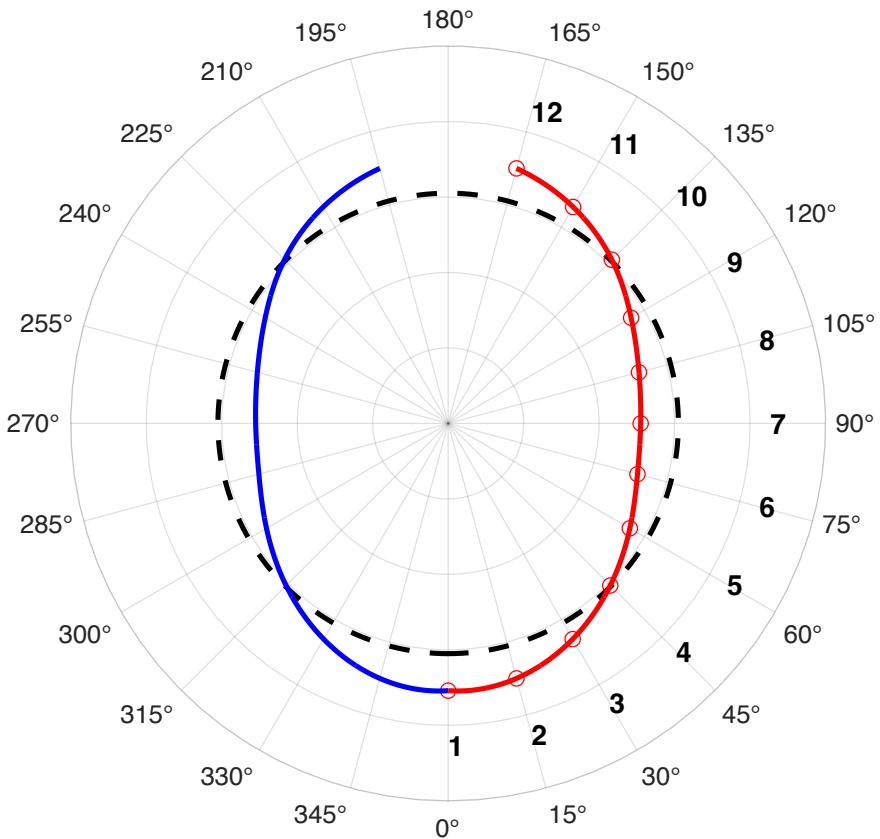
# ASSIGNMENT 1 – PART B

Work out the following items and include the corresponding results in your report of Assignment 1.

1. Apply the procedure developed within Part A to the provided experimental data, to identify the modal parameters (**natural frequencies, damping ratios and mode shapes**) of the first two axial modes.
2. Check the quality of the identification comparing the identified FRFs and the experimental ones.
3. Plot a diagram showing the identified mode shapes with the indication of the corresponding natural frequencies and damping ratios.

# MODE SHAPE IDENTIFICATION

1<sup>st</sup> axial mode



2<sup>nd</sup> axial mode

