

User's Manual

STUDY OF MAGNETIC LEVITATION SYSTEM

Model: ML-01

Manufactured by:

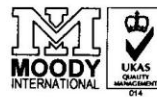
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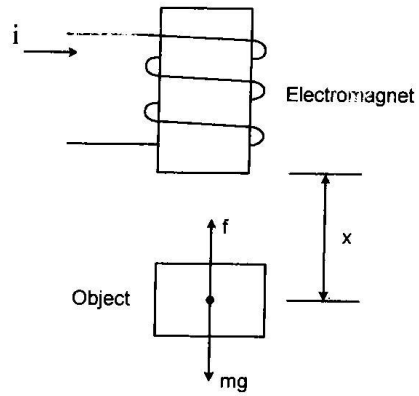


Fig.1 Basic System

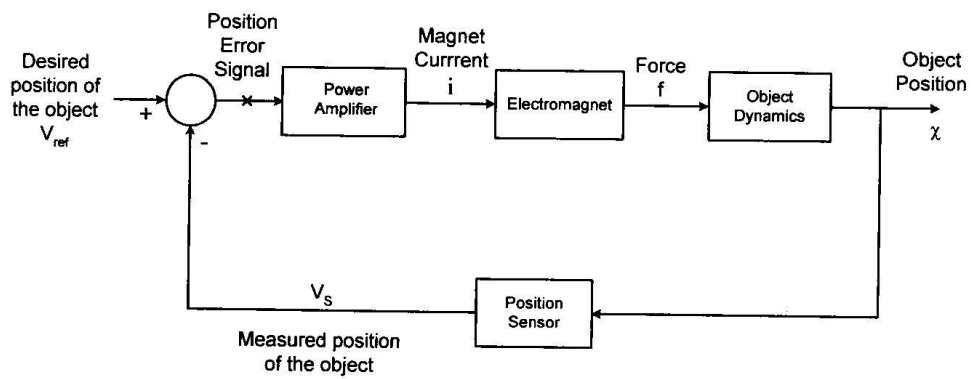


Fig.2 Automatic Scheme for Control

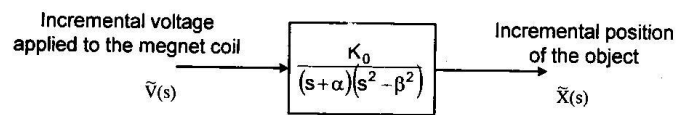


Fig.3 Open loop system model

STUDY OF MAGNETIC LEVITATION SYSTEM

1. OBJECT

Theoretical and experimental study of a magnetic levitation setup, an inherently unstable system.

2. BACKGROUND SUMMARY

The magnetic levitation system consists of an electromagnet which pulls an object (a magnetic material) in an upward direction, in the presence of downward gravitational force on it (Fig.1). If the magnet current i is adjusted to satisfy the condition, $f = mg$, the object should, at least theoretically, remain suspended in air. In a practical situation, however, even the smallest disturbance would dislocate the balance and the object would either stick to the magnet or fall down to ground. Logically therefore the current i needs to be continuously adjusted to keep the object freely suspended in air. This task is impossible to be achieved manually, and therefore needs a feedback control loop.

The basic feedback control scheme is shown in Fig.2. The idea here is to monitor the position of the object continuously and adjust magnet current automatically to ensure the upward force, f , exactly balances the weight of the object, mg , at all times. It will however be seen later that due to the unstable dynamics of the object, the automatic control scheme of Fig.2 is not workable and hence a more elaborate controller is required. A linearized model of the system is developed next.

2.1 System Model

The electromagnet pulls the object (iron ball) with a force,

$$f(x,i) = c \left(\frac{i}{x} \right)^2, \text{ and } c = \frac{L_0 x_0}{2} \quad \dots(1)$$

Here,

x is the distance between the magnet and the object

i is the current in the magnet coil

L_0 is the additional inductance of the magnet coil due to the object placed at the nominal position, $x = x_0$.

The equation of motion of the object is given by

$$m \ddot{x} = -c \left(\frac{i}{x} \right)^2 + mg, \text{ where} \quad \dots(2)$$

m is the mass of the object, and

g is the acceleration due to gravity.

A linearized form of the above equation may be derived as,

object
position
→
 x

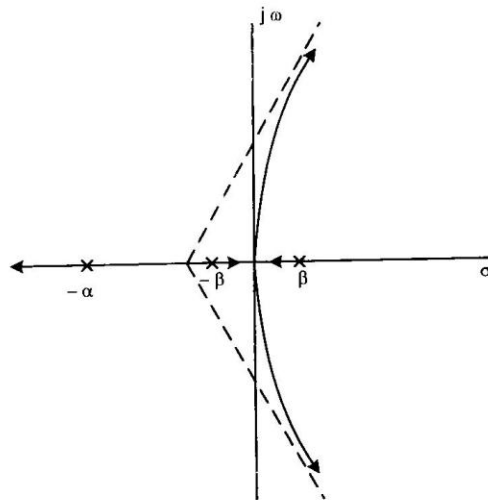


Fig.4 Root Locus with Proportional Controller

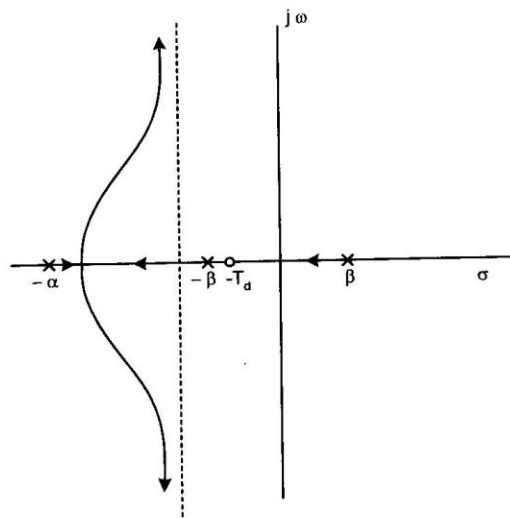


Fig.5 Root Locus with PD Controller

$$m \ddot{\tilde{x}}(t) = -c \left(\frac{i_0}{x_0} \right)^2 \left\{ 1 + 2 \left(\frac{\tilde{i}(t)}{i_0} - \frac{\tilde{x}(t)}{x_0} \right) \right\} + mg \quad \dots(3)$$

where, $\tilde{x}(t)$ and $\tilde{i}(t)$ are the incremental displacement and incremental magnet current around their nominal values, x_0 and i_0 . Since the object is assumed to be at rest at $x = x_0$ with $i = i_0$,

$$c \left(\frac{i_0}{x_0} \right)^2 = mg, \text{ which leads to}$$

$$m \ddot{\tilde{x}}(t) = - \frac{2i_0 c}{x_0^2} \cdot \tilde{i}(t) + \frac{2i_0^2 c}{x_0^3} \tilde{x}(t)$$

Taking Laplace transform and neglecting initial condition,

$$\frac{\tilde{X}(s)}{\tilde{I}(s)} = \frac{\frac{-2ci_0}{mx_0^2}}{s^2 - \frac{2ci_0^2}{mx_0^3}}, \quad \dots(4)$$

is obtained as the dynamics of the object.

The current – voltage relation of the magnet is given by

$$\tilde{v}(t) = R \tilde{i}(t) + L \frac{d\tilde{i}(t)}{dt}, \text{ where } \tilde{v}(t) \text{ and } \tilde{i}(t) \text{ are the incremental values of}$$

voltage applied to and the current flowing into the electromagnet, and R, L are the coil parameters. Taking Laplace transform and neglecting initial conditions,

$$\tilde{V}(s) = (R + sL) \tilde{I}(s), \text{ and}$$

combining the above equations, the system dynamics is given by the transfer function

$$\frac{\tilde{X}(s)}{\tilde{V}(s)} = G(s) = \frac{\frac{-2ci_0}{mLx_0^2}}{\left(s + \frac{R}{L}\right) \left(s^2 - \frac{2ci_0^2}{mx_0^3}\right)} = - \frac{K_0}{(s + \alpha)(s^2 - \beta^2)} \quad \dots(5)$$

2.2 Controller Scheme

The above equation may be represented by the block diagram of Fig. 3 which is the open loop system.

It is clear that the open loop system above is unstable, due to the plot at $s = \beta$, in the right half of the s-plane. Also, connecting a feedback loop on the line of Fig.2 will not lead to a stable closed loop system for any value of forward path gain as may be seen from the root locus diagram of Fig.4. This obviously is a proportional controller, which will not stabilize the system. In case however a proportional – derivative (PD) controller is used, the revised root locus diagram of Fig.5 indicates the possibility of stabilizing the system and also achieving good transient performance for some range of values of forward path gain.

The PD controller is assumed to have the transfer function, $G_c = (1 + T_d s)$

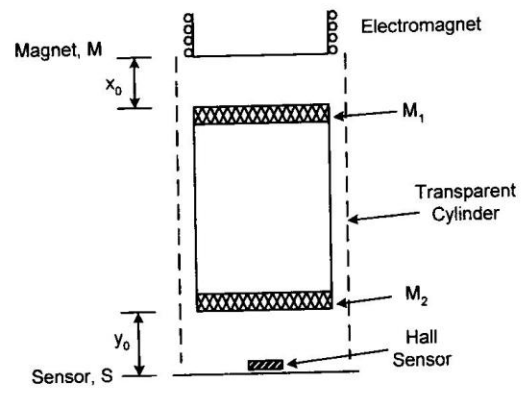


Fig.6 Mechanical Arrangement of the Object

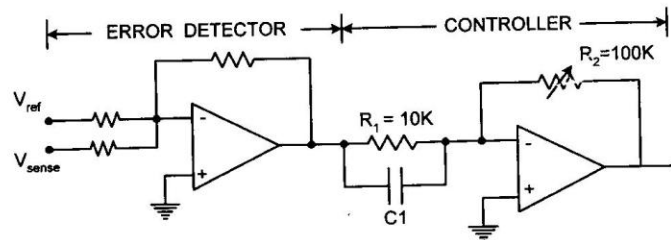


Fig.7 Electronic Circuit of the System

The present experiment involves determination of the system parameters, K_0 , α and β experimentally, and then to design T_d , the parameter of the controller and choose an appropriate gain.

2.3 Parameter determination

- (a) The value of α can be calculated from the magnet parameters, R and L , and using the expression $\alpha = R/L$.
- (b) Since the open loop system, eqn.(5) is unstable, no experimentation is possible directly on it. An alternative method is to use an adhoc setting of the PD controller to result in stability. Then the force balance equation, $c\left(\frac{i}{x}\right)^2 = mg$, is used to calculate an average value of c from measurements of i and x around the nominal equilibrium point i_0, x_0 . The mass of the object, m , is known beforehand.

The constant K_0 and β are then computed from

$$K_0 = \frac{2ci_0}{mLx_0^2} \text{ and } \beta = \sqrt{\left(\frac{2ci_0^2}{mx_0^3}\right)}$$

3. SYSTEM DESCRIPTION

The hardware involved in the various blocks of Fig.2 are described in this section.

3.1 Suspended Object

This comprises of two disc magnets M_1 and M_2 fixed on the two ends of a height plastic cylinder (Fig. 6). While M_1 is used for providing upward force to pull the object, M_2 is used for generating the necessary position information through the hall sensor fixed on the base. A cylinder made of plastic material ensures proper view and protected movement of the object. Note that our earlier analysis refers to iron as the suspended object, in the actual model a magnet M_1 is used. This ensures a better control when the object goes close to the electromagnet. Also since the thickness of a magnet is much smaller than x_0 , the calculation are not too much in error. Finally, since the system is highly non-linear and we are linearizing around the operating point x_0, i_0 , the whole analysis is reasonably accurate even for a magnet object.

3.2 Electromagnet

A powerful electromagnet is mounted on the top of the guide rod. It exerts variable attraction force on M_1 depending on the current supplied to it. The second magnet M_2 , being farther away, is assumed to have a negligible effect on the force. The electromagnet is characterised by its winding resistance R and inductance L .

3.3 Power Amplifier

It is a complementary symmetry power amplifier having an internal gain of 2, and capable of providing up to 3 amp. to the electromagnet. The external gain of the circuit may be varied from 1 to 11 using the potentiometer on the panel.

3.4 Position Sensor

It is a hall effect device, which generates an electrical signal proportional to its distance from M_2 . The sensor output is thus a measure of the position of the suspended object. Note that due to the highly non-linear nature of the overall system, we are basically concerned with small deviations around the equilibrium point. This enables us to represent the sensor as a constant gain for computation purposes.

3.5 Error detector and controller

The circuit diagram of this section is shown in Fig. 7. It performs the tasks of,

- (i) Placing the object to a suitable position which may be taken as the 'nominal position'. This is done by adjusting the reference signal, V_{ref} .
- (ii) Providing a PD controller to ensure system stability, and a simple calculation shown the controller transfer function to be, $\frac{R_2}{R_1} \cdot (1 + s R_1 C_1)$.
- (iii) Setting the forward path gain to an appropriate value.

4. EXPERIMENTS AND RESULTS

The experiments conducted on a typical unit and the results are described below in some detail. The student is expected to repeat the steps on the unit available to him and go through the design. Actual results are likely to be somewhat different in each case.

4.1 System Identification

Standard Parameter values of this unit are:

Magnet Inductance, $L = 8.1 \times 10^{-3} \text{ H} \rightarrow 8.1 \times 10^{-3} \text{ H}$

Magnet Resistance, $R = 4.7 \Omega \rightarrow 4.7 \Omega$

Mass of the Object, $m = 10 \times 10^{-3} \text{ Kg}$ ✓

- (a) Based on the parameters of the magnet, the time constant of the coil may be calculated as,

$$\alpha = \frac{4.7}{8.1 \times 10^{-3}} = 580.24 \text{ sec}^{-1} \rightarrow 580.24 \text{ sec}^{-1}$$

- (b) The steps below are now followed to determine the remaining parameters.

Step.1 Connect the PD controller ($C_1 = 2\mu\text{F}$) and close the feedback loop. Set forward gain to a medium value say 4. The object should now be suspended freely in air by adjusting V_{ref} .

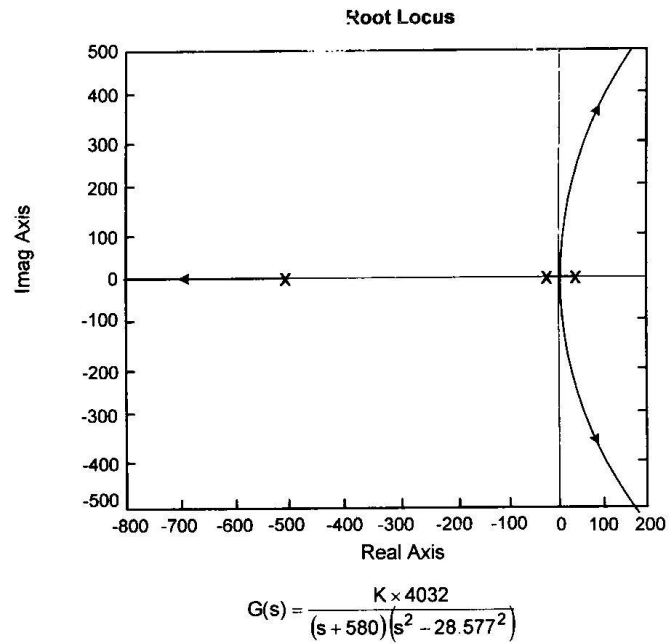


Fig. 8 Root Locus Diagram of the Uncompensated System

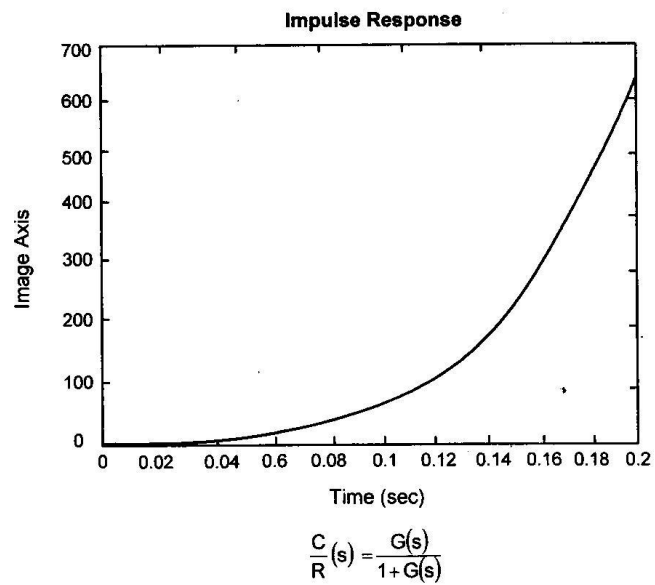


Fig. 9 Impulse Reponse of the uncompensated System

Step.2 Adjust the reference input to move the object in the gap between the magnet and the sensor. This is the nominal position of the object [x_0 is the distance between the object (top marker) and the electromagnet, M and i_0 is the electromagnet current.]

Step.3 Record x_0 , i_0 and calculate c . The mass of the object,

$$m = 10 \times 10^{-3} \text{ Kg (Specified by the manufacturer)}$$

$$x_0 = 24 \text{ mm} = 0.024 \text{ m}$$

$$i_0 = 1.20 \text{ amp}$$

$$c = mg \left(\frac{x_0}{i_0} \right)^2 = 10 \times 10^{-3} \times 9.8 \times \left(\frac{0.024}{1.20} \right)^2 = 3.92 \times 10^{-3}$$

Step.4 Compute K_0 and β as,

$$K_0 = \frac{2ci_0}{mLx_0^2} = \frac{2g}{Li_0} = \frac{2 \times 9.8}{8.1 \times 10^{-3} \times 1.20} = 2016$$

$$\beta = \sqrt{\frac{2ci_0^2}{mx_0^3}} = \sqrt{\frac{2g}{x_0}} = \sqrt{\frac{2 \times 9.8}{0.024}} = 28.577$$

Step.5 The transfer function of the system at the nominal position is now written explicitly as

$$G(s) = - \frac{2 \times 2016 \times 10^{-3}}{(s + 580)(s^2 - 28.577^2)} \quad (\text{Internal gain of power amplifier} = 2)$$

The forward path transfer function may therefore be written as

$$K.G(s) = - \frac{K \times 4032}{(s + 580)(s^2 - 28.577^2)}$$

Where K is adjustable between 1 and 11 as explained in section 3.3

Step.6 Feedback path gain (sensor gain) at the nominal position is found by displacing the object slightly around the nominal position (say $\pm 3\text{mm}$) and monitoring the change in sensor output.

$$(i) y_0 = 17 \text{ mm} \quad \text{Sensor output, } V_s = 3.17 \text{ V}$$

$$(ii) y_0 + \Delta y = 21 \text{ mm} \quad \text{Sensor output, } V_s - \Delta V_s = 2.86 \text{ V}$$

$$\text{Sensor gain } K_s = \frac{\Delta V_s}{\Delta y_0} = 77.5 \text{ V/m}$$

The feedback path transfer function may therefore be written as

$$H(s) = 77.5$$

Step.7 Sketch the root locus diagram from the transfer function obtained in Step. 5 and 6 using MATLAB or otherwise, as shown Fig.8. Instability of the closed loop system for all values of open loop gain is obvious, and may also be verified through an impulse response plot as in Fig. 9.

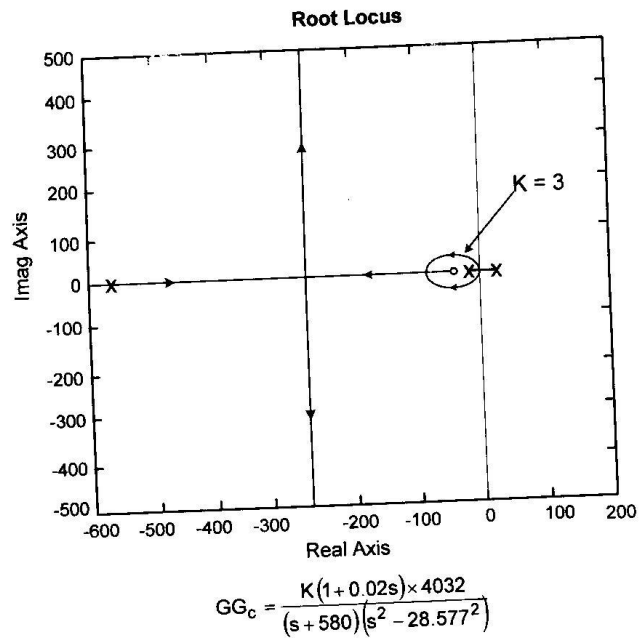


Fig. 10 Root Locus Diagram of the Compensated System

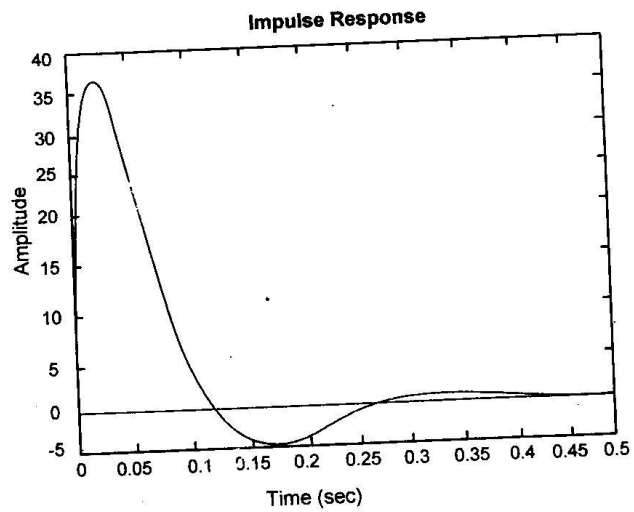


Fig. 11 Impluse Response of the Closed Loop System with K = 3

Note that since the system has a non-unity feedback path transfer function, the root locus plot must take this into account. Sample MATLAB commands for this purpose are listed below.

```
s=tf('s') (3.972)/(15+569)*(5^2-24^2)
g=(4032)/((s+580)*(s^2-28.577^2));
h=77.5 336.6 230
gh=g*h
rlocus(gh)
impz(((gh)/(1+gh)), 2);
```

Step.8 Choose a suitable closed loop pole location (P) and design a PD controller. A good choice may be a zero at $S = -50$. The compensator transfer function, $G_C = (1+0.02s) = 0.02(s+50)$. With $R_1 = 10K\Omega$ (internal), the value of compensator capacitance is $C_1 = 2\mu F$. A revised root locus diagram may be drawn as shown in Fig. 10. Note that the system is now stable for $K > 1.5$. Impulse response plot for $K = 3$ is shown in Fig. 11

MATLAB command:

```
gc=((1/50)*(s+50))
rlocus(gh*gc)
impz(((3*gh*gc)/(1+3*gh*gc)), 0:0.001:5)
```

Calculate and connect the designed value of capacitor on the panel and operate the system with the computed value of the forward path gain.

A careful observation of the root locus of Fig.10 would show that the system could be stabilized by using a wide range of capacitors. This may be verified experimentally.

Also it might appear that large values of K would be preferred in all cases. This however is not true in the practical situation due to the saturation of the amplifier.

5. FURTHER WORK

The experimental unit provides the user with an interesting platform to conduct further experimental work. This however is most conveniently done with the support of MATLAB. Some suggestions are:

- Simulate different PD controllers on MATLAB check the root locus diagram impulse response their effect on the unit.
- Attempt lead compensator design and implement it.

Note: Do not expect the experimental performance to match exactly with theoretical prediction. While the theoretical work is valid for linear system only, the experimental system is a non-linear one, which has been approximated as a linear system for small variation around the operating point.

REFERENCE

- [1] Franklin GF, JD Powell and Michael Workman, "Digital Control of Dynamic System", Addison Wesley, 2000
- [2] Shiao YS, "Design and Implementation of a controller for a Magnetic Levitation System", Proc. Natl. Sci.Comc. ROC(D), Vol. II, No. 2, 2001, pp. 88-94