

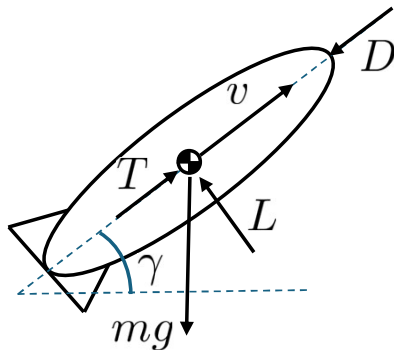
The nonlinear dynamics of a shuttle during the climb are described by these four coupled differential equations:

$$m\dot{v} = T - C_D v^2 - mg \sin \gamma$$

$$m\dot{\gamma}v = C_L v^2 - mg \cos \gamma$$

$$\dot{h} = v \sin \gamma$$

$$\dot{m} = -\alpha T$$



\*rotational inertia negligible

$$x_1 = h \quad \text{Altitude}$$

$$x_2 = v \quad \text{Velocity}$$

$$x_3 = m \quad \text{Mass (varies with the fuel consumption)}$$

$$x_4 = \gamma \quad \text{Flight angle}$$

$$u = T \quad \text{Thrust (control input)}$$

$$C_D, C_L \quad \text{Drag and Lift Coefficients (constant)}$$

$$\alpha \quad \text{Constant related to fuel consumption}$$

$$\dot{x}_1 = x_2 \sin x_4$$

$$\dot{x}_2 = \frac{u(t)}{x_3} - \frac{C_D x_2^2}{x_3} - g \sin x_4$$

$$\dot{x}_3 = -\alpha u(t)$$

$$\dot{x}_4 = \frac{C_L x_2}{x_3} - \frac{g \cos x_4}{x_2}$$

Define a nonlinear control problem and solve it through **direct** methods.

Feel free to consider additional control actions or introduce additional features/dynamics