

# Chip Scale Atomic Clocks Sources

Working principles

---

Tommaso Bocchietti

March 20, 2024

University of Waterloo

**API** Application Programming Interface

**LAN** Local Area Network

**ASCII** American Standard Code for Information Interchange

## Toolbox

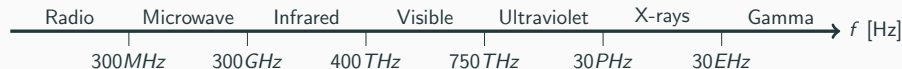
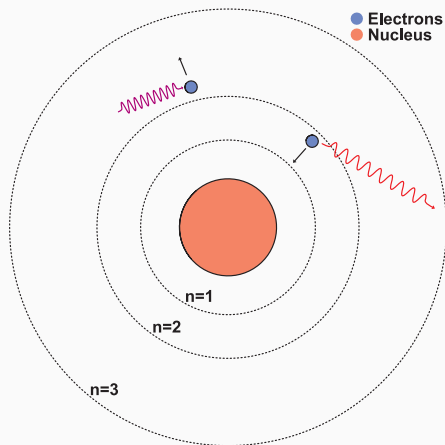
---

# Energy quantization

Energy is a quantized quantity.  
The energy of a photon is given  
by the **Planck's relation**:

$$e = hf \quad (1)$$

Unit of energy: electron-volt  
(eV) or Joule (J).



# Rubidium and Cesium

We will deal with Rubidium (isotopes  $^{85}\text{Rb}$  &  $^{87}\text{Rb}$ ) and Cesium ( $^{133}\text{Cs}$ ).

- They are both alkali metals with a single valence electron.
- Their first ionization energy is low.

## Rb

### Rubidium

Atomic number  
protons / electrons

**37**

Electron Affinity  
[kJ/mol]

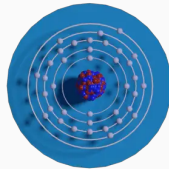
**46.9**

Electronegativity  
(Pauling scale)

**0.82**

Ionization Energy  
[eV]

**4.177**



[Kr] 5s1

7s ☐ 7p ☐☐☐  
6s ☐ 6p ☐☐☐ 6d ☐☐☐☐  
5s ☒ 5p ☐☐☐ 5d ☐☐☐☐ 5f ☐☐☐☐  
4s ☒ 4p ☒☒☒ 4d ☐☐☐☐ 4f ☐☐☐☐  
3s ☒ 3p ☒☒☒ 3d ☒☒☒  
2s ☒ 2p ☒☒  
1s ☒

## Cs

### Caesium

Atomic number  
protons / electrons

**55**

Electron Affinity  
[kJ/mol]

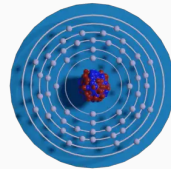
**45.5**

Electronegativity  
(Pauling scale)

**0.79**

Ionization Energy  
[eV]

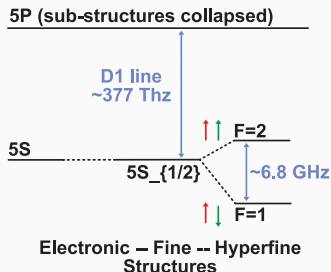
**3.894**



[Xe] 6s1

7s ☐ 7p ☐☐☐  
6s ☒ 6p ☐☐☐ 6d ☐☐☐☐  
5s ☒ 5p ☒☒☒ 5d ☐☐☐☐ 5f ☐☐☐☐  
4s ☒ 4p ☒☒☒ 4d ☒☒☒☒ 4f ☐☐☐☐  
3s ☒ 3p ☒☒☒ 3d ☒☒☒  
2s ☒ 2p ☒☒  
1s ☒

# Quantum levels



**Figure 1:**  $^{87}\text{Rb}$  quantum levels.

**Elementary energy level ( $n = 1, 2, 3, \dots$ ), can further be split.<sup>1</sup>**

Substructures are due to various quantum phenomena acting inside the atom domain.

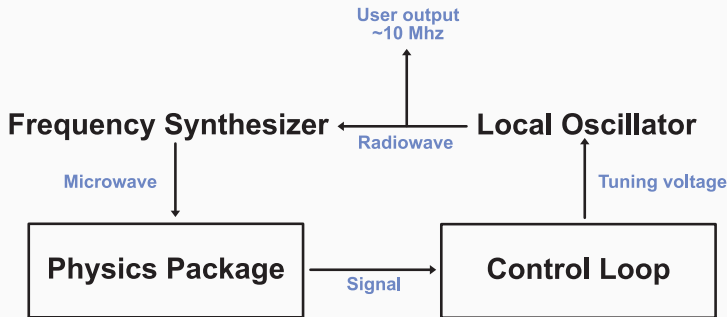
- Electronic: classical orbital levels.
- Fine: electronic spin-orbit coupling.
- Hyperfine: **nuclear spin-electron spin** coupling.

<sup>1</sup>For the purpose of the CSACs, we can consider the sub-5P structures as collapsed into a single one.

# CSAC Block Diagram

---

# Block diagram of a generic CSAC



In the following slides, we are going to see:

- Physics Package
  - Based on Microwave Optical Double-Resonance (MODR)
  - Based on Coherent Population Trapping (CPT)
- Control loop
- Local Oscillator

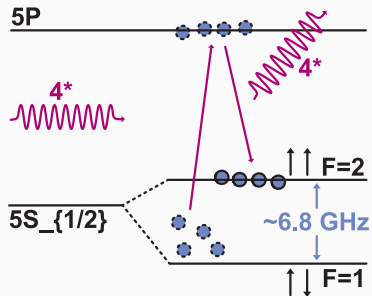


**Physics Package based on  
Microwave Optical  
Double-Resonance (MODR)**

---

# $^{87}\text{Rb}$ Reference Cell

At the heart of a MODR based CSAC, we find a  $^{87}\text{Rb}$  reference cell.



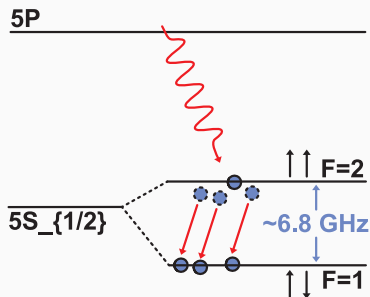
We can distinguish 3 phases:

1. Optical Pumping (Population Inversion)

Ground state population  $F = |1\rangle$  gets pumped to  $F = |2\rangle$ .

# $^{87}\text{Rb}$ Reference Cell

At the heart of a MODR based CSAC, we find a  $^{87}\text{Rb}$  reference cell.



We can distinguish 3 phases:

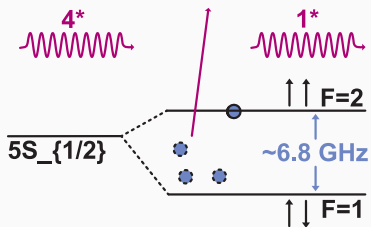
1. Optical Pumping (Population Inversion)
2. Microwave Excitation

Microwave tuned at the atomic resonance frequency ( $\approx 6.8 \text{ GHz}$ ) brings part of the population back to  $F = |1\rangle$ .

# $^{87}\text{Rb}$ Reference Cell

At the heart of a MODR based CSAC, we find a  $^{87}\text{Rb}$  reference cell.

5P



We can distinguish 3 phases:

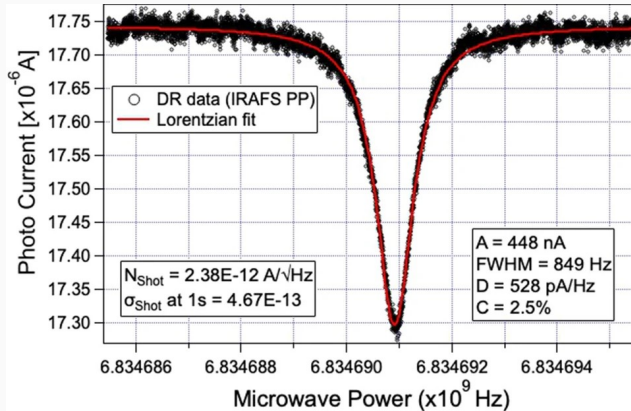
1. Optical Pumping (Population Inversion)
2. Microwave Excitation
3. Optical Pumping (Interrogation)

Depending on the intensity of the transmitted radiation, **we can infer if the microwave frequency was on resonance or not.**

In this case, given that one photon was able to go through the cell, we can infer that the microwave frequency was not in resonance.

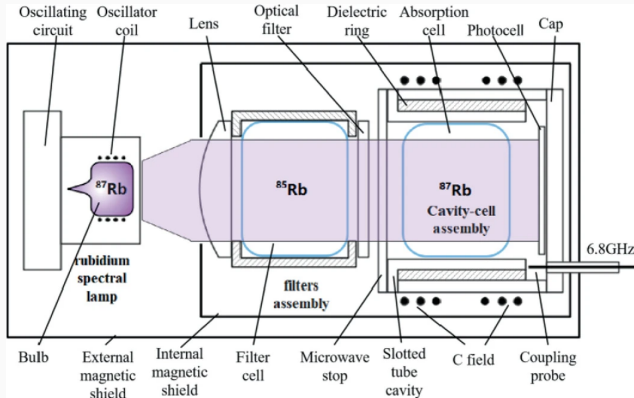
# Photodetection

At the end of the cell, a photodiode is used to measure the intensity of the transmitted radiation.



Our target is to stay at the dip of the transmission curve.

# Complete physics package for a MODR-based CSAC



Other notable components are:

- $^{87}\text{Rb}$  Bulb: high frequency radiation source.
- $^{85}\text{Rb}$  Filter cell: because of overlapping hyperfine levels, it filters out the unwanted transitions frequencies from the lamp.
- Microwave cavity: enhances the interaction between radiation and atoms.

*...goal of developing an ultra-miniaturized, low-power, atomic time and frequency reference units...*

In case of a MODR-based CSAC, we can recognize multiple problematic areas:

- Power consumption: each component inside the physics package is usually oven controlled (70% of the total power consumption).
- Size: microwave cavity imposes a low limit ( $L_{min} = \frac{c}{2f_{transition}} \approx 2.2cm$ ).
- Optical instabilities<sup>1</sup>: Stark shifts, Zeeman effects, internal wall gas collision.

---

<sup>1</sup>More on this in the "Extra slides" section.

# **Physics Package based on Coherent Population Trapping (CPT)**

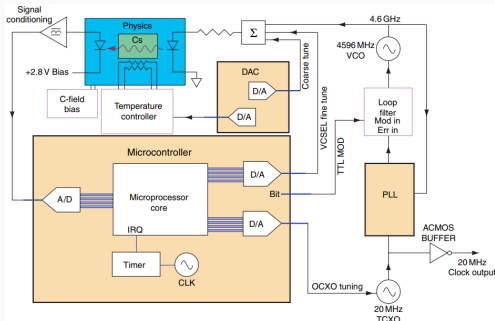
---



## Control loop

---

# Control loop



**Figure 2:** Control loop block diagram.

Close-loop control approach.  
Usually multiple PI controllers are used to operate a series of servo loops.

Indispensable targets:

- Laser temperature
- Cell temperature
- Laser frequency
- LO frequency

Here are some possible problematic areas:

- Stability in the voltage and current provided to VCO and VCSEL (highly sensitive components)
- Cross-talk between the various control loops
- Noise from the electronics
- Power consumption

## Local Oscillator

---

Normally, the local oscillator in a CSAC is a quartz crystal oscillator (XO).

There exist many versions of the XO, differentiated based on the environmental correction type applied to enhance stability:

- TCXO: Temperature Compensated Crystal Oscillator
- MCXO: Microcomputer Compensated Crystal Oscillator
- OCXO: Oven Controlled Crystal Oscillator

**At short time scales, the quartz crystal oscillator is the main source of instability** in a CSAC due to its phase noise.

Here are some other problematic areas:

- High temperature sensitivity
- Power consumption (in case of temperature compensation or oven control)
- Aging and frequency drift

In the end, the choice of a local oscillator is a trade-off between stability and power consumption.



DARPA.

**Atomic clock with enhanced stability (aces).**

<https://www.darpa.mil/program/atomic-clock-with-enhanced-stability>.



DARPA.

**Darpa chip-scale atomic clocks aboard international space station.**

<https://phys.org/news/2012-03-darpa-chip-scale-atomic-clocks-aboard.html>.



GISGeography.

**How gps receivers work - trilateration vs triangulation.**

<https://gisgeography.com/trilateration-triangulation-gps/>.



J. Kitching.

**Time for a better receiver: Chip-scale atomic frequency references.**

(18), 2007-11-01 2007.



B. L. S. Marlow and D. R. Scherer.

**A review of commercial and emerging atomic frequency standards.**

*IEEE Transactions on Ultrasonics, Ferroelectrics, and Frequency Control*,  
68(6):2007–2022, 2021.



Microchip.

**Microchip technology inc. (website).**

<https://www.microsemi.com/>.



Questions?

**Thank you!**