Chapter 4 Conclusion

Estimation of the Mean μ

 σ known

$$\mu \in \left[\overline{x} \ \pm \ \frac{\sigma}{\sqrt{n}} Z_{1-\frac{\alpha}{2}} \right]$$

• σ unknown and n > 30

$$\mu \in \left[\overline{x} \pm \frac{s}{\sqrt{n}} Z_{1-\frac{\alpha}{2}} \right]$$

• σ unknown and n < 30

$$\mu \in \left[\overline{x} \pm \frac{s}{\sqrt{n}} T_{\left(n-1,1-\frac{\alpha}{2}\right)} \right]$$

Estimation of the difference between two Means $\mu_1 - \mu_2$

• σ_1^2 and σ_2^2 knowns

$$\mu_{1} - \mu_{2} \in \left[\left(\overline{x} - \overline{y} \right) \pm \sqrt{\frac{\sigma_{1}^{2}}{n_{1}} + \frac{\sigma_{2}^{2}}{n_{2}}} Z_{1 - \frac{\alpha}{2}} \right]$$

• σ_1^2 and σ_2^2 unknowns and $n_1, n_2 > 30$

$$\mu_1 - \mu_2 \in \left[\left(\overline{x} - \overline{y} \right) \pm \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} Z_{1 - \frac{\alpha}{2}} \right]$$

• σ_1^2 and σ_2^2 unknowns and $n_1, n_2 < 30$

$$S_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

$$\mu_1 - \mu_2 \in \left[\left(\overline{x} - \overline{y} \right) \pm S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}} T_{\left(n_1 + n_2 - 2, 1 - \frac{\alpha}{2}\right)} \right]$$

Estimation Proportion P

$$P \in \left[\hat{P} \pm \sqrt{\frac{\hat{P}\hat{q}}{n}} Z_{1-\frac{\alpha}{2}} \right]$$

Estimation of the difference between two Proportions

$$P_1 - P_2$$

$$P \in \left[\left(\widehat{P_1} - \widehat{P_1} \right) \pm \sqrt{\frac{\widehat{P_1}\widehat{q_1}}{n_1} + \frac{\widehat{P_2}\widehat{q_2}}{n_2}} Z_{1 - \frac{\alpha}{2}} \right]$$

Estimation of σ^2

$$\frac{(n-1)S^{2}}{\chi_{1-\frac{\alpha}{2}}^{2}} \leq \sigma^{2} \leq \frac{(n-1)S^{2}}{\chi_{\frac{\alpha}{2}}^{2}}$$

Estimation of $\,\sigma\,$

$$\sqrt{\frac{(n-1)S^2}{\chi_{1-\frac{\alpha}{2}}^2}} \le \sigma \le \sqrt{\frac{(n-1)S^2}{\chi_{\frac{\alpha}{2}}^2}}$$