

Optimizing compiler

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Commercial uses: Going functional on exotic trades

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- Simon Frankau, Diomidis Spinellis, Nick Nassuphis, Christoph Burgard. *Commercial Uses: Going Functional on Exotic Trades*. J. Funct. Program. 19, 1, 27–45.
- Tim Williams. *Exotic Tools for Exotic Trades* @ CodeMesh 2013.
- Tim Williams, Peter Marks. *Structural Typing for Structured Products* @ Haskell Exchange 2014.

Why not Haskell?

- Haskell is an amazing language for writing your own compiler.
- A rich ecosystem of libraries dedicated to compiler-related tasks.
- A really powerful type system that can eliminate large classes of errors at compile time.
- Many excellent educational resources for compiler writers:
 - Stephen Diehl. *Write You a Haskell*.
 - Andres Löf, Conor McBride, Wouter Swierstra. *A Tutorial Implementation of a Dependently Typed Lambda Calculus*.
- Compilers, written in Haskell: GHC, Elm, Purescript, Idris, Agda...

SIMPL — Simple IMPerative Language

- Scalar and vector Double-valued variables: `a`, `b[i]`, `c[i][j]`.
- Vector length is statically known beforehand.
- Arithmetic operators, comparisons and ternary operator.
- Only `for`-loops without preliminary `break`.
- Basically, its computational power is equivalent to Excel sheet.
- Powerful enough for physical/financial Monte-Carlo simulations with calculations repeated over random inputs and step-by-step time.

Why not Fortran?

Example: *n*-body problem, youtube.com/embed/qlVe_xEv6zQ

- $m[i]$ is the mass of i -th object (is known in compile time),
- $x[i]$ and $y[i]$ are its coordinates,
- $vx[i]$ and $vy[i]$ are its velocities by X- and Y-axis,
- $ax[i]$ and $ay[i]$ are its accelerations.

```
dt = 0.001; G = 6.67e-11
```

```
foreach i in 1..n
```

```
    ax[i] = 0
```

```
    ay[i] = 0
```

```
    foreach j in 1..n
```

```
        d[i][j] = (x[i] - x[j]) ^ 2 + (y[i] - y[j]) ^ 2
```

```
        ax[i] = ax[i] - G * m[j] * (x[i]-x[j]) / d[i][j] ^ 3/2
```

```
        ay[i] = ay[i] - G * m[j] * (y[i]-y[j]) / d[i][j] ^ 3/2
```

```
foreach i in 1..n
```

```
    vx[i] = vx[i] + ax[i] * dt
```

```
    vy[i] = vy[i] + ay[i] * dt
```

```
    x[i] = x[i] + vx[i] * dt
```

```
    y[i] = y[i] + vy[i] * dt
```

Abstract syntax tree: types

Loop counters and variables are annotated with sizes on type level.

```
data Counter (range :: Nat) = Counter String
```

```
data Reference (arity :: [Nat]) where
```

```
  V      :: String -> Reference xs
```

```
  (!)    :: Reference (x : xs) -> Counter x -> Reference xs
```

```
data Expr a where
```

```
  Ref    :: Reference '[] -> Expr Double
```

```
  Num    :: Double -> Expr Double
```

```
  (:+)   :: Expr Double -> Expr Double -> Expr Double
```

```
  (:*)   :: Expr Double -> Expr Double -> Expr Double
```

```
  (:^)   :: Expr Double -> Expr Double -> Expr Double
```

```
  (:<)   :: Expr Double -> Expr Double -> Expr Bool
```

```
  If     :: Expr Bool -> Expr a -> Expr a -> Expr a
```

```
data Stmt where
```

```
  (:=)   :: Reference '[] -> Expr Double -> Stmt
```

```
  For    :: Counter x -> [Stmt] -> Stmt
```

Abstract syntax tree: utils

```
instance Num (Expr Double) where
  (+) = (:+)
  (*) = (:*)
  negate x = x :* (-1)
  abs x     = If (x :< 0) (negate x) x
  signum x = If (x :< 0) (-1) (If (0 :< x) 1 0)
  fromInteger = Num . fromInteger
```

```
(&&) :: Expr Bool -> Expr Bool -> Expr Bool
a && b = If a b a
```

```
(||) :: Expr Bool -> Expr Bool -> Expr Bool
a || b = If a a b
```


Code example

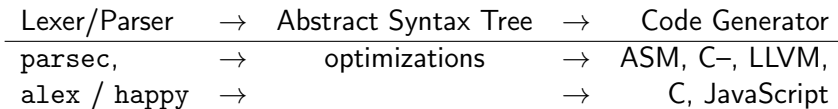
Return the sum of squares of $[c, c+1\dots]$.

```
[ For i
  [ a!i := Ref c
    , c  := Ref c + 1 ]
, For i
  [ b!i := Ref (a!i) :^ 2 ]
, ret   := 0
, For i
  [ ret := Ref ret + Ref (b!i) ] ]
where a = "a"; b = "b"; c = "c"; ret = "ret"; i = "i"
```

Optimized:

```
[ ret   := 0
  For i
    [ ret := Ref ret + Ref c :^ 2
      , c  := Ref c + 1 ]
where c = "c"; ret = "ret"; i = "i"
```

Compiler's architecture



Semantically:

- Lexer reads a list of tokens.
- Parser transforms tokens into syntax tree.

Grammars:

- Lexer reads a regular grammar (regex without backtracking).
- Parser reads a context-free grammar (can parse nested brackets).
- parsec can read even a context-sensitive grammar.

Static advantages:

- Lexer generates a very efficient finite automaton.
- Parser checks grammar for ambiguities.

Gentle optimizations

We are interested in optimizations of SIMPL such that

- no auxiliary statements or variables are introduced,
- expressions are replaced with equivalent in runtime ones.

We cannot:

- dismantle expressions into three-address code:
 $x = y * 3 + 2 \not\Rightarrow t = y * 3; x = t + 2.$
- dismantle loops into blocks, labels and gotos;
- use Single Static Assignment or Continuation Passing Style.

We are free to

- rewrite expressions;
- eliminate dead statements;
- shuffle statements both top-down and inside-out;
- detect high-level patterns such as maps and folds.

Despite SIMPL is an imperative language with global side effects, its expressions are pure and has no effects.

- Constant folding:

$$2 : * 3 \implies 6.$$

- Short circuiting:

$$\text{If } (0 : < 1) \ a \ b \implies b.$$

- Algebraic simplifications:

$$x : + 0 \implies x, x : * 0 \implies 0.$$

- Reassociation and redistribution:

$$(x : + 2) : + 3 \implies x : + (2 : + 3) \implies x : + 5,$$

$$(x : + 3) : * 2 \implies x : * 2 : + 3 : * 2 \implies x : * 2 : + 6.$$

Dead code: a time to keep, and a time to cast away

- Detect statements, which can be entirely removed.
- The analysis goes *backwards* in terms of control flow, from the return statement up to the start.
- Transform as you go: if left-hand side reference is not *live set*, remove the statement at once. Otherwise remove LHS reference from *live set* and add RHS references.

```
                -- Live set
a = 1           -- {}
b = a + 2       -- {a}, remove
c = a + 3       -- {a}
d = b * 2       -- {c}, remove
ret = c         -- {c}
                -- {ret}
```

Dead code: loops

- Loops change control flow and are executed one or more times.
- Perform a dummy backward pass without stripping of statements to collect circular references.
- Then unite obtained live set with the live set at the end of loop and perform actual pass.

```
a = 0          -- {}
for i          a = 0          -- {}, remove
  b[i] = a      -- {a} / {a}  for i
  a = b[i] + 1  -- {b} / {b}    b[i] = a      -- {} / {}, remove
end            -- {b} / {a,b}  a = b[i] + 1  -- {} / {}, remove
r = 0          -- {b}          end            -- {} / {}
for i          r = 0          -- {}
  r = r + b[i]  -- {r,b} / {r,b} -- {r}
end            -- {r} / {r,b}
```

Inlining: a time to rend, and a time to sew

- Substitute RHS expression instead of LHS reference.
- The analysis goes *forward* in terms of control flow.
- Transform as you go: use the result of inlining for further substitutions.

Use cases:

- Always inline, when RHS is a constant or a reference.
- Always inline live variables, which are consumed only once.

```
data Liveness = One | Many
instance Semigroup Liveness where
  _ <> _ = Many
```

- Inline if it gives way to non-growing expression after local optimizations.

Inlining: example

```
a = 2
```

```
b = x + a
```

```
c = b
```

```
d = c + 1
```

```
e = c * 2
```

```
f = c ^ 3
```

```
g = d * e * f * f
```

```
a = 2
```

```
b = x + 2 -- inline constants
```

```
c = x + 2 -- b is a one-shot variable
```

```
d = x + 3 -- non-growing local optimization
```

```
e = c * 2 -- x * 2 + 4 is larger
```

```
f = c ^ 3 -- (x + 2) ^ 3 is larger
```

```
g = (x + 3) * (c * 2) * f * f
```

```
-- d and e are one-shot variables
```

Loop fusion: a time to break down and a time to build up

- Detect maps and folds in imperative code. Loops, which effect is invariant to permutation of iterations' order, are map. Other loops are fold.
- Fuse using map/map and map/fold rules.

```
for i
  y[i] = x[i] * 2
```

```
for i
  z[i] = y[i] * 3
```

$\text{map } f . \text{map } g = \text{map } (f . g)$

```
for i
  y[i] = x[i] * 2
  z[i] = y[i] * 3
```

Loop fusion: map/fold rule

```
for i
  y[i] = x[i] * 2
ret = 0
for i
  ret = ret + y[i] * 3
```

Shuffle blocks:

```
ret = 0
for i
  y[i] = x[i] * 2
for i
  ret = ret + y[i] * 3
```

$$\text{foldr } f \, x \cdot \text{map } g = \text{foldr } (f \cdot g) \, x$$

```
ret = 0
for i
  y[i] = x[i] * 2
  ret = ret + y[i] * 3
```

Loop fission - 1

```
ret = 0
for i
    y[i] = x[i] * 2
    ret = ret * 2 + y[i]
for i
    z[i] = y[i] * 3
```

Distribute first loop:

```
ret = 0
for i y[i] = x[i] * 2
for i ret = ret * 2 + y[i]
for i z[i] = y[i] * 3
```

Shuffle blocks:

```
ret = 0
for i y[i] = x[i] * 2
for i z[i] = y[i] * 3
for i ret = ret * 2 + y[i]
```

Loop fission - 2

```
ret = 0
for i y[i] = x[i] * 2
for i z[i] = y[i] * 3
for i ret = ret * 2 + y[i]
```

Apply map/map rule:

```
ret = 0
for i
  y[i] = x[i] * 2
  z[i] = y[i] * 3
for i
  ret = ret * 2 + y[i]
```

Apply map/fold rule:

```
ret = 0
for i
  y[i] = x[i] * 2
  z[i] = y[i] * 3
```

Thank you!