

# Earth and Mars Hypsometry

February 17, 2020

## 1 Hypsometry of Earth and Mars

*Note: For the interested or advanced user: The ETOPO5 data can be downloaded at: [ETOPO5](#) and information about the data can be obtained [here](#). Note that there is a new, high resolution dataset available [globally](#). But these data, however, are too large to perform fast calculations on them. Once you have downloaded the data, you can view them with ENVI or ArcMAP. I have used ENVI, to import the data with the following parameters (saved in the header file): Samples: 4320, Lines: 2160, Data Type: Integer, Byte Order: Network (IEEE). You can save the file as a Tif/Geotiff and import it into Matlab using either the command `importdata('ETOPO5.TIF')` or the using the menu File->Import data... ]*

*Alternatively, you can download a geotiff version of the [ETOPO5-geotiff](#).*

Obtain information about the DEM file with gdal. On the command line, you can use:

```
gdalinfo DEM_geotiff/alwdgg.tif | more
```

and you will obtain:

```
Driver: GTiff/GeoTIFF
Files: DEM_geotiff/alwdgg.tif
       DEM_geotiff/alwdgg.aux
       DEM_geotiff/alwdgg.tif.rrd
Size is 4320, 2160
Coordinate System is:
GEOGCS["Clarke_1866",
    DATUM["Clarke_1866",
        SPHEROID["Clarke 1866",6378206.4,294.9786982138982]],
    PRIMEM["Greenwich",0],
    UNIT["degree",0.0174532925199433]]
Origin = (-179.999994914978743,90.000002544373274)
Pixel Size = (0.0833333335816860,-0.0833333335816860)
Metadata:
  AREA_OR_POINT=Area
  TIFFTAG_RESOLUTIONUNIT=1 (unitless)
  TIFFTAG_SOFTWARE=IMAGINE TIFF Support
Copyright 1991 - 1999 by ERDAS, Inc. All Rights Reserved
@(#) $RCSfile: etif.c $ $Revision: 1.9.1.2 $ $Date: 2001/12/05 00:33:12Z $
  TIFFTAG_XRESOLUTION=1
  TIFFTAG_YRESOLUTION=1
```

Image Structure Metadata:

INTERLEAVE=BAND

Corner Coordinates:

Upper Left (-179.9999949, 90.0000025) (179d59'59.98"W, 90d 0' 0.01"N)

Lower Left (-179.9999949, -90.0000028) (179d59'59.98"W, 90d 0' 0.01"S)

Upper Right ( 180.0000158, 90.0000025) (180d 0' 0.06"E, 90d 0' 0.01"N)

Lower Right ( 180.0000158, -90.0000028) (180d 0' 0.06"E, 90d 0' 0.01"S)

Center ( 0.0000104, -0.0000001) ( 0d 0' 0.04"E, 0d 0' 0.00"S)

Band 1 Block=4320x1 Type=Int16, ColorInterp=Gray

Description = alwdgg

Min=-10376.000 Max=7833.000

Minimum=-10376.000, Maximum=7833.000, Mean=-1895.840, StdDev=2658.686

Overviews: 1078x538, 538x268, 268x133, 133x65, 65x31

Metadata:

LAYER\_TYPE=athematic

STATISTICS\_MAXIMUM=7833

STATISTICS\_MEAN=-1895.8397216797

STATISTICS\_MINIMUM=-10376

STATISTICS\_STDDEV=2658.6857910156

We note that no nodata value has been assign. We also see the projection information and pixel size. Next, Load data into Python and display. Here we use [richDEM](#) and [rd.LoadGDAL](#), but we could have used [gdal](#) and the [Python API](#) directly.

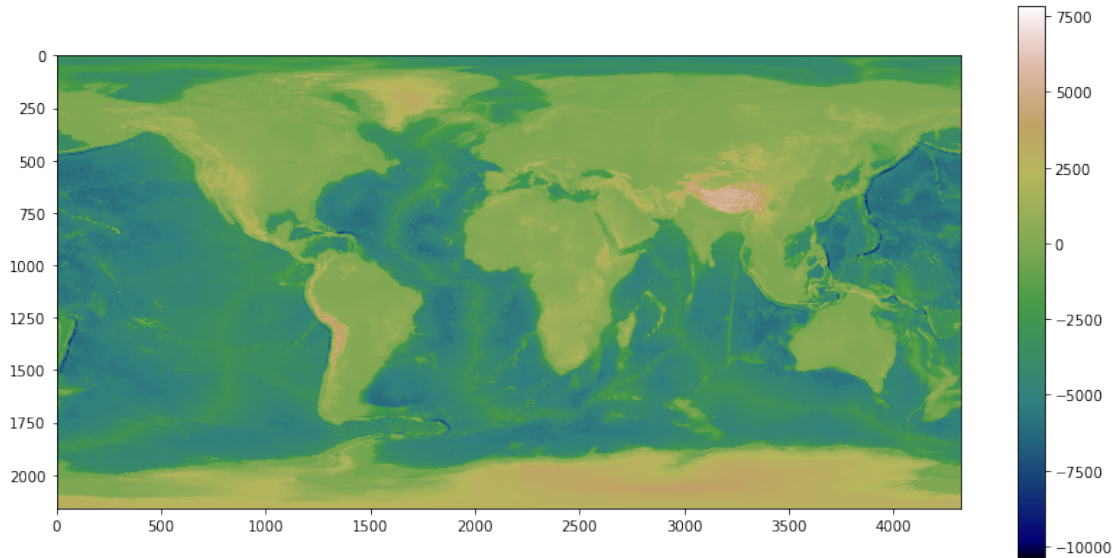
```
[5]: #import richdem as rd
#earth_dem = rd.LoadGDAL(earth_dem_fname, no_data=-32678)
#richdem not running on Windows systems, use gdal instead
#conda install gdal

import numpy as np
from matplotlib import pyplot as pl
pl.rcParams['figure.figsize'] = [14, 7]

from osgeo import gdal
earth_dem_fname='/home/bodo/Dropbox/Teaching/IITGn-QuantGeomorph_2020/github/
↳Earth/DEM_geotiff/alwdgg.tif'

ds = gdal.Open(earth_dem_fname, gdal.GA_ReadOnly)
rb = ds.GetRasterBand(1)
earth_dem = rb.ReadAsArray()

pl.imshow(earth_dem, interpolation='none', cmap='gist_earth')
pl.colorbar()
pl.show()
```



### Question: Plot a profile across the equator

We can obtain a histogram (hypsometry) of Earth using `np.hist` or directly with `matplotlib.pyplot.hist`.

A simple histogram using 100 equally-spaced bins (hypsometry of Earth):

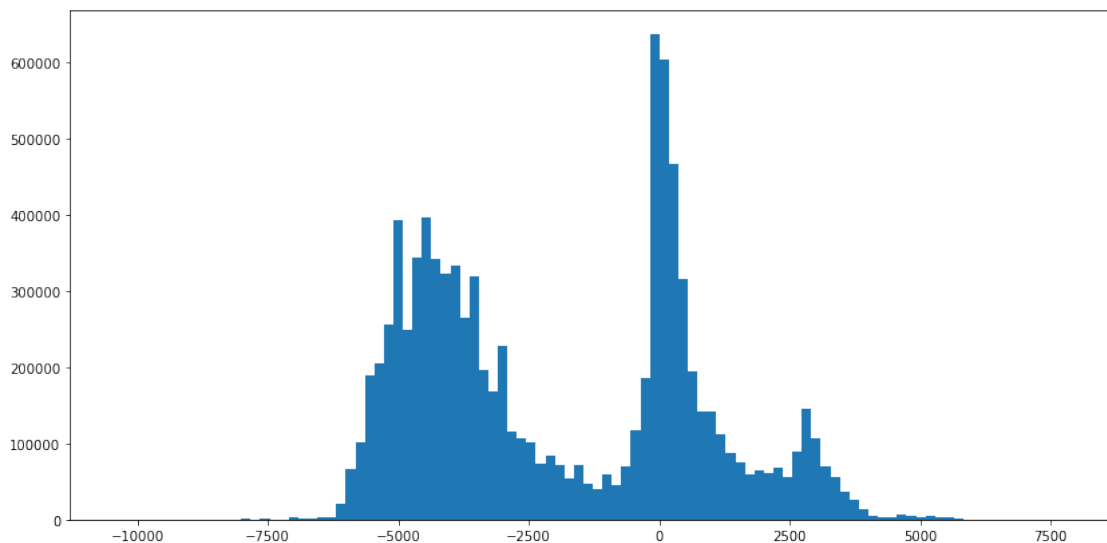
```
[7]: pl.hist(earth_dem.ravel(), bins=100)
```

```
[7]: (array([3.00000e+00, 5.00000e+00, 1.50000e+01, 2.00000e+00, 6.00000e+00,
4.20000e+01, 4.20000e+01, 2.26000e+02, 2.00000e+02, 1.03000e+02,
1.87000e+02, 1.40000e+02, 3.03000e+02, 9.53000e+02, 2.55000e+02,
5.75000e+02, 4.93000e+02, 4.53000e+02, 3.16100e+03, 1.07700e+03,
1.30300e+03, 2.87500e+03, 2.71300e+03, 2.14850e+04, 6.68590e+04,
1.01532e+05, 1.89160e+05, 2.05411e+05, 2.55997e+05, 3.92635e+05,
2.49754e+05, 3.43994e+05, 3.96398e+05, 3.42630e+05, 3.23799e+05,
3.33791e+05, 2.64363e+05, 3.20423e+05, 1.96603e+05, 1.68757e+05,
2.28883e+05, 1.16071e+05, 1.06691e+05, 1.01195e+05, 7.28270e+04,
8.43160e+04, 7.14010e+04, 5.36310e+04, 7.23910e+04, 4.79100e+04,
3.96860e+04, 6.01070e+04, 4.47890e+04, 6.95240e+04, 1.16677e+05,
1.85904e+05, 6.37050e+05, 6.04667e+05, 4.67142e+05, 3.16942e+05,
1.94659e+05, 1.42417e+05, 1.42865e+05, 1.12067e+05, 8.67240e+04,
7.52730e+04, 5.88670e+04, 6.54750e+04, 6.17870e+04, 6.77340e+04,
5.53450e+04, 8.91890e+04, 1.45858e+05, 1.07678e+05, 6.98980e+04,
5.66750e+04, 3.68140e+04, 2.57010e+04, 1.30100e+04, 4.58900e+03,
3.48100e+03, 2.90200e+03, 5.87900e+03, 4.65200e+03, 3.13000e+03,
5.08500e+03, 2.45800e+03, 3.09700e+03, 9.09000e+02, 2.06000e+02,
1.82000e+02, 2.50000e+01, 3.20000e+01, 7.00000e+00, 0.00000e+00,
1.00000e+00, 0.00000e+00, 1.00000e+00, 0.00000e+00, 1.00000e+00]),
```

```

rdarray([-1.037600e+04, -1.019391e+04, -1.001182e+04, -9.829730e+03,
        -9.647640e+03, -9.465550e+03, -9.283460e+03, -9.101370e+03,
        -8.919280e+03, -8.737190e+03, -8.555100e+03, -8.373010e+03,
        -8.190920e+03, -8.008830e+03, -7.826740e+03, -7.644650e+03,
        -7.462560e+03, -7.280470e+03, -7.098380e+03, -6.916290e+03,
        -6.734200e+03, -6.552110e+03, -6.370020e+03, -6.187930e+03,
        -6.005840e+03, -5.823750e+03, -5.641660e+03, -5.459570e+03,
        -5.277480e+03, -5.095390e+03, -4.913300e+03, -4.731210e+03,
        -4.549120e+03, -4.367030e+03, -4.184940e+03, -4.002850e+03,
        -3.820760e+03, -3.638670e+03, -3.456580e+03, -3.274490e+03,
        -3.092400e+03, -2.910310e+03, -2.728220e+03, -2.546130e+03,
        -2.364040e+03, -2.181950e+03, -1.999860e+03, -1.817770e+03,
        -1.635680e+03, -1.453590e+03, -1.271500e+03, -1.089410e+03,
        -9.073200e+02, -7.252300e+02, -5.431400e+02, -3.610500e+02,
        -1.789600e+02,  3.130000e+00,  1.852200e+02,  3.673100e+02,
        5.494000e+02,  7.314900e+02,  9.135800e+02,  1.095670e+03,
        1.277760e+03,  1.459850e+03,  1.641940e+03,  1.824030e+03,
        2.006120e+03,  2.188210e+03,  2.370300e+03,  2.552390e+03,
        2.734480e+03,  2.916570e+03,  3.098660e+03,  3.280750e+03,
        3.462840e+03,  3.644930e+03,  3.827020e+03,  4.009110e+03,
        4.191200e+03,  4.373290e+03,  4.555380e+03,  4.737470e+03,
        4.919560e+03,  5.101650e+03,  5.283740e+03,  5.465830e+03,
        5.647920e+03,  5.830010e+03,  6.012100e+03,  6.194190e+03,
        6.376280e+03,  6.558370e+03,  6.740460e+03,  6.922550e+03,
        7.104640e+03,  7.286730e+03,  7.468820e+03,  7.650910e+03,
        7.833000e+03]),
<a list of 100 Patch objects>)

```



**Question:** Change the binning parameters to obtain bins spaced in 250-m elevation

slices

**Question:** We have used a geographic projection system. This is distorted at the higher latitude. It will be more useful to have an equal-area projection such as Mollweide. Either use 'gdal' to convert the projection or load the data contained in ETOP05\_dem\_mollweide\_geotiff.zip. Make sure to properly assign the nodata value and repeat the binning analysis (results with not be very different, but more accurate.

```
[ ]: bins_250m = np.linspace(-10000,10000, 250)
```

## 2 Hypsometry of Mars

Next, we load a DEM of Mars. There is a high resolution [MARS MOLA DEM](#) available (1000 m spatial resolution) that I prepared. But this is of high resolution and the analysis performed on this file may take a little longer. Instead, we will rely on a 5000m DEM of Mars mola128\_mola64\_merge\_90Nto90S\_SimpleC\_clon0\_5000m\_bilinear.tif. But feel free to experiment with other resolution data. Again, we first obtain information about the geotiff file:

```
gdalinfo mola128_mola64_merge_90Nto90S_SimpleC_clon0_5000m_bilinear.tif
```

with the following output:

```
Driver: GTiff/GeoTIFF
Files: mola128_mola64_merge_90Nto90S_SimpleC_clon0_5000m_bilinear.tif
Size is 4268, 2134
Coordinate System is:
PROJCS["Mars2000_ECylindrical_clon0",
  GEOGCS["GCS_Mars_2000_Sphere",
    DATUM["Mars_2000_Sphere",
      SPHEROID["Mars_2000_Sphere",3396190,0]],
    PRIMEM["Reference_Meridian",0],
    UNIT["degree",0.0174532925199433]],
  PROJECTION["Equiarectangular"],
  PARAMETER["latitude_of_origin",0],
  PARAMETER["central_meridian",0],
  PARAMETER["standard_parallel_1",0],
  PARAMETER["false_easting",0],
  PARAMETER["false_northing",0],
  UNIT["metre",1,
    AUTHORITY["EPSG","9001"]]]
Origin = (-10669677.095995118841529,5334954.318897561170161)
Pixel Size = (5000.000000000000000,-5000.000000000000000)
Metadata:
  AREA_OR_POINT=Area
  DataType=Generic
Image Structure Metadata:
  COMPRESSION=DEFLATE
  INTERLEAVE=BAND
```

Corner Coordinates:

Upper Left (-10669677.096, 5334954.319) (179d59'45.94"E, 90d 0'14.06"N)

Lower Left (-10669677.096, -5335045.681) (179d59'45.94"E, 90d 0'19.61"S)

Upper Right (10670322.904, 5334954.319) (179d59' 6.71"W, 90d 0'14.06"N)

Lower Right (10670322.904, -5335045.681) (179d59' 6.71"W, 90d 0'19.61"S)

Center ( 322.904, -45.681) ( 0d 0'19.61"E, 0d 0' 2.77"S)

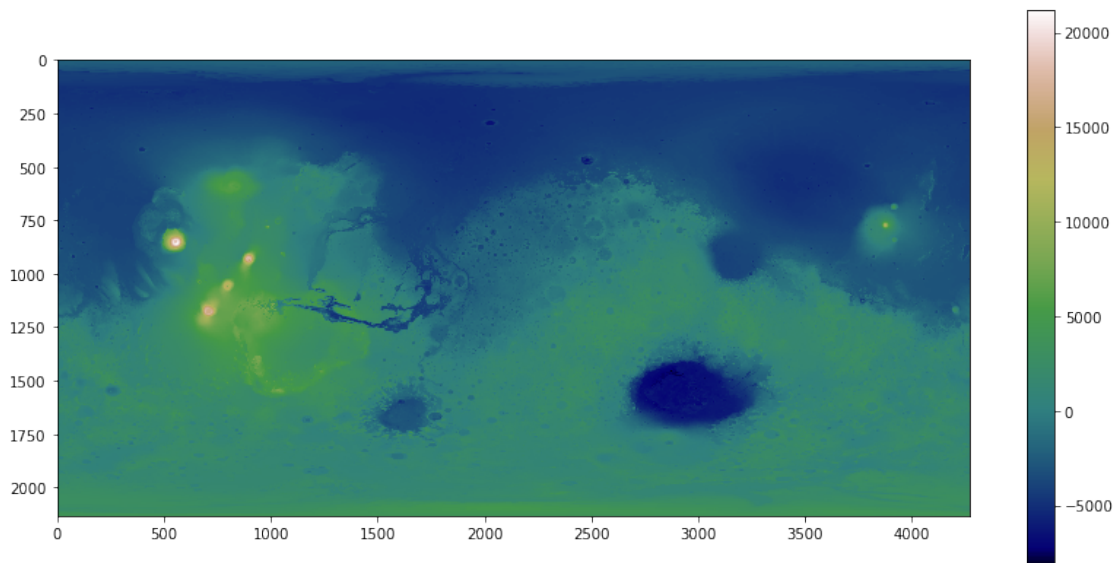
Band 1 Block=4268x1 Type=Int16, ColorInterp=Gray

NoData Value=-32768

[ ]:

```
[6]: mars_dem_fname='/home/bodo/Dropbox/Teaching/IITGn-QuantGeomorph_2020/github/  
      ↪Earth/mola128_mola64_merge_90Nto90S_SimpleC_clon0_5000m_bilinear.tif'  
      #mars_dem = rd.LoadGDAL(mars_dem_fname, no_data=-32768)
```

```
ds = gdal.Open(mars_dem_fname, gdal.GA_ReadOnly)  
rb = ds.GetRasterBand(1)  
mars_dem = rb.ReadAsArray()  
pl.imshow(mars_dem, interpolation='none', cmap='gist_earth')  
pl.colorbar()  
pl.show()
```



**Question:** What geomorphic/tectonic features do you observe on Mars?

**Question:** Calculate the hypsometry of Mars and make one plot that combines Earth's and Mars' Hypsometries. Why are they different?

**Question:** Compare the slope distribution of Mars and Moon. How and why are these different?

You can either use the numerical slope function we have created before or you use the [Terrainattributes function](#) included in [richDEM](#). For example:

```
slope = rd.TerrainAttribute(mars_dem, attrib='slope_riserun')
rd.rdShow(slope, axes=False, cmap='magma', figsize=(8, 5.5))
plt.show()
```

**Question:** A lot of information is contained in 2D histogram. You can evaluate slope and elevation (i.e., what slope dominates at what elevation) using a 2D kernel density estimator. See [here](#).

**Question:** The directory contains a DEM of Moon - load this and calculate hypsometry as well