

Problem

Suppose you are an economist analyzing the economy of AlphaLand, a small country.

Consumption expenditure in AlphaLand for the current year is \$40 billion. Foreign direct investment (FDI) in AlphaLand for the current year is \$15 billion. Government expenditure for the current year is \$20 billion. AlphaLand is a net importer, meaning its imports exceed its exports. The trade deficit for the current year is \$9 billion.

There's a:

- 40% chance that consumption will decrease by 60% and a 60% chance it will decrease by 30 billion.
- 30% chance that investment will decrease by 20% and a 70% chance it will remain unchanged.
- 50% chance that government spending will decrease by 40% and a 50% chance it will decrease by 10 billion.
- 60% chance that net exports will decrease by \$2 billion and a 40% chance they will remain unchanged.

Determine the expected GDP of AlphaLand for the upcoming year, rounded to the nearest billion, and calculate the fraction: $\frac{GDP}{10}$.

Solution

Next year's expected:

$$\text{Consumption (C)} = 40\% \cdot (40 - 60\% \cdot 40) + 60\% \cdot 10 = 12.4$$

$$\text{Foreign Investment (I)} = 30\% \cdot (15 - 20\% \cdot 15) + 70\% \cdot 15 = 14.1$$

$$\text{Government Spending (G)} = 50\% \cdot (20 - 40\% \cdot 20) + 50\% \cdot 10 = 11$$

$$\text{Net Exports (NX)} = -1 \cdot [60\% \cdot (9 - 2) + 40\% \cdot 9] = -7.8 \text{ (minus because it is a deficit)}$$

$$GDP = C + I + G + NX$$

$$GDP = 12.4 + 14.1 + 11 - 7.8 = 29.7 \approx 30 \text{ billion}$$

$$\frac{GDP}{10} = \frac{30}{10} = 3$$

Answer: 3