

## Greek alphabet

$\Sigma$	Sigma	Set of alphabet symbols
$\Gamma$	Gamma	Set of stack/tape symbols
$\alpha$	alpha	
$\beta$	beta	
$\gamma$	gamma	
$\delta$	delta	Transition function
$\varepsilon$	epsilon	Empty string
$\sigma$	sigma	

## Strings

$w$	String made of symbols from $\Sigma$
$w^R$	String obtained by writing $w$ in the reverse order
$ w $	Length of the string $x$
$xy$	String made by concatenating $x$ and $y$
$w^n$	String made by concatenating $n$ copies of $w$ : $\underbrace{ww \dots w}_{n \text{ copies}}$

In particular:  $w^0 = \varepsilon$ ,  $w^1 = w$  and  $w^2 = ww$

$\{0, 1\}^n$	Binary strings of length exactly $n$ symbols
$\{0, 1\}^*$	Binary strings of any length: $\{\varepsilon, 0, 1, 00, 01, 10, 11, 000, \dots\}$

## Regular expressions

$\square + \square$	Union ("or")	
$\square \square$	Concatenation ("glueing" two strings)	(juxtaposition/no symbol)
$\square^*$	Star (zero or more copies)	e.g. $1^* = \{\varepsilon, 1, 11, 111, 1111, \dots\}$
$\square^+$	One or more copies – shorthand for $\square \square^*$	e.g. $1^+ = \{1, 11, 111, 1111, \dots\}$
$\Sigma^*$	Any string of finite length over the given alphabet, including $\varepsilon$	(zero length)
$\Sigma^+$	Any string of finite non-zero length over the given alphabet	(not $\varepsilon$ )
$()$	Grouping, to override usual precedence rule: <i>star, concatenation, union</i>	
$\varepsilon$	Empty string	
$\emptyset$	No strings at all	

## Set and logic notation

$\{x_1, \dots, x_n\}$	Finite set consisting of the elements $x_1$ until $x_n$
$\{pattern \mid condition\}$	Set of items matching <i>pattern</i> and satisfying <i>condition</i> . The $\mid$ symbol is read “such that”
$\emptyset$	Empty set, i.e. $\{\}$
$\in$	“in”, member of a set
$\notin$	“not in”, not a member of a set
$\cup$	Union of two sets
$\cap$	Intersection of two sets
$-$	Difference of two sets
$\times$	Cartesian product of two sets
$\subset$	Subset of ...
$ A $ or $\#A$	Cardinality of the set $A$ , i.e. count of its elements
$2^A$	Power set of $A$ , i.e. set of all subsets of $A$
$\wedge$	Logical “and”
$\vee$	Logical “or”
$\neg$ or $\neg$	Logical “no”
$\oplus$	Logical “xor” – “exclusive or”
$\mathbb{N}$	Natural numbers: $\{1, 2, 3, \dots\}$
$\mathbb{Z}$	Integers: $\{0, 1, -1, 2, -2, 3, -3, \dots\}$
$\mathbb{Z}_{\geq 0}$	Non-negative integers: $\{0, 1, 2, 3, \dots\}$
$S'$	A set called “ $S$ prime” (a way of making new names)
$S''$ or $S'''$	A set called “ $S$ double prime” / “ $S$ triple prime”

## Numeric

$=$	equals
$\neq$	not equal
$<$	less than
$\leq$	less than or equal
$>$	greater than
$\geq$	greater than or equal
$n!$	Factorial of $n$ : $n \times (n-1) \times (n-2) \times \dots \times 2 \times 1$